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D. P. Schmidt

T. H. Okiishi



MULTISTAGE AXIAL-FLOW TURBOMACHINE WAKE PRODUCTION, TRANSPORT, AND INTERACTION

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Interim Report

MULTISTAGE AXIAL-FLOW TURBOMACHINE WAKE PRODUCTION, TRANSPORT, AND INTERACTION

> D. P. Schmidt T. H. Oklishi

November 1976

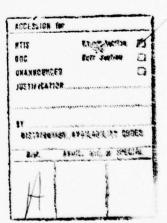
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SUMMARY

The first year results of a study of multistage axial-flow turbomachine wake production, transport and interaction are described in this report. Evidence indicating how the noise level measured at the inlet of a low speed, multistage, axial-flow research compressor was found to vary appreciably with inlet guide vane and stator row relative circumferential positioning with the largest amount of noise reduction occurring at the blade passing frequency is presented. The results of detailed slow- (cobra probe and surface pressure taps) and fast-response (hot-wire) measurements made within the research compressor flow field to aid in understanding the physics involved are shown in scalar and vector plots and tables. Significant local changes in blade-section aerodynamic performance and flow field appearance with variation in stationary blade row placement were observed although corresponding improvement of overall efficiency could not be ascertained. Several interesting periodically unsteady aspects of the flow field and its measurement are demonstrated and some conclusions about blade row interaction are proposed.

TABLE OF CONTENTS

			Page
	ACK	NOWLEDGEMENTS	ii
	SUM	MARY	iii
I.	INT	PRODUCTION	1
II.	DIR	ECTLY RELATED RESEARCH	3
	Α.	Blade Interaction Effects	3
	В.	Experimental Procedures and Instrumentation	8
111.	RES	EARCH COMPRESSOR FACILITY	12
	Α.	Multistage Axial-Flow Research Compressor	12
	В.	Probe and Stationary Blade-Row Actuators	20
	С.	Pressure and Temperature Sensing Instrumentation	22
	D.	Fast-Response Measurement System	23
	Ε.	Calibration Nozzle	26
	F.	Sound-Pressure Level (SPL) Measurement Instrumentation	27
	G.	Data Acquisition and Reduction System	27
IV.	EXP	PERIMENTAL PROCEDURES AND DATA REDUCTION	30
	Α.	Sound-Pressure Level (SPL) Measurements	31
		 Testing for noise variation over compressor rpm range 	31
		Determining the minimum and maximum sound settings	33
		 Obtaining detailed SPL measurements at minimum and maximum sound-level blade-row settings 	34
	В.	Slow-Response Measurements	34
		1. Probe calibration	34
		a. Total pressure calibrationb. Probe yaw-angle calibrationc. Kiel probe comparison	36 37 40

				Page
		2. 3.	Data acquisition Data reduction	40 43
			a. Flow-field parameters	43
			 Rotor, stator, and stage performance parameters 	47
	С.	Fas	t-Response Measurements	47
		1. 2.	Periodic sampling and averaging technique	47
		۷.	Single hot-wire three-dimensional velocity measurement technique	51
			a. Probe geometry	53
			 Effective cooling velocity/actual velocity ratio 	55
			c. Measurement technique	58
		3.	Calibration procedure	63
			a. Linearizer velocity calibration	64
			b. Second order velocity calibrationc. Effective cooling velocity calibration	65 66
		4.	Data acquisition Data reduction	68 75
٧.	PRE	SENT	TATION AND DISCUSSION OF DATA	78
	Α.	Sou	nd-Pressure Level Measurement Results	78
	В.	S1o	w-Response Measurement Results	84
	С.	Fas	t-Response Measurement Results	126
VI.	CON	CLUS	IONS	155
VII.	REC	OMME	NDATIONS FOR FUTURE RESEARCH	158
VIII.	BIB	LIOG	RAPHY	161
IX.	SYN	IBOLS	S AND NOTATION	164
х.	APP	ENDI	X A: PERIODIC-SAMPLING CIRCUIT DESIGN	169
XI.	APP	ENDI	X B: CALCULATOR PROGRAMS AND DATA STORAGE	174

			Page
XII.	APP	ENDIX C: PARAMETER EQUATIONS	176
	Α.	General Parameters	176
		 Basic fluid properties Blade-element quantity Miscellaneous 	176 178 178
	В.	Slow-Response Instrument Parameters	178
		 Point and circumferential-average blade- element quantities Global parameters 	178 182
	С.	Three-Dimensional Fast-Response Hot-Wire Parameters	183
XIII.	APP	ENDIX D: LEAST SQUARES EMPIRICAL CORRELATION FOR EFFECTIVE COOLING VELOCITY RATIO	185
XIV.	APP	ENDIX E: TABULATION OF SLOW-RESPONSE DATA	188
XV.	APF	ENDIX F: TABULATION OF FAST-RESPONSE HOT-WIRE DATA	210

LIST OF FIGURES

			Page
Figure 3	.1.	Driving motor and research compressor.	13
Figure 3	.2.	The axial-flow compressor rig.	14
Figure 3	.3.	Blade nomenclature.	16
Figure 3	.4.	Compressor blading.	17
Figure 3		Schematic diagram showing axial location of probe measurement stations (dimensions in mm).	18
Figure 3	.6.	Research compressor apparatus side view.	19
Figure 3	.7.	Probe and stationary blade-row actuators.	21
Figure 3		Schematic setup diagram of fast-response measurement system.	24
Figure 3		Calibration nozzle, probe positioner, and optical alignment telescope used for probe calibration.	28
Figure 4		Sound-level meter and position of microphone for compressor inlet noise measurement.	32
Figure 4		Total-pressure and flow-yaw-angle cobra probe and probe angle nomenclature.	35
Figure 4	.3.	Cobra probe total-pressure calibration curves.	38
Figure 4	.4.	Cobra probe yaw angle sensitivity calibration curve.	39
Figure 4	.5.	Cobra and Kiel probe comparison.	39
Figure 4		Static-pressure radial equilibrium solution for the compressor behind the third stator.	46
Figure 4		Percent variation coefficient of the periodic- sample averages for different values of N.	52
Figure 4	.8.	Hot-wire configuration relating velocity vector \vec{V} to hot-wire sensor and probe coordinates x, y, z.	54
Figure 4	.9.	Typical effective cooling velocity calibration results for a 35.35 degree inclined hot-wire.	57

			Page
Figure	4.10.	Hot-wire measurement positions and nomenclature, viewed from above along probe axis.	61
Figure	4.11.	Probe actuator positioned at calibration nozzle for hot-wire velocity calibration.	72
Figure	4.12.	Compressor coordinate system showing nomenclature and sign convention for three-dimensional fast-response velocity and angle parameters.	76
Figure	4.13.	Hot-wire measurement positions with respect to compressor coordinates ${\bf Y}$ and ${\bf Z}$.	76
Figure	5.1.	Compressor inlet noise level over compressor rpm range.	79
Figure	5.2.	Required noise reductions for subjective improvement from Sofrin (11).	82
Figure	5.3.	Compressor inlet noise spectrum (1% filter bandwidth).	83
Figure	5.4.	Blade-to-blade plane, time-average, velocity vector plot for first stator at mid-span (constructed from slow-response data).	85
Figure	5.5.	Blade-to-blade plane, time-average, velocity vector plots at constant passage height for the minimum sound blade-row schedule; constructed from slow-response data.	87
Figure	5.6.	Blade-to-blade plane, time-average, velocity vector plots at constant passage height for the maximum sound blade-row schedule; constructed from slow-response data.	96
Figure	5.7.	Circumferential-average axial velocity blade span distribution.	107
Figure	5.8.	Circumferential-average absolute tangential velocity blade span distribution.	108
Figure	5.9.	Circumferential-average absolute tangential flow angle blade span distribution.	109
Figure	5.10.	Blade span distribution of total-head-loss coefficient for rotor and stator blade rows.	110

		Page
Figure 5.11.	Blade span distribution of incidence and deviation blade angles, rotor and stage head-rise coefficient and hydraulic efficiency.	113
Figure 5.12.	Comparison of slow-response and fast-response data behind the first stator.	128
Figure 5.13.	Mid-span slow-response instrument averaged velocity vector variation for first stator with inlet guide vane wake streets shown.	129
Figure 5.14.	Multiple oscilloscope traces of hot-wire signal for location \boldsymbol{A} .	131
Figure 5.15.	Multiple oscilloscope traces of hot-wire signal for location $\ensuremath{\mathtt{B}}.$	132
Figure 5.16.	Circumferential distribution of periodic-average flow field parameters behind the first rotor at 50% passage height for locations A and B, obtained with rotor-passing survey method.	133
Figure 5.17.	Circumferential distribution of periodic-average flow field parameters obtained at different rotor positions with frozen rotor-blade flow-field sur- vey method.	135
Figure 5.18.	Blade-to-blade velocity vector plots obtained at different rotor positions with frozen rotor-blade survey method.	141
Figure 5.19.	Circumferential distribution of periodic-average flow field parameters obtained at different radial positions with frozen rotor-blade survey method.	150
Figure 5.20.	Blade-to-blade velocity vector plots obtained at different radial positions with frozen rotor-blade survey method.	152
Figure 10.1.	Block diagram of periodic-sampling circuit.	166
Figure 10.2.	Circuit diagram of triggering and sample-and-hold circuits.	167
Figure 10.3.	Power supply for triggering and sample-and-	168

			Page
Figure	10.4.	Interfacing cable connections.	169
Figure	12.1.	Sketch showing nomenclature, sign convention, and velocity triangles for slow-response	
		instrument parameters.	177

LIST OF TABLES

			Page
Table	3.1.	Geometric blade details for IGV, rotors and stators at several radial locations.	16
Table	4.1.	Specifications for periodic-average hot-wire circum- ferential surveys, all measurements were made at the minimum sound stationary blade-row schedule.	69
Table	5.1.	Stationary blade-row circumferential placement schedules for minimum and maximum sound.	81
Table	5.2.	Overall and octave band analyses of compressor inlet noise for minimum and maximum noise blade-row schedules.	81
Table	5.3.	Uncertainty levels of slow-response parameters.	121
Table	5.4.	Flow rate comparison between venturi and integrated measurement station flow rates.	122
Table	5.5.	Uncertainty and scatter of periodic-average flow field parameters.	127
Table	13.1.	Equation 13.14.	187
Table	14.1.	Point-by-point circumferential distributions of total head for minimum noise condition.	189
Table	14.2.	Point-by-point circumferential distribution of total head for maximum noise condition.	197
Table	14.3.	Blade-to-blade circumferential-average values of total head, static head, tangential flow angle, and incidence and deviation angles for minimum noise condition.	205
Table	14.4.	Blade-to-blade circumferential-average values of total head, static head, tangential flow angle, and incidence and deviation angles for maximum noise condition.	207
Table	14.5.	Circumferential-average outer-annulus-surface static head for minimum and maximum noise conditions.	209
			20)

		Page
Table 15.1.	Fast-response circumferential survey data obtained with frozen rotor-blade survey method at minimum noise condition.	211
Table 15.2.	Fast-response circumferential survey data obtained with passing rotor-blade survey method at minimum noise condition.	221

I. INTRODUCTION

Although most modern multistage turbomachine design procedures are very sophisticated in many respects, they remain incomplete because of our present inability to consistently determine some important details of the complicated fluid flow field involved. For example, the general calculation of spatial and unsteady (periodic and random) changes of the turbomachine flow field and blade response with enough detail and precision to avoid undesirable acoustic and aeromechanical performance is still a major unresolved problem. Further, the total-pressure losses and flow turning angles precisely required by all modern computer based turbomachine design procedures are often very difficult to predict well, especially under off-design operation conditions. At best, limited empirical correlations are relied on.

One way to improve the design and reliability of turbomachines is to gain a better understanding of the fluid mechanics involved via fundamental laboratory experiments. In particular, an understanding of the unsteady interaction that occurs between moving and stationary blade rows via viscous wake and potential flow effects would provide valuable design information with respect to aeroelastic stability and noise generation. The details of blade wake production and transport are important aspects of the viscous wake interaction process. This kind of information is, however, not readily available in the open literature. For example, little is published concerning the effects of relative circumferential positioning of the blade rows in an axial-flow multistage turbomachine on the aerodynamic, acoustic, and aeromechanical characteristics of the

machine. Work in this area indicates that the rotor and stator flow fields in multistage turbomachines can be considerably influenced by the relative circumferential position of the stationary blade rows. In the research compressor used in the present investigation, the sound level at the compressor inlet could be varied significantly by adjusting the circumferential positions of the stationary blade rows relative to each other.

The primary purpose of the present research project was to experimentally investigate the three-dimensional, unsteady fluid flow field within a low-speed, three-stage, axial-flow research compressor in order to develop a better understanding of the fluid physics involved. To gain an appreciation for the unsteady flow effects of blade wake production, transport, and interaction, slow-response and fast-response instrument data were obtained between the blade rows of the research compressor. Time-average flow field measurements were obtained with a slow-response pressure and flow-angle probe throughout the compressor at two distinct stationary blade row circumferential placement schedules corresponding to minimum and maximum compressor inlet noise levels. In addition, a hot-wire measurement technique was developed and three-dimensional periodic-average measurements were made of the unsteady flow field to obtain further details of the flow.

Although some of the specific results obtained to date are peculiar to the research compressor configuration involved, the general concepts developed are applicable to all multistage axial-flow turbomachines.

II. DIRECTLY RELATED RESEARCH

A. Blade Interaction Effects

The effects and importance of the interaction between blade rows have been considered by numerous individuals. (See for example Meyer (1), Smith (2), Kerrebrock and Mikolajczak (3), Parker and Watson (4), Walker and Oliver (5), Kiock (6), Lockhart and Walker (7), and Mikolajczak (8).) Blade row interaction appears to be of particular importance when turbomachine performance and blade vibration and noise generation improvements are sought. It is also possible that blade interaction effects could significantly influence cavitation occurrence in hydraulic turbomachines and blade surface heat transfer rates in gas turbines. The interaction can involve blade rows several stages apart (2,4) as well as those that are adjacent to each other. Basically, there are two recognized types of interaction, a viscous wake one which primarily is a result of downstream blades cutting through the wakes of upstream blades, and a potential flow one which would be present even if the working fluid was inviscid. Both types of blade interaction can play important roles in the development of the unsteady flow field and subsequent consequences in a turbomachine. Data presented by Fincher (9) and Doak and Vaidya (10) suggest that the importance of potential flow interaction becomes insignificant in comparison to viscous wake interaction when the axial blade row spacing is 30% or greater of the blade chord. As indicated by Sofrin (11), the interaction phenomena involve periodic events at blade passing frequency and harmonics as well as random occurrences. According to Evans (12) and Raj and Lakshminarayana (13), periodic and random unsteadiness

values are of the same order of magnitude near design point operation.

Evans (12) further concluded that random unsteadiness becomes most important near stall. As pointed out by Horlock (14), the work of Tyler and Sofrin (15) on the rotating adjacent blade row interaction pressure pattern is an outstanding accomplishment of the past. Their conclusion relating the speed of spinning acoustic patterns to duct sound propagation is well accepted and is applied in present design procedures.

Blade row interaction is obviously related to the manner in which fluid is transported through a blade row. Several individuals including Smith (2), Walker and Oliver (5), Okapuu (16), and Lockhart and Walker (7) have found experimentally that the rotor exit flow can be significantly influenced by a periodic flow pattern at the rotor inlet from an upstream stationary blade row such as inlet guide vanes, stators or nozzles. Stationary periodic flow patterns were observed to propagate through the rotor row, and considerable viscous wake interactions were identified in some instances. Smith (2) offered a qualitative description of the wake interaction phenomenon between an upstream stationary blade row and a downstream rotor blade row, and provided a means for calculating some of the geometrical aspects of the flow. He proposed that as the wakes from the upstream stationary blade row move through the rotor row, they are affected not only by viscous action but also by dispersive wake chopping and uneven energy addition. The chopping action results from the rotor blades cutting through and reorienting the upstream flow disturbance, while the uneven energy addition results from the wake fluid residing in the rotor longer than the freestream fluid. Qualitative hot-wire

anemometer measurements obtained in a four-stage, low-speed, axial-flow compressor behind the first rotor at the mean diameter were displayed by Smith (2) to illustrate how the rotor exit flow field varies with circumferential position because of the influence of the IGV blade wakes on the rotor exit flow. In addition, Smith (2) observed that the flow pattern behind the third rotor could be altered significantly by circumferentially moving the IGV row. Savell and Wells (17) have shown that the attenuation of a stationary periodic flow variation (produced, for example, by an upstream stationary blade row) through a rotor blade probably depends upon a number of variables including distortion wave length and rotor design characteristics (chord length, solidity, loading, flow Mach number levels and angles, blade angle, and flow passage annulus shape). Measurements made by Walker and Oliver (5) on a single-stage (IGV-rotor-stator combination), low-speed axial-flow compressor with the same number of IGV and stator blades showed that considerable reduction of compressor inlet noise (at blade passing frequency) could be achieved with appropriate circumferential positioning of the IGV and stator blade rows relative to each other. They claimed that the noise reduction was due to a combination of blade section pressure fluctuation reduction and sound wave interference. Further measurements by Lockhart and Walker (7) in the same research compressor, indicate that the mean velocity, apparent turbulence levels. and rotor wake decay rate all varied periodically in the circumferential direction as a result of the IGV and rotor wake interaction. A simple physical model of the wake interaction process was proposed by these authors on the basis of their slow and fast response instrument measurements. Kerrebrock and Mikolajczak (3) offered an explanation of the

experimentally observed stagnation temperature variations in the tangential direction downstream of stators in high Mach number compressor stages. They proposed that the transport of rotor wakes through the stator row is the cause of this phenomenon and presented a wake transport theory. While the experimental evidence presented by the authors in support of their theory is convincing, Lockhart and Walker (7) concluded that the analysis is not appropriate in a multistage turbomachine because of the significant wake-to-wake interactions that can occur upstream of a stator.

Also related to blade row interaction are the detailed characteristics of rotor and stator wakes. Important research on this aspect includes the works of Whitfield et al. (18), Lockhart and Walker (7), Evans (12), Raj and Lakshminarayana (13), Thompkins and Kerrebrock (19), and Hirsch and Kool (20). Lockhart and Walker (7) concluded that because rotor wake apparent turbulence level decay can vary significantly with circumferential position, the rotor wake should not be modeled by the wake decay behind an isolated airfoil or a single cascade as is commonly assumed in current blade row interaction theories. In one instance, they observed that rotor wake turbulence level increased instead of decayed with distance downstream. Raj and Lakshminarayana (13) compared isolated rotor wake decay data with those for an isolated airfoil and a cascade of aerofoils, and found that the rotor wake velocity defect, turbulence intensities, and Reynolds stresses decayed much faster. Further, they found that the anisotropy, the magnitude of turbulence intensities, and the Reynolds stresses associated with an isolated rotor blade wake are much higher than those of a cascade blade wake. Based on their measurements,

Raj and Lakshminarayana (13) developed an approximate quasi-threedimensional turbulent wake model for a turbomachine rotor blade. Lieblein and Roudebush (21) found that the downstream variations of turbulent cascade and isolated airfoil wake characteristics (minimum velocity, form factor, full thickness, and total pressure loss) were generally similar. Parker and Watson (4) indicate that preliminary comparisons of uncambered C4 airfoil cascade velocity defect decay data and isolated airfoil wake data calculated after Silverstein et al. (22) do not compare favorably. Raj and Lakshminarayana (13) concluded that a cascade blade wake differs from that of a cylinder, a flat plate and an isolated and symmetrical airfoil at zero incidence in several ways. Several researchers (see Refs. 13, 18, 19, 20) noted that the radial velocities in rotor wakes are significant due to an imbalance of centrifugal and pressure forces inside the wakes. Further, substantial variations in downstream stator incidence angle were observed by Evans (12). Thompkins and Kerrebrock (19) claimed that large static pressure variations can occur in rotor wakes. The data of Whitfield et al. (18), Raj and Lakshminarayana (13), Thompkins and Kerrebrock (19), and Hirsch and Kool (20) indicated that substantial variations may occur in rotor wake characteristics in the spanwise direction. Raj and Lakshminarayana (13) showed the variation of wake halfwidth decay with radius. Thompkins and Kerrebrock (19) presented numerous rotor exit flow field contour plots illustrating radial and circumferential variations of total pressure, static pressure, radial, axial, and tangential Mach numbers, total temperature, and entropy rise at 0.1 and 1.0 chord downstream of the rotor. Whitfield et al. (18) and Hirsch and Kool (20) showed three-dimensional velocity vector plots as well as more

conventional scalar graphs which demonstrate the spanwise variations in rotor wake velocities. Additionally, Whitfield et al. (18) offered rotor blade row exit flow field contour plots to display radial and circumferential variations of absolute velocity, swirl angle, and pitch angle. Kiock (6), Evans (12), and Hirsch and Kool (20) presented limited data showing the variation of rotor wake characteristics with changes in flow coefficient.

While much has already been accomplished in the past, more remains to be done. For example, data related to the variation of periodic-average rotor wake shape with frozen rotor section circumferential position when the rotor flow is unsteady in all frames of reference do not appear to be available in the open literature. Detailed slow- and fast-response instrument data related to multistage turbomachine blade wake production, transport, and interaction as well as data showing the results of particular blade row placement schedules are scarce. As noted recently by Mikolajczak (8),

The state of the art in turbomachinery technology has advanced to the point where further significant improvements will come from the understanding and control of the unsteady flows which exist in turbomachines.

The present work is intended as a modest contribution to the growing body of literature in this area.

B. Experimental Procedures and Instrumentation

Because modern turbomachine flow measurement techniques can involve complicated procedures and instruments, a brief review of related research on this topic area follows. A good overview of state-of-the-art

turbomachine flow measurement techniques including the use of slow- and fast response probes and transducers, flow visualization, and laser based optical methods is available in Ref. 23. As pointed out by Whitfield et al. (18), most of the measurements made prior to 1971 were obtained upstream and downstream of blade rows using stationary slow-response instrumentation. These tests provided much information on the time-average flow field and the overall performance characteristics of the blade rows. In the case of rotor row exit flow, however, very little if any, circumferential survey information was available until recently. Detailed unsteady flow data were scarce. Rotating instrumentation and fast-response stationary instrumentation were developed by a few early investigators (24,25), but none of these methods were used to measure the complete three-dimensional, time-dependent flow field involved behind a rotating blade row.

Of particular relevance to the present research are the hot-wire anemometer measurement techniques developed by Whitfield et al. (18), Lakshminarayana and Poncet (26), Lockhart and Walker (7), Evans (12), Raj and Lakshminarayana (13), and Hirsch and Kool (20). In all instances cited above, a means of phase locking the measurement with the rotor motion was used and some form of ensemble averaging was accomplished. Lockhart and Walker (7) used a single-wire probe aligned radially while Evans (12) used a single wire probe aligned perpendicular to the radius as well as an X-type probe. In both cases, radial velocities were ignored. A technique involving a single-wire sensor inclined 54.7 degrees with respect to the probe axis was used by Whitfield et al. (18) for measurement of the three-dimensional, periodic-average flow field behind an isolated rotor. The

slant wire was rotated about the probe axis at increments of 120 degrees and data were obtained for each of three mutually orthogonal orientations of the sensor. A relatively simple set of equations (simple because of the geometry of the probe and the measurement positions selected) were used to relate the readings at the three wire orientations to the axial, tangential, and radial velocity components. Hirsch and Kool (20) further developed this general single-wire technique, and through a more complex set of reduction equations extended the method so that probes of any inclined wire angle could be used with any three wire measurement orientations. To demonstrate this technique, they presented (20) periodicaverage velocity measurements of the flow field behind a rotor with an upstream IGV row in a low-speed, axial-flow turbomachine. Lakshminarayana and his students (13,26,27) have developed some three-dimensional, hot-wire anemometry procedures which utilize stationary and rotating probes with three orthogonally directed sensors. Raj (13) obtained three-dimensional, periodic-sample, circumferential blade-to-blade profiles of velocity, turbulence intensity, and Reynolds stress behind an isolated axial-flow fan rotor while Gorton (27) made measurements within a pump inducer rotor and Poncet (26) obtained data downstream of a pump inducer rotor. Although experimental data are not yet available, Hardin (see Ref. 28) developed a triaxial hot-wire technique which has been used to make on-rotor measurements of a compressor rotor wake.

In comparing the single-wire and three-wire systems, the three-wire system seems especially advantageous for measuring the three-dimensional components of turbulence intensity (random unsteadiness) since the three sensor readings can be obtained simultaneously. However, as pointed out

by Hirsch and Kool (20), the three-wire system can have several disadvantages including: (1) poor spatial resolution, (2) increased possibility of encountering probe prong interference effects, (3) difficulty of securing optimum wire positions for all flow situations, (4) increased work in obtaining a complete and accurate calibration, and (5) increased cost of initial system and repairs. The three-wire systems developed to date could be improved further by optimizing the relative positions of the three wires and deriving a more general set of reduction equations which would apply for any wire configuration. Hirsch and Kool (20) note that the advantages of a single-wire system include: (1) better spatial resolution since the sensor is rotated about the probe centerline, (2) less calibration effort required, (3) greater possibility for optimization of wire measurement positions, and (4) smaller cost of initial system and repairs. On the other hand, the time required to obtain a set of measurements is much greater, and it is more difficult to acquire the threedimensional flow quantities of turbulence intensity with the single-wire system.

The distinction between measurements made with a stationary hot-wire probe and those made with a circumferentially traversing probe moved ahead of or behind a periodically frozen rotor blade row has not yet been seriously considered in the open literature. For a rotor operating under unsteady relative flow conditions, the difference can be significant as will be shown in the present report.

III. RESEARCH COMPRESSOR FACILITY

The research compressor facility of the Iowa State University

Engineering Research Institute/Mechanical Engineering Department Turbomachinery Components Research Laboratory was used in this research program. A description of the compressor and related equipment and instrumentation is presented in this section.

A. Multistage Axial-Flow Research Compressor

The low Mach number, three-stage, axial-flow research compressor, shown schematically in Figure 3.1, was used in the experimental investigation. Photographs of the compressor rig are shown in Figure 3.2. A smooth gradually contracting inlet to the compressor guided the flow entering the inlet guide vanes and three subsequent sets of rotor-stator stages. The compressor flow path involved constant hub and tip diameters of .285 m (11.2 in.) and .406 m (16.0 in.), respectively, resulting in a hub/tip radius ratio of 0.7. The blades were made up of British C4 sections reflecting a free vortex design and were constructed of a plastic (Monsanto ABS) material. Overall blade characteristics are as follows:

Number of blades per row	IGV and stator rows - 37
	rotor rows - 38
Blade span (constant)	6.10 cm (2.4 in.)
Blade chord (constant), c	3.05 cm (1.2 in.)
Blade section maximum thickness/ chord ratio, t	10%

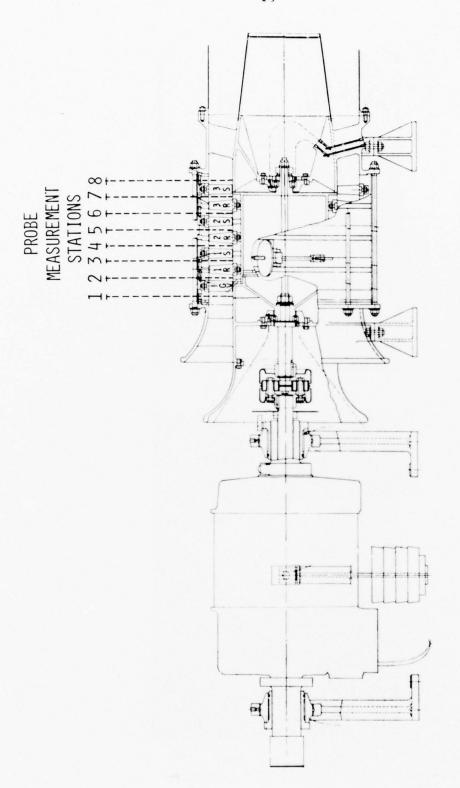
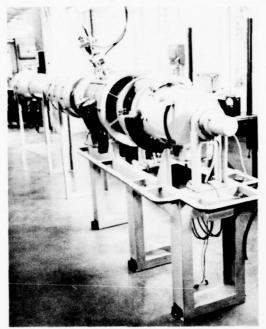
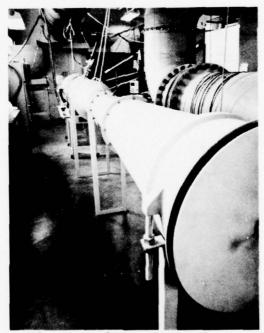


Figure 3.1, Driving motor and research compressor.



(a) View of the rig in the downstream direction.



(b) View of the rig in the upstream direction.
Figure 3.2. The axial-flow compressor rig.

The three rotor-stator stages were identical repeating stages, and the number of IGV blades and stator blades per row were the same. Further geometric blade details are tabulated in Table 3.1, and associated nomenclature is described in Figure 3.3. Figure 3.4 shows the arrangement of the stationary and rotor blade rows. Each blade row was in the form of an independent ring assembly which permitted rapid disassembly and reassembly of the compressor flow path and adjustment of the blade setting angles as well as the axial spacing between rows which was set for approximately 0.7 chord length (see Figure 3.5). The four stationary blade-row supporting rings were mounted in circular tracks in the outer-annulus casing to permit independent rotation of each stationary blade row about the machine axis. The stationary blade rows could be rotated during tests by means of a circumferential motion actuator which was mechanically linked to each stationary blade-row mounting ring as described in more detail later in the probe and stationary blade-row actuators section. For the present study, the three rotor-blade-row rings were positioned during assembly so that corresponding blade stacking axes for each rotor row were in line when viewed along the compressor axis. Probe-traversing measurement stations were aligned axially upstream and downstream approximately midway between each blade row, the exact axial location of each probe measurement station is shown in Figure 3.5. The compressor discharged into a downstream duct, as shown in Figure 3.6, which included an air straightening section, a venturi flow rate meter, a diffuser section, and a variable outlet-throttle plate. The compressor was driven by an 11 kW thyristor controlled variable speed (300-3000 rpm) motor mounted on air bearings to facilitate shaft torque measurement with a lever arm and weights

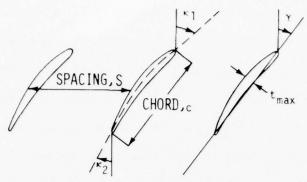
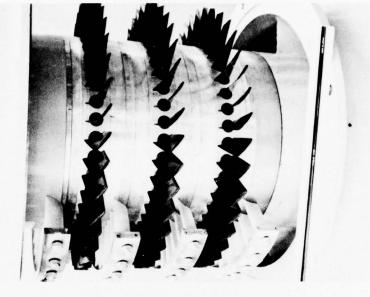


Figure 3.3. Blade nomenclature.

Table 3.1. Geometric blade details for IGV, rotors and stators at several radial locations.

		Blade Angles				
lade	Percent Passage Ht. From Hub	Solidity	Stagger	Inlet K1	Outlet	Camber
Row	PHH	c/S	Υ	1	2	κ ₁ - κ ₂
			degrees	degrees	degrees	degrees
	0	1.263	20.35	0.00	42.10	-42.10
	10	1.211	20.05	0.00	40.77	-40.77
	20	1.164	19.69	0.00	39.47	-39.47
	30	1.121	19.25	0.00	38.23	-38.23
IGV	40	1.080	18.65	0.00	37.08	-37.08
71	50	1.041	18.15	0.00	36.05	-36.05
	60	1.004	17.63	0.00	35.02	-35.02
	70	0.971	17.05	0.00	33.93	-33.93
	80	0.940	16.45	0.00	32.92	-32.92
	90	0.913	15.65	0.00	32.10	-32.10
	100	0.887	14.15	0.00	31.40	-31.40
	0	1.299	-20.54	-42.40	3.90	-46.30
	10	1.250	-24.39	-44.76	- 2.84	-41.92
	20	1.205	-28.11	-46.85	- 9.51	-37.34
	30	1.164	-31.70	-48.53	-15.96	-32.57
H	40	1.123	-3 5.15	-49.82	-21.88	-27.94
Rotor	50	1.078	-38.47	-50.81	-27.06	-23.75
æ	60	1.035	-41.66	-51.77	-31.64	-20.13
	70	0.999	-44.71	-52.90	-35.78	-17.12
	80	0.968	-47.63	-53.98	-39.26	-14.72
	90	0.939	-50.41	-54.82	-41.91	-12.91
	100	0.909	-53.07	-55.50	-44.10	-11.40
	0	1.263	40.24	54.80	26.70	28.10
	10	1.211	39.32	53.48	25.67	27.81
	20	1.164	38.39	52.36	24.68	27.68
	30	1.121	37.46	51.43	23.74	27.69
r	40	1.080	36.54	50.25	22.77	27.48
ţ	50	1.041	35.61	48.56	21.72	27.84
Stator	60	1.004	34.68	47.13	20.76	26.37
01	70	0.971	33.75	46.65	20.01	26.64
	80	0.940	32.83	46.36	19.34	27.02
	90	0.913	31.90	45.59	18.62	26.97
	100	0.887	30.97	44.50	17.85	26.65



(a) First stator blade-row assembly.

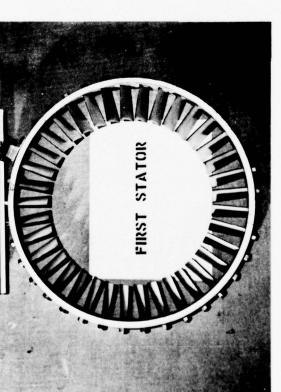


Figure 3.4. Compressor blading.

(b) Stationary and rotor blade-row arrangement.

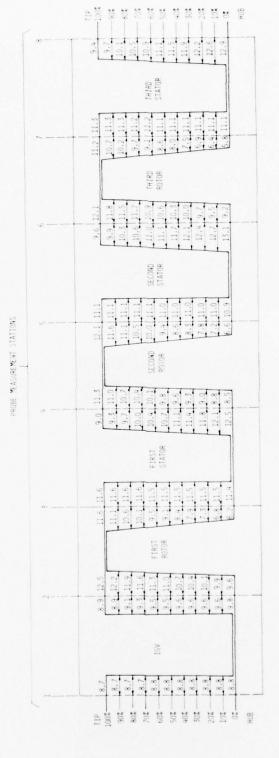


Figure 3.5. Schematic diagram showing axial location of probe measurement stations (dimensions in mm).

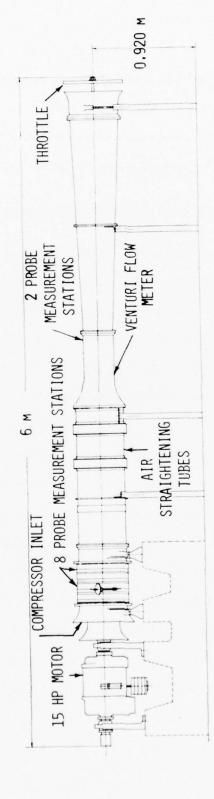
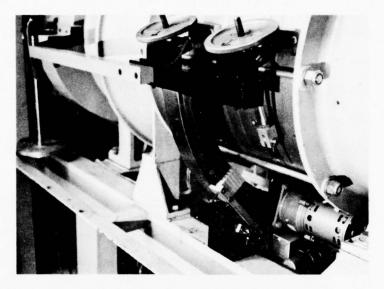


Figure 3.6. Research compressor apparatus side view.

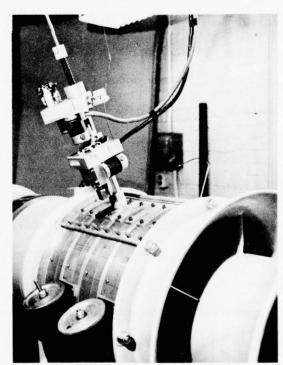
arrangement. Shaft rpm measurement was made with a frequency counter and a magnetic pickup off a 60-toothed gear on the shaft. The motor speed was controlled by a multiturn helical potentiometer balanced against a feedback voltage from a dc tachogenerator which rotated with the motor shaft. It was possible to maintain a constant rotor speed to within ± 1 rpm. More details about the research compressor may be found in Ref. 29.

B. Probe and Stationary Blade-Row Actuators

The circumferential motion actuator system, shown in Figure 3.7a, was used to set the circumferential position of the stationary blade rows. The actuator was basically composed of a semicircular dovetail slide driven by a gearmotor through a rack and pinion gear arrangement. The actuator was connected to each stationary blade-row mounting ring through an adjustable hand-screw link, making possible the simultaneous or individual circumferential movement of all the stationary blade rows. The circumferential positions of the individual stationary blade rows were determined with four circumferential blade-row scales (one for each blade row) marked in degrees and mounted on the compressor outer casing. The scales were designed so that angle readings were positive in the direction of rotor rotation, and a reading of 0.0 degrees corresponded to a position where the blade stacking axis was in axial alignment with the probetraversing stations. The circumferential position of the actuator slide could be recorded by monitoring the voltage of a linear potentiometer geared to the slide. The potentiometer output voltage was correlated to the incremental motion of the actuator by a linear least squares fit. When the stationary blade rows were moved jointly with the actuator, the



(a) Circumferential motion actuator connected to the stationary blade rows.



(b) Probe immersion and angle actuator mounted at a probe-traversing measurement station.

Figure 3.7. Probe and stationary blade-row actuators.

positions of the blade rows were specified by recording Y, the circumferential position of the actuator in degrees as determined from the potentiometer voltage, and by knowing the circumferential position of each blade row when Y was equal to zero (Y0). The values of Y0 for the stationary blade rows (Y0 $_{\rm IGV}$, Y0 $_{\rm 1S}$, Y0 $_{\rm 2S}$ and Y0 $_{\rm 3S}$) were determined from the circumferential blade row scales. The actuator system could be used to position the stationary blades to within 0.05 degrees.

Figure 3.7b shows the probe actuator (L. C. Smith Company model 6180) which was used for probe angle and immersion positioning. The probe angle and radial positions were each monitored by both mechanical digital counters and by linear potentiometers. The potentiometer voltages were correlated to their respective movements by a linear least squares fit and were used to record the probe angle and immersion positions with an accuracy of 0.05 degrees and 0.15 mm, respectively. A probe actuator control indicator (L. C. Smith Company model DI-3R) and probe actuator switchbox (L. C. Smith Company model DI-4R-SB) were used to control the probe actuator.

C. Pressure and Temperature Sensing Instrumentation

A scanning valve system (Scanivalve Company model 48D3-1) including a strain-gage pressure transducer (Scanivalve Company model PDCR22) and a bridge circuit (Endevco model 4470) were used for qualitative pressure measurements. All quantitative pressure measurements were made using various precision water in glass manometers (Meriam type Incl.) which were calibrated with a micromanometer (Meriam type Micro.). A conventional pitot tube (United Sensor type PC) was used as a calibration standard for

fluid velocity measurement. Several types of pressure probes, including Kiel, cobra, wedge, and sphere, were tested for suitability in the compressor. A cobra probe (United Sensor type CA), capable of measuring total pressure and flow yaw angle, proved most appropriate for use in the compressor and was used for almost all slow-response measurement tests.

An outer-annulus wall static pressure tap was provided at each axial location corresponding to a probe-traversing station. In addition, a hub static pressure tap was installed behind the third stator row where the hub was stationary. Several wall pressure static taps were also located at the inlet and throat of the flow rate venturi meter. Mercury in glass thermometers were used to measure room air temperature while copperconstantan thermocouples and a precision millivolt potentiometer (Leeds and Northrup Company model 8686) were used to measure flowing fluid temperatures. A mercury in glass barometer (Princo Instruments, Inc. Model B-222) was used to measure atmospheric pressure.

D. Fast-Response Measurement System

A setup diagram of the fast-response measurement system used to make periodic-average, three-dimensional velocity measurements is shown in Figure 3.8. The system consisted of the following components:

- (1) Single slant hot-wire probe (Disa model 55P02 Modified)
- (2) Constant temperature anemometer (Thermo-Systems, Inc. (TSI) model 1010A)
- (3) Linearizer (TSI model 1072)
- (4) Periodic sample-and-hold circuit
- (5) Photoelectric triggering circuit

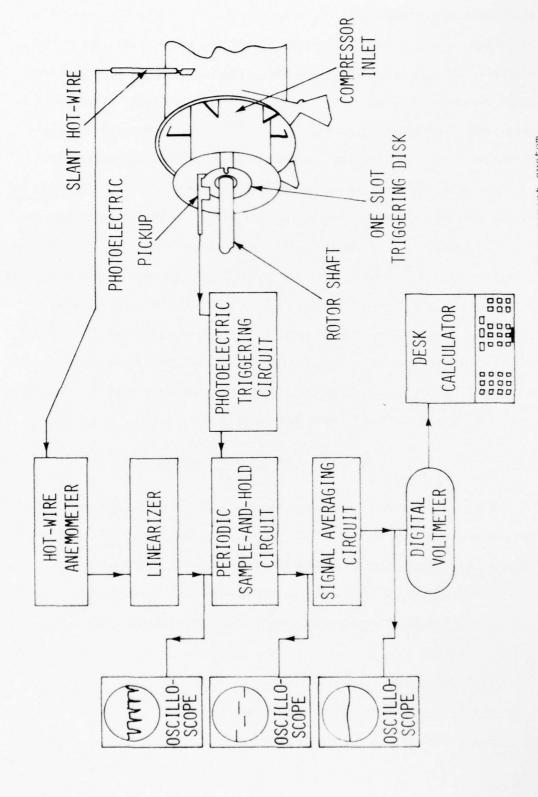


Figure 3.8. Schematic setup diagram of fast-response measurement system.

- (6) Signal averaging circuit (TSI model 1047)
- (7) Digital scanning voltmeter (Hewlett-Packard model 3480D)
- (8) Desk-top calculator (Hewlett-Packard model 9821A)
- (9) Oscilloscopes (Tektronix Inc.)

The hot-wire probe involved a 5 µm diameter platinum-plated tungsten wire with a 1.25 mm sensitive wire length and copper and gold plating at the ends. One wire was slanted with respect to a plane normal to the probe axis at an angle of 35 degrees while the other was at 45 degrees. The constant temperature anemometer was used in conjunction with a polynomial analog-signal linearizer. The periodic sample-and-hold circuit was designed and built on campus in cooperation with the Iowa State University Engineering Research Electronic Shop staff. Details on the circuit design appear in Appendix A. The circuit was used to obtain periodic-average flow field data. A photoelectric pickup triggered by a one slot per revolution disk rotating with the compressor shaft was used to synchronize the periodic sample-and-hold circuit activity and rotor motion. The sampling circuit was designed to obtain a 5 usec sample of the linearized hot-wire anemometer output-voltage signal during each revolution of the rotor shaft. Each time the 5 usec sample was taken, a stroboscope was also triggered and the periodic-sampling position of the rotor blades and shaft could be visually observed. The time delay between the triggering of the photoelectric pickup and sample-and-hold circuit could be varied to permit control of the periodic-sampling position of the rotor blades relative to the hot-wire probe and stationary blades. The photoelectric

¹The typical period of the rotor wake was 1.1 msec.

pickup could be moved circumferentially to also vary the rotor periodicsampling position, and the movement could be recorded from a circumferential degree scale attached to the photoelectric pickup. Two scribe marks, one on the rotor shaft surface locating the stacking axis position of a rotor blade and the other on the stationary hub surface corresponding to the position of the probe measurement stations, were used in conjunction with the photoelectric pickup circumterential scale to ascertain the circumferential location of the rotor blade periodic-sampling position. The photoelectric pickup motion could be mechanically linked to the stationary blade-row circumferential actuator in order to provide effective circumferential traversing of the hot-wire probe past the stationary blade rows and periodically frozen rotor blade rows. The periodic-sampling signal from the sample-and-hold circuit was electronically smoothed using a signal averaging circuit which acted like a simple low-pass filter with time constant adjustment from 1 to 100 sec. Finally, the signal from the averaging circuit was digitized by the voltmeter and recorded by the calculator.

E. Calibration Nozzle

An air nozzle was used for the calibration of slow-response pressure probes and hot-wire sensors. The nozzle had a throat diameter of 25.4 mm (1.0 in.) and a contraction ratio of 144 to 1. No measurable difference between the plenum pressure and total pressure measured with a pitot-static probe positioned 0.25 throat diameters from the exit of the nozzle was detected over a velocity range from 0.0 to 50.0 m/s. The flow at the nozzle exit involved a uniform velocity profile. Regulated compressed air

provided the air supply, and the air temperature was controlled by a variable-current heater, blower, and heat exchanger arrangement. Figure 3.9 shows the probe holder which allowed probe stream immersion and yaw and pitch angle positioning. The probe holder was designed to permit the sensing portion of the probe to remain in the same position in the flow while the probe yaw and pitch angles were varied. The telescope, shown in Figure 3.9, was used to initially align hot-wire probes in the flow.

F. Sound Pressure Level Measurement Instrumentation

A precision sound-level meter and analyzer (General Radio type 1933) was used to make overall sound-pressure level measurements and octave band analyses of the compressor inlet noise. The instrument included a 1 in. electret condenser microphone, A, B, C, and flat weighting characteristics and ten octave band filters with band center frequencies from 31.5 Hz to 16 kHz. The sound-level meter was also used as a preamplifier for a narrow band pass (down to 1%) frequency analyzer (Brüel and Kjaer model 2121) for obtaining spectrum analyses of the compressor noise. The frequency analyzer was combined with a related level recorder (Brüel and Kjaer model 2305) for automatic recording of the noise spectrum.

G. Data Acquisition and Reduction System

A desk-top calculator (Hewlett-Packard model 9821A) and related multiple channel scanning digital voltmeter (Hewlett-Packard 3480D, 3458D) were used for data collection and reduction. An interface between the calculator and voltmeter allowed the calculator to read any one of ten voltmeter channels and store the reading in memory. The calculator had

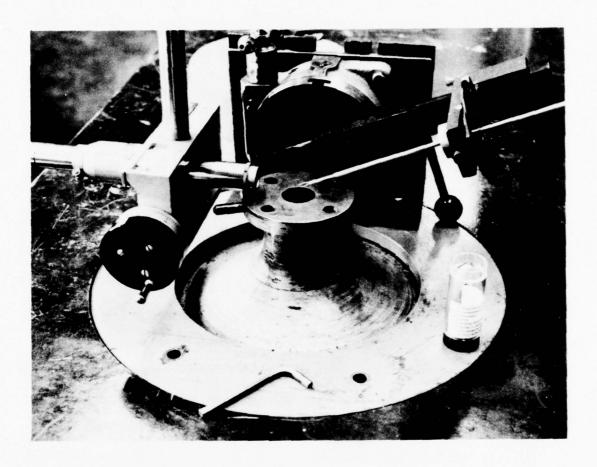


Figure 3.9. Calibration nozzle, probe positioner, and optical alignment telescope used for probe calibration.

423 available memory registers for program and data storage. The data storage and programming capabilities of the calculator were expanded by a tape cassette built into the calculator which could be used to load and record data and programs from memory. Since the calculator had limited printing and no plotting capabilities, the Iowa State University Computation Center computing system (IBM 360/65, 370/158) was utilized for data tabulation and plotting.

IV. EXPERIMENTAL PROCEDURES AND DATA REDUCTION

Basically, three types of measurements were involved during the experimental investigation. Included were sound-pressure level measurements, slow-response pressure measurements, and fast-response hot-wire anemometer measurements. One set of sound-level measurements was obtained over the entire rpm range of the compressor at constant flow coefficient. All other data were taken with the compressor speed and flow rate set at 1400 rpm and 0.94 kg/s (0.42 flow coefficient), respectively. This operating condition was near maximum efficiency for 1400 rpm.

The pitot tube, micromanometer, and mercury in-glass thermometer were respectively used as standards for velocity, pressure, and temperature calibration and measurement. Calibration of all electronic components used in this experimental investigation were performed in the Iowa State University Engineering Research Institute Electronic Shop. Before each test, sufficient time was allowed for the electronic instrumentation to warm up and for the laboratory and compressor fluid temperatures to reach equilibrium values.

Data acquisition programs were written for the desk-top programable calculator (Hewlett-Packard) to control the step-by-step procedures of the experimental tests. Data were either typed into the calculator or read by the calculator through the interface from the digital voltmeter as specified by the program. The data acquisition programs were used to (1) store data in memory, (2) make preliminary calculations, (3) print out data and preliminary results on magnetic cassette tape. In addition, data reduction programs for the

calculator were written to accept the data and preliminary results recorded on magnetic tape and to perform the required manipulations to obtain the final results. A list and brief description of the data acquisition and reduction programs are presented in Appendix B.

A. Sound-Pressure Level Measurements

During early stages of the research project, it was noticed that the inlet noise produced by the compressor could be varied significantly by changing the circumferential positions of the inlet guide vane and stator blade rows relative to each other. As a result, sound-pressure level (SPL) measurements of the compressor inlet noise were made with the stationary blade rows set at different circumferential position schedules. The microphone of the sound-level meter was positioned at the compressor inlet as shown in Figure 4.1. Three categories of sound-level tests were made: (1) testing for compressor inlet noise variation by changing the IGV row circumferential position at several points over the compressor rpm range for a fixed flow coefficient of 0.42, (2) determining the stationary blade-row circumferential settings for minimum and maximum sound at a speed of 1400 rpm and a flow coefficient of 0.42, and (3) obtaining detailed SPL measurements at the minimum and maximum noise blade-row settings found from test (2) above.

1. Testing for noise variation over compressor rpm range

In order to determine the influence of stationary blade row circumferential placement on compressor inlet noise at various compressor speeds, overall SPL measurements were obtained over the rpm range of the compressor at a constant flow coefficient of 0.42. Only the circumferen-



Figure 4.1. Sound-level meter and position of microphone for compressor inlet noise measurement.

tial position of the IGV row was varied; the positions of the three stator rows were set so that the stacking axis of one stator blade in each row was in line with the probe traversing stations. Overall SPL readings were taken at minimum and maximum noise circumferential positions of the IGV row at fifteen rpm settings over the rpm range from 200 to 2700. The flow coefficient, determined from the venturi mass flow rate indication, was maintained constant at 0.42 by adjusting the outlet throttle plate.

2. Determining the minimum and maximum sound settings

For this test and all remaining tests, the compressor operating conditions were set for a rotor speed of 1400 rpm and a flow coefficient of 0.42. The stationary blade-row circumferential settings for minimum and maximum noise at the above compressor operating conditions were uniquely obtained by monitoring the overall SPL while adjusting the circumferential positions of the four stationary blade rows relative to each other by using the iterative procedure outlined below:

- (1) Holding the IGV row stationary, the three stator rows were moved circumferentially together until minimum (maximum) inlet noise was observed.
- (2) Holding the IGV and first stator (first stator position determined in step 1) rows stationary, the remaining two stator rows were moved circumferentially together until minimum (maximum) inlet noise was observed.
- (3) Holding the IGV, first stator (first stator position determined in step 1), and second stator (second stator position determined in step 2) rows stationary, the remaining third stator row was

moved circumferentially until minimum (maximum) inlet noise was observed.

- (4) Steps 1, 2, and 3 were repeated until the relative circumferential positions of the stationary blade rows were identical for two consecutive repetitions.
- 3. <u>Obtaining detailed SPL measurements at minimum and maximum sound-level</u> blade-row settings

Once the blade-row circumferential placement schedules for minimum and maximum noise were determined, overall, octave band, and spectrum analyses SPL measurements were made at the two circumferential blade-row settings. Ten octave band measurements with center frequencies from 31.5 Hz to 16 kHz were taken with the sound-level meter, and a 1% band-pass spectrum analysis was obtained over the frequency range from 200 Hz to 2000 Hz with the sound-level meter used as a preamplifier connected to the narrow band-pass frequency analyzer and level recorder.

B. Slow-Response Measurements

Slow-response pressure measurements were taken to obtain detailed and overall time-average information of the flow field between the blade rows of the compressor. The details involved in obtaining and reducing these measurements are described in this section.

1. Probe calibration

The cobra probe sketched in Figure 4.2 was used to obtain nearly all total-pressure and flow-angle slow-response data in the compressor. In order to better understand the measurement capabilities of the cobra probe, an extensive total-pressure and flow-angle calibration of the

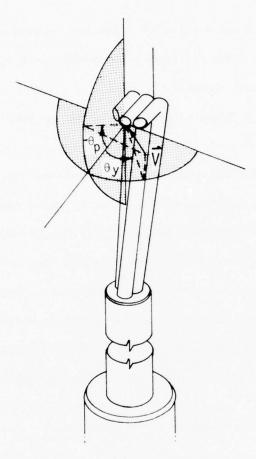


Figure 4.2. Total-pressure and flow-yaw-angle cobra probe and probe angle nomenclature.

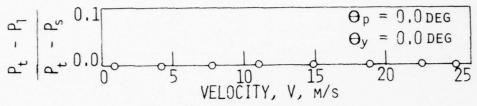
probe was made utilizing the calibration nozzle. For all calibrations, the probe was positioned 0.25 nozzle orifice diameters from the nozzle exit. The total pressure at this point was determined by measurement of the plenum wall pressure. The micromanometer was used to measure all differential pressures. The probe pitch angle, θ_p , and probe yaw angle, θ_v , were defined as indicated in Figure 4.2.

a. Total pressure calibration A total pressure calibration of the cobra probe with respect to velocity, probe pitch angle, probe yaw angle, and probe time-response was made. In order to calibrate for totalpressure velocity effect, the probe was aligned in the flow with zero pitch angle and rotated about the probe axis until the two probe side-tube pressures, P_2 and P_3 , were equal (U-tube manometer balance). The pressure difference between the plenum pressure, P_{t} , and the probe indicated total pressure, P1, was observed over the velocity range anticipated in the compressor (0.0 to 25.0 m/s). Next, the flow-angle and time-response total pressure calibrations were conducted at a constant velocity of 18.7 m/s (typical average velocity in the compressor). The effect of pitch angle on probe indicated total pressure was determined by measuring the difference between P_{t} and P_{l} at different pitch angles over the range from -4.0 to 5.5 degrees with the probe yaw angle set at zero. The total pressure calibration of yaw angle effect was made by obtaining the difference between P_{t} and P_{l} at 18 yaw angle positions from -24 to 24 degrees at a pitch angle of zero. The probe total-pressure time-response characteristics were determined with the total-pressure probe tap connected to the inclined manometer actually used for compressor flow field total pressure measurement. To suddenly change the pressure at the probe total-pressure sensing tube, a plate was temporarily placed ahead of the probe. The indicated total pressure, P_1 , was read from the manometer every 5 sec.

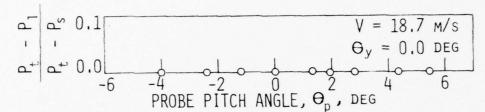
The results for the velocity, pitch angle, yaw angle, and time-response portions of the total pressure calibration are shown in Figure 4.3. No measurable difference between the nozzle plenum total pressure and the probe indicated total pressure was detected over the velocity and pitch angle measurement ranges. Also, the probe indicated total pressure was insensitive to yaw angle over the range from -5.0 to 5.0 degrees. The total-pressure time-response curves were used as guidelines for the time span needed between total-pressure readings.

b. Probe yaw-angle calibration A probe yaw-angle calibration was made to determine the yaw-angle sensitivity of the cobra probe. The pressure difference between the probe side-tube pressures, P_2 and P_3 , was measured at 19 yaw-angle settings over a range from -5.0 to 5.0 degrees at a constant velocity of 18.7 m/s. The results of this test, shown in Figure 4.4, indicate that under the steady uniform flow conditions of the calibration nozzle, the cobra probe yaw-angle measurement uncertainty was approximately 0.1 degrees (20 to 1 odds).

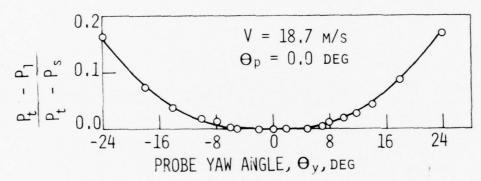
The flow angle indicated by the cobra probe when the side-tube pressures are balanced in the flow, is largely affected by hole-to-hole velocity gradients. In regions of high velocity gradients, large flow-angle errors result due to the physical distance between the side-tube pressure holes. Since there was no calibration method available to account for this effect, precautions were taken when making flow-angle measurements in the compressor. Flow-angle measurements behind stationary blade rows were made only in the freestream where the velocity gradients



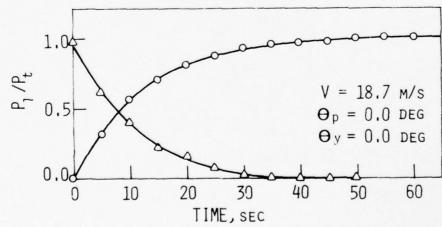
(a) Velocity total-pressure calibration curve.



(b) Probe pitch-angle total-pressure calibration curve.



(c) Probe yaw-angle total-pressure calibration curve.



(d) Time-response total-pressure calibration curve. Figure 4.3. Cobra probe total-pressure calibration curves.

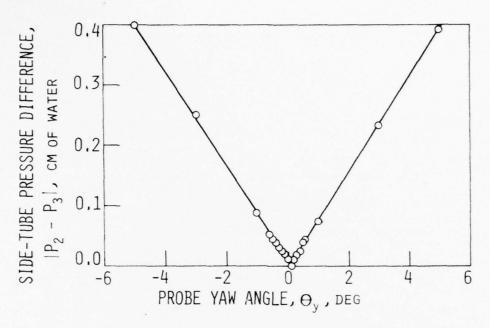


Figure 4.4. Cobra probe yaw-angle sensitivity calibration curve.

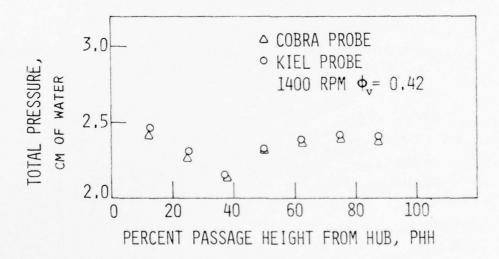


Figure 4.5. Cobra and Kiel probe comparison.

were small. The probe angle was set approximately at the average freestream value for total-pressure measurements in and near the blade wake where the velocity gradients were high.

c. Kiel probe comparison — A radial direction survey of totalpressure variation behind the first rotor at a speed of 1400 rpm and a
flow coefficient of 0.42 was made with the cobra and Kiel probes. Totalpressure measurements were made by both probes at the same eight radial
locations from 12.5 to 87.5% passage height from the hub. The cobra
probe was aligned in the flow by balancing the side-tube pressures, and
the indicated flow angle was used to set the angular position of the Kiel
probe. The results (see Figure 4.5) show that the total pressures indicated by the two probes were equal at mid-span height and deviated only
slightly (0.6 mm of water maximum) toward the hub and tip.

2. Data acquisition

Slow-response total-pressure and flow-angle circumferential direction surveys of the compressor flow field were obtained with the cobra probe at nine passage height locations of 10, 20, 30, 40, 50, 60, 70, 80, and 90% from the hub ahead and behind each of the rotating and stationary blade rows for both minimum and maximum noise conditions. In addition, outer-annulus wall static-pressure circumferential surveys were made at each probe traversing axial location for minimum and maximum noise. The steps followed to obtain this data are described below.

Prior to testing, several preliminary setups were required. The cobra probe was mounted in the probe actuator at the calibration nozzle. The probe angle zero was ascertained by balancing the probe side-tube pressures, and the probe immersion was zeroed by using a depth micrometer.

The voltages from the stationary blade-row circumferential motion, probe immersion, and probe flow-yaw-angle potentiometers were correlated with their respective motions with a linear least squares correlation. The circumferential positions of the stationary blade rows were set to either the minimum or maximum sound schedules (refer to Table 5.1). Before each test, the scales on the inclined and U-tube manometers were zeroed, and the bridge balance and gain adjustments on the Endevco pressure-transducer bridge circuit were set.

Once the preliminary setup procedures were completed, the following miscellaneous data were recorded so that the measurement conditions were always completely specified:

- (1) Probe traversing station number, see Figure 3.1
- (2) Stationary blade position settings, ${\rm Y0}_{\rm IGV}$, ${\rm Y0}_{\rm 1S}$, ${\rm Y0}_{\rm 2S}$ and ${\rm Y0}_{\rm 3S}$, degrees
- (3) Barometric pressure, 1 inches of Hg
- (4) Barometer ambient temperature, 1 °F
- (5) Room temperature, 1 °F
- (6) Compressor rpm
- (7) Compressor rpm variation
- (8) Differential pressure across venturi, inches of water
- (9) Station pressure at venturi throat, inches of water
- (10) Temperature at venturi throat, millivolts
- (11) Date
- (12) Time¹

¹Taken at beginning and end of each circumferential survey.

The circumferential direction surveys were made with the probe actuator mounted at one of the probe-traversing stations with the probe immersed to the specified radial position. A qualitative trace of the circumferential variation of total pressure with the probe set at the approximate average flow yaw angle was made on an X-Y storage oscilloscope from the electrical signals of the strain-gage pressure transducer and the circumferential motion potentiometer. The trace was used to select the positions of the flow-field measurement points. For each circumferential direction survey, measurements were obtained over one circumferential stationary blade pitch, eleven measurement points behind each rotor blade row and between fourteen and seventeen points behind each stationary blade row. The cobra probe side-tube pressures were balanced with the aid of a U-tube manometer at every flow-field measurement point behind a rotor blade row and at measurement points in the freestream behind a stationary blade row. The probe angle and the circumferential position Y were recorded at each point along with the total pressure measured with the inclined water manometer. After the last measurement point of each circumferential survey was taken, the miscellaneous and flow-field data were printed out and recorded on magnetic tape for reduction at a later time.

Once the total-pressure and flow-angle circumferential surveys were completed for all radial positions at one axial probe station, a circumferential survey over one blade pitch was made of the outer-annulus wall static pressure with the wall tap at the axial location of the probe station.

3. Data reduction

The first step in the reduction of the slow-response data was to determine the primary flow-field quantities of total head, static head, and tangential flow angle. Once these primary values were obtained, other flow-field parameters such as absolute velocity, relative velocity, incidence angle, deviation angle, etc. were calculated along with their circumferential average values. Finally, overall rotor, stator, and stage parameters were determined. Since the velocities in the compressor were all less than that corresponding to a Mach number of 0.2, the flow was assumed to be incompressible for all calculations. Integrated averages were computed using a spline-fit integration (see Ref. 30). A complete list of all equations used in reducing the data is presented in Appendix C.

a. Flow-field parameters — The total head 1 , H, was determined for each flow-field measurement point from the measured total pressure, and a circumferential integrated average was calculated for each radial position at every probe-traversing measurement station. The tangential flow angle, β_y , was assumed to be circumferentially constant and a circumferentially integrated average value was determined for each radial position at every measurement station. All circumferential averages except for flow angle averages behind stationary blade rows were determined by integrating over one stator blade pitch. The average flow angle behind a stationary blade row at each radial position was obtained by integrating only over the freestream portion. The static head 1 , h, was also assumed to be circum-

¹With respect to atmospheric pressure.

ferentially constant, and the radial distribution of h was determined at each measurement station by solving the radial equilibrium equation. Since the compressor involved cylindrical annulus walls, the radial velocities between the blade rows at the probe traversing stations were assumed to be zero. By making this assumption and by neglecting viscous effects locally, the equation of motion in the radial direction reduces to

$$g_{c} \frac{dh}{dr} = \frac{V^{2}}{r}$$
 (4.1)

where h = static head, Nm/kg

r = radius, m

 V_{v} = tangential velocity, m/s

 $g_c = gravitational constant, kgm/Ns^2$

The tangential velocity is equal to

$$V_{y} = \sqrt{2g_{c}(H-h)\sin\beta_{y}}$$
 (4.2)

where β_v = tangential flow angle, degrees.

Substituting the expression for $\mathbf{V}_{\mathbf{y}}$ into Equation (4.1), the radial equilibrium equation becomes

$$\frac{dh}{dr} = \frac{2 \sin^2(\beta_y) (H-h)}{r} \tag{4.3}$$

Equation (4.3) is a first order ordinary differential equation and was solved by the Runge-Kutta numerical technique (see Ref. 31) for the radial distribution of static head. The solution was obtained by using the average outer-annulus static wall pressure as an initial value and by marching radially toward the hub at increments of 5% of passage height. The radial distributions of H and β_y required for the solution were obtained by a second order Lagrange interpolation of the known circumferen-

tial average values. A typical static-pressure radial equilibrium solution behind the third stator is shown in Figure 4.6. The radial distribution of static pressure from the solution is in good agreement with the measured static wall pressure at the hub.

With the circumferential distributions of H and the circumferential average values of β_y and h determined, the circumferential variation and integrated average of absolute velocity, V, were calculated for each radius at every probe measurement station. From the circumferential average velocity and tangential flow angle, the following circumferential average quantities were computed for all nine radial positions at each measurement station:

- (1) Axial velocity, m/s, Eq. 12.16
- (2) Tangential velocity, m/s, Eq. 12.18
- (3) Blade incidence angle, degrees, Eqs. 12.24, 12.26, and 12.28
- (4) Blade deviation angle, degrees, Eqs. 12.25, 12.27, and 12.29
- (5) Flow coefficient, Eq. 12.30
- (6) Relative velocity, m/s, Eq. 12.22
- (7) Relative tangential velocity, m/s, Eq. 12.20
- (8) Relative flow angle, degrees, Eqs. 12.23

In addition, an overall integrated flow rate and flow coefficient at each probe-traversing station was computed and compared with the flow rate and flow coefficient obtained from the flow rate venturi meter data. In order to determine the integrated flow rate at the probe stations, the flow near the hub and tip in the passage height regions beyond 10% and 90% was estimated by extrapolating the axial velocity variation with a straight line.

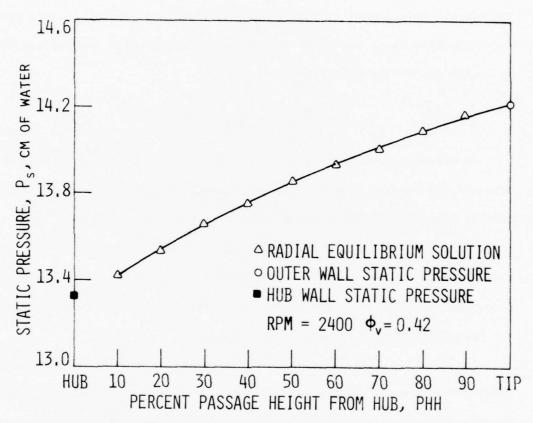


Figure 4.6. Static-pressure radial equilibrium solution for the compressor behind the third stator.

b. Rotor, stator, and stage performance parameters The actual and ideal head-rise coefficients and hydraulic efficiency were calculated at the nine radial positions for each of the three rotor rows, three rotor-stator stages, and the overall compressor. In addition, blade-section total-head-loss coefficients for each rotor and stator blade row were determined. Finally, the mechanical power and mechanical efficiency were calculated from the motor torque-meter measurements and the overall head rise across the compressor.

C. Fast-Response Measurements

Fast-response hot-wire anemometer measurements were taken to obtain a detailed description of the three-dimensional, periodic-average, instantaneous flow between the blade rows of the research compressor. The periodic-average hot-wire measurement technique is described in the first two sections, and the procedures involved in calibration, data acquisition, and data reduction are presented in the remaining sections.

1. Periodic sampling and averaging technique

The flow field in a turbomachine is generally made up of two types of fluctuating flows: a periodic component and a random (turbulent) component. When a stationary fast-response instrument such as a hot-wire probe is used to measure the flow, the hot-wire signal s(t) will be composed of a periodic signal p(t) with known period T in phase with the blade passing frequency of the moving blade row and a random signal n(t); hence

$$s(t) = p(t) + n(t)$$
 (4.4)

The periodic component p(t) can be obtained by periodically sampling s(t) with period T and averaging arithmetically. As shown by Hirsch and Kool (20), the periodic-average signal $\tilde{s}(t)$ can be expressed as follows:

$$\tilde{s}(t) = \frac{1}{N} \sum_{k=1}^{N} s(t + kT)$$
 (4.5)

or

$$\tilde{s}(t) = \frac{1}{N} \sum_{k=1}^{N} p(t + kT) + \frac{1}{N} \sum_{k=1}^{N} n(t + kT)$$
(4.6)

If N is made large enough, the last term of Equation 4.6 will be zero due to its random character. Thus,

$$\tilde{s}(t) = p(t) \tag{4.7}$$

and the periodic component p(t) can be obtained from s(t) by using a periodic-sampling and averaging technique.

The hot-wire anemometer system and periodic-sampling and averaging circuits described earlier (see Figure 3.8) were used to procure periodic-average velocity data of the flow between blade rows in the compressor. A periodic average of the linearized anemometer signal for each distinct position and orientation of the hot-wire probe was obtained by taking approximately 1200 periodic samples (one sample each revolution) and averaging both electronically and arithmetically. The electronic averaging was accomplished with the signal averaging circuit (low-pass filter) set for a time constant of 1.0 sec. The electronically averaged signal was subsequently sampled 180 times (equivalent to approximately 1200 hot-wire signal samples) once every 0.17 sec by the calculator through the digital voltmeter interface after which an arithmetic average was calculated. Two types of periodic-average circumferential surveys were made:

(1) frozen rotor-blade flow-field surveys made by effectively traversing the hot-wire probe circumferentially relative to stationary IGV, stator, and periodically frozen and sampled rotor blades and (2) passing rotor-blade flow-field surveys made with a stationary hot-wire probe sampling the passing rotor blade flow.

Measurements made by the first method yield the periodic component of the flow field at an instant in time with the rotor blades periodically frozen in one position with respect to the stationary blades. Results obtained with the frozen rotor-blade survey method include the stationary periodicity produced by the stationary blade rows. With this method it is possible to obtain both periodic-frozen rotor and stator blade wake profiles. Frozen rotor-blade surveys were obtained by mechanically locking the photoelectric pickup motion (periodic-frozen rotor blade circumferential motion) with the circumferential movement of the stationary blade rows. Jointly moving the periodic-frozen rotor and stationary blades past the stationary probe results in the effective circumferential traversing by the probe. Since a frozen rotor-blade flow-field probe survey is representative of the blade exit flow field at only one instant of time. information must be obtained for several instants of time as the rotor blade passes in stop action sequence by the stator blade in order to obtain a more complete picture of the blade exit flow field. This was done by making frozen rotor-blade flow-field surveys for several periodicfrozen rotor blade positions relative to the position of the stationary blades. These varying frozen rotor blade/stator blade relative position schedules were attained by simply shifting the photoelectric pickup with

respect to the stationary blades. Most of the hot-wire data were obtained using this method.

Periodic-average circumferential surveys made by the second method represent the flow field as seen by a stationary observer *(e.g., stator blade or stationary probe) as the rotor blade passes by during a finite length of time. The passing rotor-blade survey method disregards the stationary periodicity produced by the stationary blade rows. A passing rotor-blade survey behind a stationary blade row lends little information with regard to the overall wakes produced by the upstream stationary blade row. Passing rotor-blade flow-field surveys were obtained by moving only the photoelectric pickup, maintaining the stationary blade rows motion-less while hot-wire data were collected. This is similar to the methods used by Evans (12), Raj and Lakshminarayana (13), Whitfield et al. (18), and Hirsch and Kool (20). The frozen rotor-blade and passing rotor-blade measurement techniques should yield the same results when the rotor flow is steady in the relative (rotating) reference frame, for example, in the case of isolated rotor measurements.

The accuracy of the periodic-sampling and averaging technique is largely dependent on N, the number of samples. If N is small, the random component term in Equation 4.6 will be significant, and an accurate average of the periodic component will not be obtained. The accuracy is also dependent on the magnitude of the random fluctuations about the mean value. The accuracy decreases as the magnitude of the random fluctuations increase. Hirsch and Kool (20) present a relation between σ , the standard deviation of the periodic-sample average, and σ_n , the standard deviation

of the random fluctuations, which is dependent on N, the number of samples. This relationship

$$\sigma^2 = \frac{1}{N} \sigma_n^2 \tag{4.8}$$

shows that as N is increased, σ is reduced as the square root of N. This relation is valid when the periodic-sample averaging is done arithmetically.

In order to obtain a relationship between σ and N when the averaging of the periodic samples is performed using the electronic and arithmetic technique described previously, an experiment was conducted with a hot wire positioned in the axial direction behind the second rotor of the compressor at 50% passage height with the compressor at typical operating conditions of 1400 rpm and 0.42 flow coefficient. The linearized anemometer signal was sampled at periodic rotor positions corresponding to the hot-wire positioned in and out of the rotor wake. A set of ten periodic-average velocity values was obtained for several values of N over a range from 4 to 1556 samples at both periodic-sampling rotor-blade positions. The variation coefficient of the ten values within each set was then calculated and plotted against the corresponding value of N. The results in Figure 4.7 show that as N increases, σ decreases rapidly at first and then tapers off until increasing N has little further effect on σ because of gradual variations in temperature and rpm.

2. Single hot-wire three-dimensional velocity measurement technique

A hot-wire measurement technique involving a single inclined hot-wire sensor was used to measure the periodic-average, three-dimensional flow

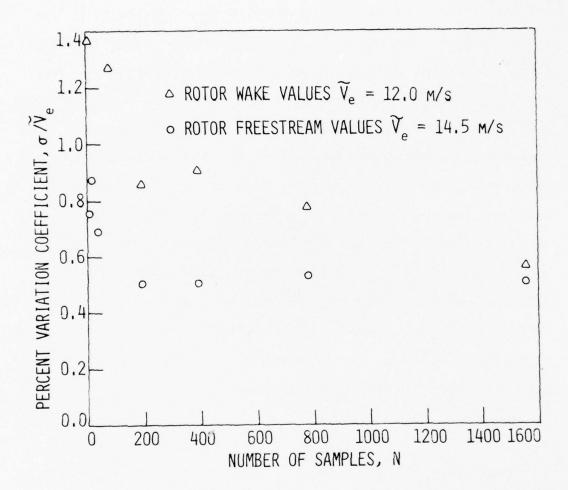


Figure 4.7. Percent variation coefficient of the periodic-sample averages for different values of N.

field in the compressor. The details related to this technique are described below.

The hot-wire probe configuration shown in a. Probe geometry Figure 4.8 relates the hot-wire sensor to the probe coordinates x, y, and z and to the velocity vector \vec{V} . The z coordinate was placed along the hot-wire probe axis while the x coordinate was located so that the sensor lay in the x-z plane. The wire sensor is represented in Figure 4.8 by the unit vector \vec{A} slanted at the angle θ to the x axis. The direction of the velocity vector with respect to the probe is defined by $\theta_{_{\mathbf{V}}}$, the probe yaw angle, and θ_{p} , the probe pitch angle. Since the probe coordinates x, y, and z were fixed to the probe, the probe angle $\boldsymbol{\theta}_{_{\boldsymbol{V}}}$ changed by the amount of turning whereas the pitch angle $\theta_{\rm p}$ remained constant as the probe was rotated about its axis. The sensor yaw angle α was defined as the angle between the velocity vector \vec{V} and the axis to the hot-wire sensor. It will be useful to note that the sensor yaw angle can be expressed in terms of the angles θ_0 , θ_p , and θ_y . The unit vector \vec{A} and the velocity vector \vec{V} expressed in terms of vector components are

$$\vec{A} = \cos \theta_0 \vec{i} + \sin \theta_0 \vec{k} \tag{4.9}$$

and

$$\vec{V} = -V \cos \theta_{p} \cos \theta_{y} \vec{i} - V \cos \theta_{p} \sin \theta_{y} \vec{j} - V \sin \theta_{p} \vec{k}$$
 (4.10)

The dot product of \vec{A} and \vec{V} is

$$\vec{A} \cdot \vec{V} = |\vec{A}| |\vec{V}| \cos(180 - \alpha) = -|\vec{V}| \cos \theta_0 \cos \theta_p \cos \theta_y - |\vec{V}|$$

$$\sin \theta_0 \sin \theta_p$$
(4.11)

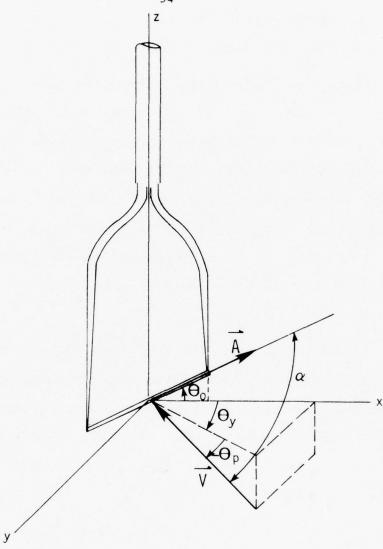


Figure 4.8. Hot-wire configuration relating velocity vector $\overset{\bigstar}{V}$ to not-wire sensor and probe coordinates x, y, z.

Hence, the sensor yaw angle relationship is

$$\cos \alpha = \cos \theta_0 \cos \theta_p \cos \theta_y + \sin \theta_0 \sin \theta_p$$
 (4.12)

b. Effective cooling velocity/actual velocity ratio — If a hotwire velocity calibration is made in the typical manner with the sensor yaw angle, α , equal to 90 degrees (wire sensor normal to the flow) and the hot-wire sensor is then used for velocity measurement at a sensor yaw angle other than 90 degrees, the velocity indicated by the sensor will not equal the actual velocity and is therefore defined as the "effective cooling velocity," V_e . V_e was related to the linearized anemometer bridge voltage, E_{ϱ} , by the empirical second order equation

$$V_{e} = K_{1} + K_{2}E_{g} + K_{3}E_{g}^{2}$$
 (4.13)

where the three coefficients K_1 , K_2 , and K_3 were determined from a velocity calibration with the wire sensor normal to the flow. The hotwire measurement technique used in the present study was based on knowing the precise relationship for the effective cooling velocity/actual velocity ratio, V_e/V . The sine law is a useful relationship for sensor yaw angles near 90 degrees:

$$\frac{V_{e}}{V} = \sin \alpha \tag{4.14}$$

Another commonly used relationship is

$$\left(\frac{v_e}{v}\right)^2 = \sin^2\alpha + k^2\cos^2\alpha \tag{4.15}$$

where k is claimed to be dependent on the sensor type and lengthto-diameter ratio. The latter relationship attributed to Champagne et al. (32) takes into consideration the residual velocity sensitivity when the velocity vector is parallel to the sensor due to the finite

The state of the s

length and nonuniform temperature of the sensor. For this experimental investigation, both the sine law and the Champagne, Sleicher, and Wehrmann relationship were judged as being inadequate for the inclined hot-wire probe and the measurement conditions involved. The sine law was not appropriate since sensor yaw angles as small as 40 degrees were encountered. Experimentally determined values of k for the Champagne, Sleicher, and Wehrmann relationship for the slant wire probe were found to vary considerably depending on sensor yaw angle and pitch angle.

Experiments showed that V_e/V was strongly dependent on sensor yaw angle, weakly dependent on pitch angle, and only very slightly dependent on velocity level. The dependence of V_e/V on sensor yaw angle was determined for several combinations of velocities and pitch angles with the calibration nozzle. Typical results for a 35.35-degree slant hot-wire sensor are shown in Figure 4.9. A second order empirical correlation was used to express the effective cooling velocity ratio as a function of sensor yaw angle, pitch angle, and velocity as follows:

$$\frac{v_e}{v} = b_0 + b_1 \alpha + b_2 \theta_p + b_3 V + b_4 \alpha^2 + b_5 \theta_p^2 + b_6 V^2 + b_7 \alpha \theta_p + b_8 \alpha V + b_9 \theta_p V$$
(4.16)

The coefficients b_0 through b_9 were determined with a least squares fit of effective cooling velocity calibration data as described in the calibration procedure section. Since the sensor yaw angle, α , and the probe yaw angle, θ_y , are geometrically related (Equation 4.12), either angle could have been selected as one of the independent variables in Equation 4.16. However, the sensor yaw angle was chosen since the dependence of V_p/V with

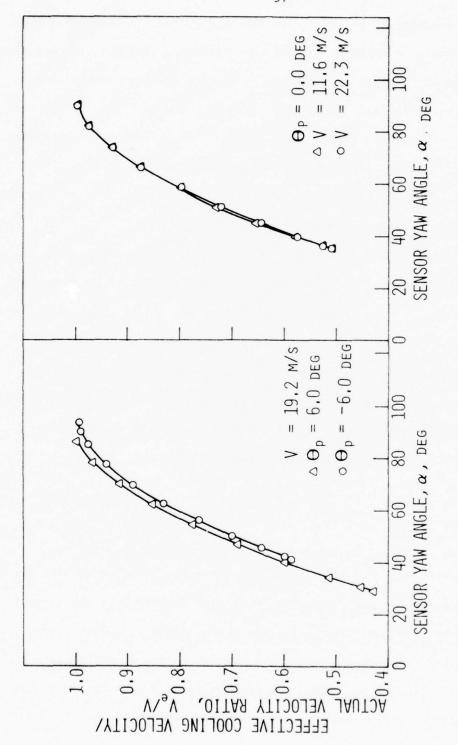


Figure 4.9. Typical effective cooling velocity calibration results for a 35-degree inclined hot wire.

respect to α facilitated correlation with a second order empirical type fit. Since hot-wire sensor behavior was not symmetrical about the axis of the probe, two sets of coefficients were used, one for each of the probe yaw angle $\theta_{_{\rm V}}$ ranges 0 to 90 degrees and 0 to -90 degrees.

c. Measurement technique Hot-wire measurements were made at compressor flow-field measurement points by positioning the hot-wire sensor and recording data at each of three probe angle orientations (a, b, and c) corresponding to probe yaw angles of $\theta_{y,a}$, $\theta_{y,b}$, and $\theta_{y,c}$ which equal:

$$\theta_{\mathbf{v},\mathbf{a}} = \theta_{\mathbf{v}} \tag{4.17}$$

$$\theta_{\mathbf{v},\mathbf{b}} = \theta_{\mathbf{v}} - \mathbf{m}_{\mathbf{b}} \tag{4.18}$$

$$\theta_{y,c} = \theta_y - m_c \tag{4.19}$$

where $m_{\tilde{b}}$ and $m_{\tilde{c}}$ are constant probe turning angle increments. For each wire orientation a geometric relationship similar to Equation 4.12 could be expressed and an effective cooling velocity relationship similar to Equation 4.16 applied. The resulting six equations are:

For position a

$$\frac{v_{e,a}}{v} = b_{0a} + b_{1a}\alpha_a + b_{2a}\theta_p + b_{3a}V + b_{4a}\alpha_a^2 + b_{5a}\theta_p^2 + b_{6a}V^2 + b_{7a}\alpha_a\theta_p + b_{8a}\alpha_aV + b_{9a}\theta_pV$$
(4.20)

$$\cos \alpha_a = \cos \theta_0 \cos \theta_p \cos \theta_y + \sin \theta_0 \sin \theta_p$$
 (4.21)

For position b

$$\frac{V_{e,b}}{V} = b_{0b} + b_{1b}\alpha_b + b_{2b}\theta_p + b_{3b}V + b_{4b}\alpha_b^2 + b_{5b}\theta_p^2 + b_{6b}V^2 + b_{7b}\alpha_b\theta_p + b_{8b}\alpha_bV + b_{9b}\theta_pV$$
(4.22)

$$\cos \alpha_{b} = \cos \theta_{0} \cos \theta_{p} \cos(\theta_{y} - m_{b}) + \sin \theta_{0} \sin \theta_{p}$$
 (4.23)

For position c

$$\frac{V_{e,c}}{V} = b_{0c} + b_{1c}\alpha_{c} + b_{2c}\theta_{p} + b_{3c}V + b_{4c}\alpha_{c}^{2} + b_{5c}\theta_{p}^{2} + b_{6c}V^{2} + b_{7c}\alpha_{c}\theta_{p} + b_{8c}\alpha_{c}V + b_{9c}\theta_{p}V$$
(4.24)

$$\cos \alpha_{c} = \cos \theta_{0} \cos \theta_{p} \cos (\theta_{y} - m_{c}) + \sin \theta_{0} \sin \theta_{p}$$
 (4.25)

The coefficients (b₀, b₁, b₂ ... b₉) in Equations 4.20, 4.22, and 4.24 were known by empirical fitting of calibration data and selected depending on whether the respective probe measurement angle ($\theta_{y,a}$, $\theta_{y,b}$, $\theta_{y,c}$) for each orientation was within the probe yaw angle calibration range of 0 to 90 or 0 to -90. Since the effective velocities $V_{e,a}$, $V_{e,b}$, and $V_{e,c}$ were measured values, six unknown variables (α_a , α_b ; α_c , θ_p , θ_y , V) remained, and the six nonlinear equations (Equations 4.20 through 4.25) could be solved simultaneously by using the Newton-Raphson numerical method. With V, θ_p , θ_y determined, the velocity vector is completely specified with respect to the probe coordinate system. The velocity vector with respect to compressor coordinates is determined by accounting for the rotation of the probe coordinate system about the compressor coordinate system. More will be said about the method of solution and transformation to compressor coordinates in the section on data reduction.

The precision of this measurement technique was largely dependent on the selection of the three probe measurement angles θ_y , a, θ_y , b, and θ_y , c. It was important to select the measurement angles in regions of high sensor yaw angle sensitivity for best resolution. As can be seen from Figure 4.9, the sensor yaw angle region near 90 degrees was unfavorable

since large variations in α (5 degrees) could result from small changes of effective cooling velocity ratio. Therefore, in this region, substantial measurement errors were likely to occur. In fact, if the sensor yaw angle was near 90 degrees at any one of the three probe angle measurement positions, the solution would not converge. In addition, sensor yaw angles near 90 degrees were also avoided since this position was most susceptible to velocity gradients along the sensor. Since the effective cooling velocity ratio was calibrated over the two distinct probe angle regions 0 to 90 and 0 to -90, probe angle measurement positions were selected to insure that the varying sensor yaw angle caused by the random variation of the velocity direction at the measurement point always remained in one of these two regions. To avoid probe prong interference, the shorter prong was always positioned into the flow upstream of the longer prong.

Figure 4.10 is a view of the three probe angle measurement positions looking along the axis of the probe. To insure acceptable probe angle measurement positions at each flow-field measurement point, the periodic-average tangential flow angle was approximately determined (within 5 degrees), and appropriate measurement positions were selected. This was done by determining the angle corresponding to minimum effective cooling velocity, $\beta_{\rm mv}$, (see Figure 4.10) while rotating the probe about its axis. The three sensor measurement positions were then located by rotating the probe from the angle $\beta_{\rm mv}$ according to the off-set angles $\theta_{\rm a}$,off, $\theta_{\rm b}$,off, and $\theta_{\rm c,off}$. Where the off-set angles were equal to:

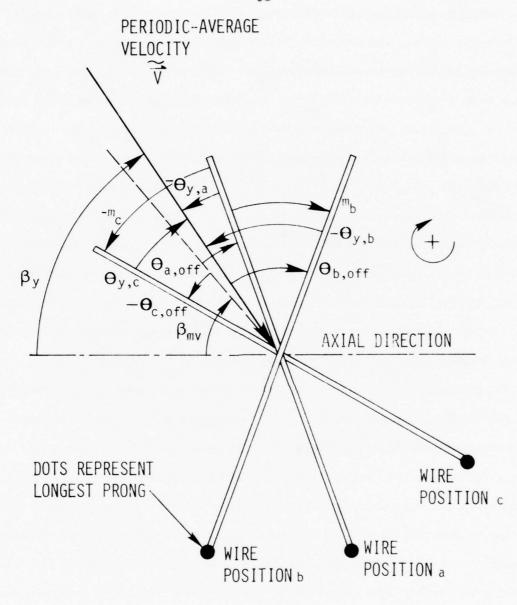


Figure 4.10. Hot-wire measurement positions and nomenclature, viewed from above along probe axis.

$$\theta_{a,off} = 20 \text{ degrees}$$

$$\theta_{b,off} = 60 \text{ degrees}$$

$$\theta_{c,off} = -20 \text{ degrees}$$

and therefore, as can be seen from Figure 4.10

$$\theta_{v,a} = \theta_v \approx -20 \text{ degrees}$$

$$\theta_{y,b} = \theta_y - m_b^{\alpha} - 60 \text{ degrees}$$

$$\theta_{y,c} = \theta_{y} - m_{c} \approx 20 \text{ degrees}$$

and

$$m_b = 40 \text{ degrees}$$

$$m_c = -40 \text{ degrees}$$

This method of positioning the sensor at each flow-field measurement point was necessary since the periodic-average tangential flow angle varied as much as 20 degrees over the circumferential traverse range.

The angle of wire inclination, θ_0 , is also an important factor in the measurement technique since it affects the sensitivity and uniqueness of solution. The measurement sensitivity to tangential and radial angles increases as θ_0 is decreased. The lower limit of θ_0 is governed by the value of the radial angle and the selection of the probe angle measurement positions. Hirsch and Kool (20) state that in order to obtain a unique solution, the pitch angle θ_p must be smaller than the value computed from

$$\tan \theta_{p} = \frac{\tan \theta_{0}}{\cos \theta_{y}} \tag{4.26}$$

which is dependent on the wire angle and probe measurement yaw angle. In addition, if θ_0 is too small, unsteady probe prong interference effects

could cause large errors for probe measurement angles near 0.0 degrees. Of the two hot-wire probes used (θ_0 of 45 and 35 degrees), the results obtained from the 35-degree probe were more consistent and judged to be more accurate. For this reason, the majority of the measurements were made with the 35-degree probe. Possibly, the accuracy can be slightly increased by further optimization of the wire angle for the measurement conditions involved.

3. Calibration procedure

A complete velocity sensing calibration of the hot wire was made employing the calibration nozzle. The probe was positioned at 0.25 nozzle orifice diameters from the nozzle exit, and at this location the static pressure was assumed to be atmospheric, and the total pressure was equal to the plenum wall static pressure over the velocity range involved. The compressor and hence calibration nozzle flow-velocity range consisted of Mach numbers less than 0.2, thus permitting the assumption of incompressible flow conditions. The nozzle jet velocity was calculated by the following equation:

$$V = \sqrt{\frac{2g_c \gamma_{H2O} \Delta P_n}{\rho}}$$
 (4.27)

where V = velocity, m/s

 $g_c = gravitational constant, 1.0 kgm/Ns^2$

 $\gamma_{\rm H_2O}$ = specific weight of manometer fluid, N/m³

 ρ = density of air, kg/m³

 ΔP_n = differential pressure between plenum pressure and atmospheric pressure, m of water

Before actual calibration took place, sufficient warm-up time was allowed for the nozzle stream temperature to reach its equilibrium state. It was possible to maintain the nozzle stream temperature to within 0.15 °K over a calibration period. Three types of hot-wire velocity sensing calibrations were made: linearizer velocity calibration, second order velocity calibration, and effective cooling velocity calibration.

a. <u>Linearizer velocity calibration</u> The anemometer linearizer approximated the hot-wire curve of effective cooling velocity versus bridge voltage with a fourth order polynomial curve. The "zero" degree polynomial term was set equal to zero, and the four polynomial coefficient values were determined with a fourth order least squares curve fit of calibration nozzle data obtained as explained below.

The hot-wire sensor was positioned in the nozzle jet stream normal to the flow by optical alignment with a telescope. The cold resistance of the sensor was measured and the anemometer resistance deck was set corresponding to an overheat ratio (operating sensor resistance/cold sensor resistance) of 1.8 using the relationship

 $R_{s,op,d} = 1.8(R_{s,c,d} - R_{cb} - R_{ph} - R_{pl}) + R_{cb} + R_{ph} + R_{pl}$ (4.28)

R_{s.op.d} = sensor operating resistance deck setting, ohms

 $R_{s,c,d} = cold resistance read off anemometer resistance deck, ohms$

R_{cb} = cable resistance, ohms

 $R_{\rm ph}$ = probe holder resistance, ohms

 R_{pl} = probe lead resistance, ohms

The cable and probe holder resistances were measured using an impedance bridge and a shorting probe while the probe lead resistance was specified by the manufacturer of the hot-wire probe. The following parameters were recorded at the beginning and end of the calibration run:

- (1) Barometric pressure, inches of Hg
- (2) Barometer ambient temperature, °F
- (3) Room temperature, °F
- (4) Nozzle stream temperature, millivolts
- (5) Anemometer standby voltage, volts

Anemometer voltage and plenum pressure readings were taken at 16 velocity level values over a range of 0.0 to 23 m/s. After the last calibration point was recorded, a calculator program proceeded to reduce the data and to determine the polynomial coefficients. In addition, the percent error each data point between the actual nozzle jet velocity determined with Equation 4.27 and the velocity predicted by the polynomial relationship was calculated. The majority of errors were within 0.25% and none were larger than 1.0%. The coefficient potentiometers of the linearizer were then adjusted to reflect the four calculated polynomial coefficients, and the zero suppression and input gain of the linearizer were adjusted (see Ref. 33). The linearizer velocity calibration was performed initially for each hot-wire probe and thereafter approximately every 40 hours of actual running time.

b. <u>Second order velocity calibration</u> As mentioned previously, a second order relationship between the linearized anemometer bridge voltage and the effective cooling velocity with the form

$$V_e = K_1 + K_2 E_{\ell} + K_3 E_{\ell}^2$$
 (4.13)
where

 V_e = effective cooling velocity, m/s

 E_{ϱ} = anemometer linearizer output voltage, volts

 K_1 , K_2 , and K_3 = least square coefficients was used to determine the effective cooling velocity from the measured linearized anemometer bridge voltage. A velocity calibration was made to determine the three coefficients K_1 , K_2 , and K_3 by a least squares fit of calibration nozzle data.

For this calibration, the position of the sensor was also aligned normal to the flow, and an overheat ratio of 1.8 was used. The barometric pressure, barometer ambient temperature, room temperature, and nozzle stream temperature were taken before and after the calibration test. The anemometer linearizer output voltage and the plenum pressure were recorded at 14 points over a velocity range from 4 to 23 m/s. The three coefficients and the percent error at each calibration point were then computed by the calculator calibration program. The error between the actual calibration velocity and the predicted velocity from the second order equation was almost always within 1% or better. This second order velocity calibration was made before each circumferential blade-to-blade survey in the compressor, and was also used in the calibration of effective cooling velocity described in the next section.

c. Effective cooling velocity calibration A comprehensive calibration procedure was followed to determine the coefficients involved in the previously presented V_ρ/V relationship

the same of the same of the

$$\frac{v_{e}}{v} = b_{0} + b_{1}\alpha + b_{2}\theta_{p} + b_{3}V + b_{4}\alpha^{2} + b_{5}\theta_{p}^{2} + b_{6}V^{2} + b_{7}\alpha\theta_{p} + b_{8}\alpha V + b_{9}\theta_{p}V$$
(4.16)

The effective cooling velocity calibration was made over the entire velocity, probe yaw angle θ_y , and pitch angle θ_p measurement ranges expected in the compressor. The coefficients were obtained and spot checked approximately every 30 hrs of running time and the calibration was repeated when the drift was discerned to be greater than 2.0 to 3.0%.

The slant hot-wire probe was mounted near the calibration nozzle exit in a manual actuator which allowed both probe yaw angle and pitch angle variation (see Figure 3.9). The hot-wire sensor was zeroed in the actuator with the optical telescope and was positioned so that the center of the sensor remained at the same point in the nozzle flow stream for various θ_y and θ_p . A second order velocity calibration of the linearized anemometer voltage was first made to determine the coefficients K_1 , K_2 , and K_3 in Equation 4.13. The nozzle stream and atmospheric conditions were recorded and the effective cooling velocity calibration involving the following velocity, pitch angle, and probe yaw angle levels was begun:

Velocity 11.6, 15.2, 19.2, 22.3, m/s

Pitch angle -9 to 6, degrees, in increments of 3 degrees

Probe yaw 0 to 90, degrees, in increments of 5 degrees angle 0 to -90, degrees, in increments of 5 degrees

The probe yaw angle was varied over each range for each pitch angle setting and each velocity level. At every probe yaw angle position, the probe yaw angle was recorded along with the linearized anemometer voltage, and the calculator was used to perform the following preliminary calcula-

tions and steps:

- The actual velocity was calculated from nozzle data with Equation
 4.27.
- (2) The effective cooling velocity was determined from the linearized anemometer voltage with the second order velocity relationship, Equation 4.13.
- (3) The sensor yaw angle α was calculated using Equation 4.12.
- (4) V_{ρ}/V was calculated.

After all the calibration data were taken, the ten coefficients in Equation 4.16 were determined with a least squares method (see Appendix D), one set for the probe yaw angle range 0 to 90 degrees and another set for the angle range 0 to -90 degrees. In order to inspect the accuracy of the $V_{\rm e}/V$ relationship, the percent error between the measured velocity and the predicted velocity ratio from Equation 4.16 was calculated. The majority of errors were within 0.80% and no errors were greater than 2.0%.

4. Data acquisition

Three-dimensional, periodic-average, compressor flow-field velocity measurements were made with the periodic-sampling-and-averaging method and the slant hot-wire measurement technique. Circumferential traversing surveys of velocity were made between the blade rows over the first two stages of the compressor with the stationary blade rows set for minimum sound. The measurement location, rotor blade setting position YO_{R} , and periodic-sampling circumferential survey method (frozen rotor-blade type or passing rotor-blade type) for each survey are summarized in Table 4.1. The rotor setting position YO_{R} , is the periodic-sampling position of the

Table 4.1. Specifications for periodic-average hot-wire circumferential surveys, all measurements were made at the minimum sound stationary blade-row schedule.

Probe Measurement Station	Percent Passage Ht. from Hub PHH	Rotor Position YO _R /S _R	Periodic	-Sampl	ing Method	Probe Wire Angle θ ₀ degrees
3	10	0.0	Frozen r	otor-b	lade survey	35
3	20	0.0	11	11	"	35
3	30	0.0		**	n	45
3	40	0.0	11	11	11	35
3	50	0.0	11	"	"	35
3	50	0.17	"	"	**	35
3	50	0.28	11	11	11	35
3	50	0.28	Passing	rotor-	blade surve	y ^a 35
3	50	0.50	Frozen r	otor-b	lade survey	35
3	50	0.69	"	"	"	35
3	50	0.69	Passing	rotor-	blade surve	y ^b 35
3	50	0.83	Frozen r	otor-b	lade survey	35
3	60	0.0	11	11	"	35
3	70	0.0	ff	"	"	45
3	80	0.0	u	"	11	45
3	90	0.0	"	"	**	35
4	50	0.0	"	**	**	35
4	50	0.17	"	11	11	35
4	50	0.34	ti.	**	11	35
4	50	0.50	n n	11	"	35
4	50	0.69	***	"	**	35
4	50	0.83	11	11	11	35
5	50	0.0	11	11	**	35
5	50	0.17	m .	11	11	35
5	50	0.34	"	"	11	35
5	50	0.50	"	"	"	35
5 5	50	0.67		***	"	35
5	50	0.83	n n	**	u ,	35
6	50	0.00	"	**		35
6	50	0.34	"	**	"	35
6	50	0.67	***	**	"	35

 $^{^{\}mathrm{a}}$ Circumferential position of stationary blade rows set at Y = 3.50.

 $^{^{\}mathrm{b}}$ Circumferential position of stationary blade rows set at Y = 0.00.

first rotor blade in each rotor row, when the circumferential traversing position Y is equal to zero. YO_R is measured as the angular circumferential distance from the probe-traversing measurement stations to the periodic-sampling position of the rotor blade stacking axis, and is positive in the direction of rotor rotation. Measurement errors due to temperature variation and dirt accumulation on the hot-wire sensor were minimized by maintaining the room and compressor flow passage temperatures constant at their respective values to within 0.5 $^{\rm o}$ K for the duration of a test and by frequent calibration of the hot-wire sensor. The remaining portion of this section is a detailed description of the data procurement procedure.

Several preliminary steps were required before measurements were made in the compressor. The alignment telescope was used to position the slant hot-wire sensor in the probe actuator so that the hot-wire probe prongs were in line with the compressor axis with the shortest prong forward when the actuator angle indicator read 0.0 degrees. After the initial warm up, the instruments were electronically zeroed and the linearizer coefficient adjustments were made. The voltages from the circumferential motion actuator potentiometer and the probe actuator yaw angle motion potentiometer were correlated to their respective motions using a linear least squares correlation. The circumferential position of the stationary blade rows relative to each other were set corresponding to the minimum sound placement schedule (see Table 5.1). The stationary blade rows were connected to the circumferential motion actuator for periodic-average frozen rotor-blade flow-field surveys. For the passing rotor-blade flow-field

surveys, the stationary blade rows were moved jointly to a circumferential position Y specified for the test with the minimum sound schedule maintained, but the blade rows were not connected to the circumferential motion actuator. For either type of periodic-average survey, the periodic-sampling rotor blade position ${\rm YO}_{\rm R}$ was set to the desired value for each test by moving the photoelectric pickup to the appropriate position and subsequently locking its movement to the circumferential motion actuator.

Immediately before each circumferential traversing survey, a second order hot-wire velocity calibration was performed with the sensor positioned at the calibration nozzle normal to the flow (see Figure 4.11) and with the linearized anemometer signal routed through the periodic-sampling and averaging circuits. The sensor operating resistance was set corresponding to an overheat ratio of 1.8. The temperature of the fluid flowing through the calibration nozzle was maintained to within 0.5 $^{\rm O}$ K of the compressor fluid temperature. From the calibration, the three coefficients K_1 , K_2 , and K_3 of Equation 4.13 were determined as described previously. After calibration, the probe actuator was positioned at a compressor probe traversing station and the radial position of the hotwire sensor was set.

The following miscellaneous parameters were recorded in order to completely specify the measurement conditions:

- (1) Probe traversing station number, see Figure 3.1
- (2) Passage height position from hub, inches
- (3) Periodic-sampling rotor position setting YO_R , degrees

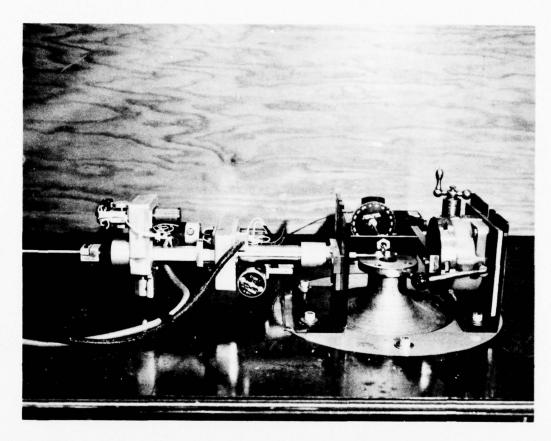


Figure 4.11. Probe actuator positioned at calibration nozzle for hot-wire velocity calibration.

- (4) Stationary blade position settings ${
 m YO}_{1{
 m GV}}, {
 m YO}_{1{
 m S}}, {
 m YO}_{2{
 m S}}, {
 m YO}_{3{
 m S}},$ degrees
- (5) Measurement offset angles $\theta_{a,off}$, $\theta_{b,off}$, $\theta_{c,off}$, degrees
- (6) Actuator linear correlation coefficients, for immersion, probe yaw angle, and circumferential traversing movements
- (7) Date
- (8) Barometric pressure, inches of Hg
- (9) Barometer ambient temperature, °F
- (10) Differential pressure across venturi, inches of water
- (11) Temperature at venturi throat, millivolts
- (12) Room temperature, °F
- (13) Compressor flow passage temperature, millivolts
- (14) Compressor rpm
- (15) Compressor rpm variation
- (16) Hot-wire sensor angle θ_0 , degrees
- (17) Calculator sampling and averaging number related to N
- (18) Sensor resistance overheat ratio Roh
- (19) Sensor operating resistance $R_{s,op}$, ohms
- (20) Sensor cold resistance R_{s,c}, ohms
- (21) Anemometer bridge standby voltage, volts

In order to insure the same compressor operating conditions for each test, the flow coefficient was calculated preceding the test using flow rate venturi meter data. Before activating the hot-wire anemometer, the anemometer bridge standby voltage was checked against the recorded calibration value, and the sensor operating resistance was set according to the

value used during calibration. A four channel time-base oscilloscope was used to observe the behavior and to detect any anomalies of the output signals from the triggering circuit, anemometer linearizer, sample-and-hold circuit, and electronic averaging circuit. Two X-Y channel storage oscilloscopes were used to display the periodic-average voltage signal from the electronic averaging circuit, one as a function of probe yaw angle position and the other as a function of circumferential traversing position Y. A qualitative trace on the oscilloscope was made of the circumferential varying velocity profile to determine the best circumferential distribution of flow-field measurement points.

A series of repetitive steps were then taken to obtain the hot-wire data. First, the circumferential position Y was set by adjusting the position of the circumferential motion actuator and was recorded by the calculator. Next, the approximate tangential flow angle β_{mv} was determined, and the hot-wire sensor was positioned at the three measurement orientations in the manner described previously. For each orientation, the effective cooling velocity was measured and recorded using the periodic-sampling-and-averaging technique. This point-by-point measurement procedure was repeated for each of 30 flow-field measurement points over one stator blade spacing.

After the last circumferential point, the data were printed on thermal sensitive paper and recorded on magnetic tape for reduction at a later time. If time remained, the second order hot-wire velocity calibration was repeated and another circumferential survey was made.

5. Data reduction

The reduction of the hot-wire data involved solving the six nonlinear simultaneous equations (Equations 4.20 through 4.25) at each flow-field measurement point and expressing the solution in terms of the compressor coordinate system. The Newton-Raphson method which is a general technique for finding real roots of simultaneous transcendental equations (see Ref. 31) was used to solve these six equations. The solution convergence rate was typically about 5 iterations but never greater than 100 iterations per solution point. The convergence rate seemed to be dependent on the selection of the probe angle measurement positions, the initial guess of the unknowns, and the accuracy required of the solution.

The compressor coordinate system is shown in Figure 4.12. The Z and R coordinates are respectively directed along the machine axis and radius of the compressor, while the Y axis is in the direction of rotor rotation. The direction of the velocity vector with respect to the compressor is completely specified by the absolute tangential angle β_y and the radial angle β_r . The sign convention for β_y , β_r and the velocity components V_z , V_y , and V_r (axial, tangential, and radial) are shown in the figure. Since the probe was immersed radially into the compressor, the probe coordinate axis z and compressor coordinate axis R were coincident. As the probe was rotated about its axis, the probe coordinate system (x, y, z) rotated about the compressor coordinate system with Y and Z, and x and y axes always in the same plane. The pitch angle and the radial angle could be related by

$$\beta_{\mathbf{r}} = -\theta_{\mathbf{p}} \tag{4.29}$$

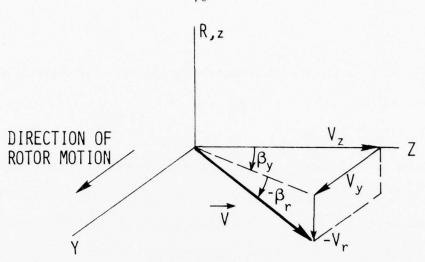


Figure 4.12. Compressor coordinate system showing nomenclature and sign convention for three-dimensional fast-response velocity and angle parameters.

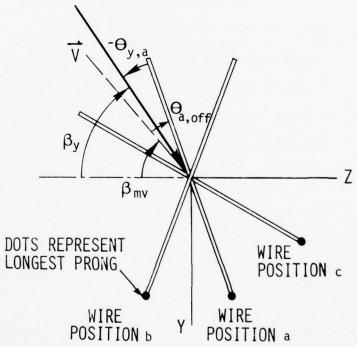


Figure 4.13. Hot-wire measurement positions with respect to compressor coordinates Y and Z.

Since

$$\theta_{\mathbf{y},\mathbf{a}} = \theta_{\mathbf{y}} \tag{4.30}$$

The tangential angle transformation relationship from inspection of Figure 4.13 is

$$\beta_{y} = \beta_{mv} + \theta_{a,off} + \theta_{y} \tag{4.31}$$

The values of β_{mv} and $\theta_{a,off}$ were recorded during data acquisition, and the value of θ_y was determined solving the six simultaneous equations. In addition to V, β_y , and β_r , the following velocity and angle parameters were calculated at each flow-field measurement point:

- (1) Axial velocity, m/s, Eq. 12.55
- (2) Absolute tangential velocity, m/s, Eq. 12.56
- (3) Radial velocity, m/s, Eq. 12.57
- (4) Relative velocity, m/s, Eq. 12.59
- (5) Relative tangential velocity, m/s, Eq. 12.58
- (6) Relative tangential angle, degrees, Eq. 12.60

A circumferential integrated average for each parameter was also computed. A complete listing of the equations used appears in Appendix C.

V. PRESENTATION AND DISCUSSION OF DATA

The results involving the sound pressure level (SPL) data, slowresponse data, and fast-response hot-wire data are presented and discussed
in this section. The primary flow field parameters for the slow and fast
response data are tabulated in Appendices E and F. In graphing the results,
all data variation curves were drawn through the actual data points; statistical curve fitting of the data was not attempted.

A. Sound-Pressure Level Measurement Results

The variation of overall SPL measured at the compressor inlet over the rpm range of the compressor at a constant flow coefficient of 0.42 is shown in Figure 5.1 for each of the two cases obtained by adjusting the circumferential position of the IGV blade row (the stator blade rows were not moved) for minimum and maximum noise. It should be noted that varying the IGV row circumferential position resulted in significant changes of the compressor inlet noise level at rotor speeds greater than 700 rpm. At rotor speeds below 600 rpm, moving the IGV row had little if any effect on the noise level detected at the compressor inlet. The spinning mode "cut-off" rotor speed (see Tyler and Sofrin (15)) required for the propagation of blade-row interaction noise established by the number of rotor and stator blades per row in the research compressor was independently estimated as being about 610 rpm. These results seem to indicate that the level of discrete frequency noise due to adjacent blade row interaction can be influenced by stationary blade-row circumferential positioning at rotor speeds greater than the "cut-off" amount. The varying amounts of

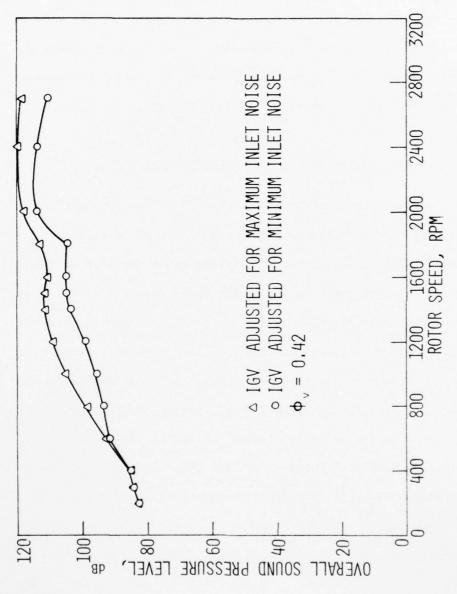
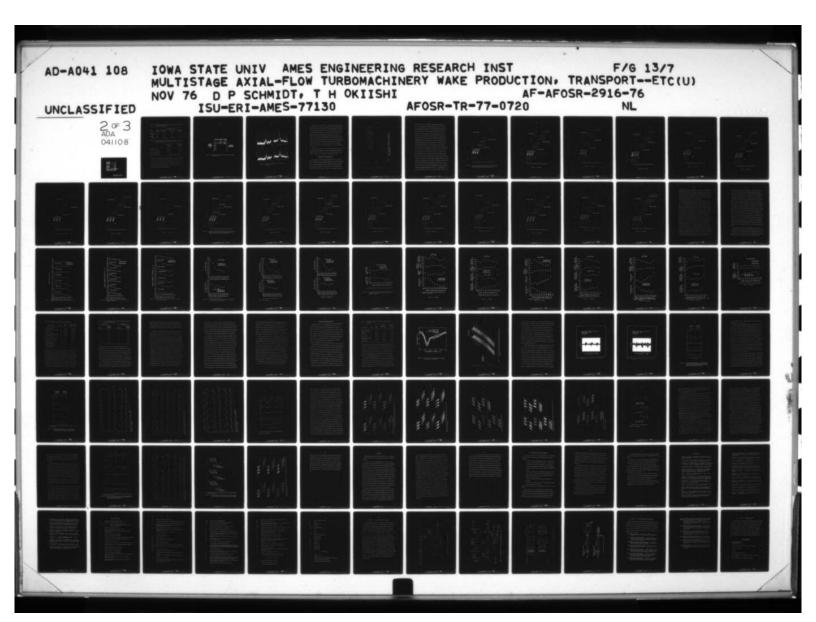


Figure 5.1. Compressor inlet noise level over compressor rpm range.

compressor inlet noise reduction possible at the different rotor speeds may be related to the proportions of noise reduction attributable to wake cancellation and sound wave interference. As pointed out by Walker and Oliver (5), a combination of these phenomena is the probable cause of noise variation with circumferential placement of stationary blade rows. It appears as if more sound-pressure level data at various rotor speeds are required before this aspect of noise reduction is understood.

The stationary blade-row circumferential settings (all of the stationary blade rows were set) for minimum and maximum noise at a rotor speed of 1400 rpm and a flow coefficient of 0.42 are presented in Table 5.1. These circumferential position schedules were each found to be distinct and uniquely obtainable on a repeatable basis. The circumferential positioning of the IGV, first stator, and second stator blade rows was critical, whereas the placement of the third stator row had little effect on the overall sound level (1 dB variation range) perceived at the inlet.

Overall SPL and octave band SPL analyses of the compressor inlet noise at the minimum and maximum noise blade-row schedules (specified in Table 5.1) are presented in Table 5.2. A difference in the overall SPL of 11.5 dB was measured, and in terms of the perceived sound this is equivalent to about a 1/2 reduction in relative annoyance as defined by Sofrin (see Figure 5.2). The SPL octave band analyses were found to differ for the two cases within the 500 and 1000 Hz bands only, which are nearest to the rotor blade passing frequency of 887 Hz. A narrow band spectrum analysis for each of both minimum and maximum noise conditions (see



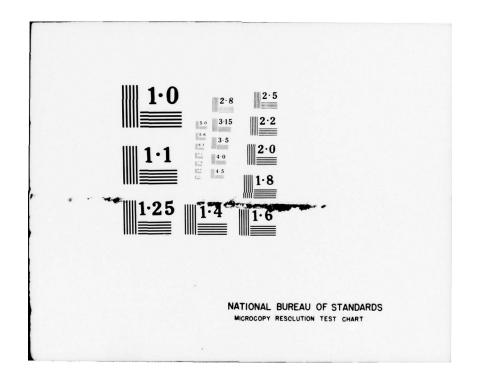


Table 5.1. Stationary blade-row circumferential placement schedules for minimum and maximum sound.

Noise Level			Blade-Row Schedule	
	IGV YO _{IGV} /S _S	First Stator YO1s/S	Second Stator YO _{2S} /S _S	Third Stator YO3S ^{/S} S
Minimum sound	0.000	0.1285	0.5601	-0.2261
Maximum sound	0.000	0.5447	0.1439	0.1490

Table 5.2. Overall and octave band analyses of compressor inlet noise for minimum and maximum noise blade-row schedules.

	Minimum Noise Blade-Row Schedule	Maximum Noise Blade-Row Schedule
Overall SPL (flat)	101.0 dB	112.5 dB
500 Hz octave band SPL	92.5 dB	98.5 dB
1000 Hz octave band SPL	96.5 dB	112.8 dB
Other octave band SPL	Insignificant	difference

Figure 5.3) shows large and distinct discrete frequency noise level peaks at the first and second harmonics of blade passing frequency. Also shown are some broadband noise peaks. The spectrum analyses point out that the reduction in noise level obtained by proper circumferential positioning of the stationary blade rows involved the discrete frequency noise only. No change in broadband noise could be discerned.

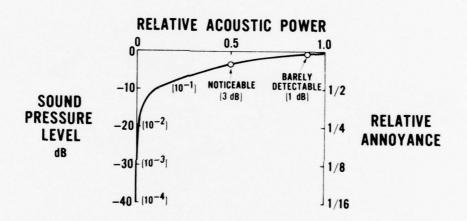


Figure 5.2. Required noise reduction for subjective improvement from Sofrin (11).

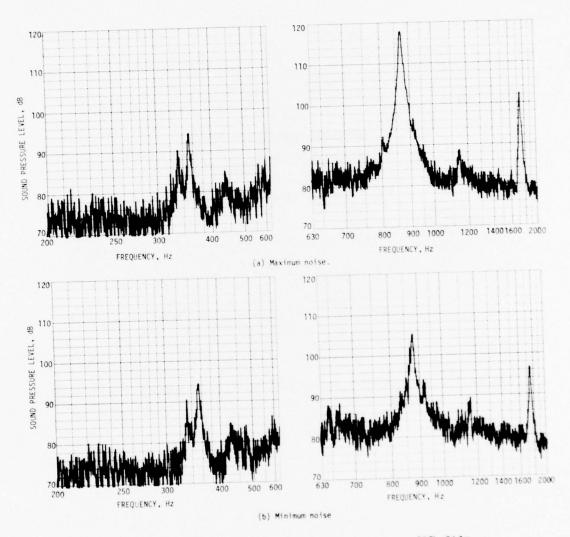


Figure 5.3. Compressor inlet noise spectrum (1% filter bandwidth).

A similar noise level reduction in a low-speed, single-stage, axial-flow compressor also with identical numbers of IGV and stator blades per row was obtained by Walker and Oliver (5) through appropriate circumferential positioning of the IGV and stator blade rows. Variations in SPL at the first and second harmonics of the rotor blade passing frequency were achieved by varying the circumferential position of the IGV row. The difference in SPL between the maximum and minimum IGV row positions was chiefly at the rotor blade passing frequency. Although inlet noise level reduction was attributed to wake cancelling (stator blade section pressure fluctuation reduction) and sound wave interference, Walker and Oliver (5) concluded, on the basis of a test involving removal of the downstream stator row, that wake cancelling eliminates much of the noise generated by the stator row.

In order to further explain the inlet noise reduction achieved in the Iowa State University research compressor with appropriate positioning of stationary blade rows, detailed slow- and fast-response measurements were obtained. These data are discussed in the following sections.

B. <u>Slow-Response Measurement Results</u>

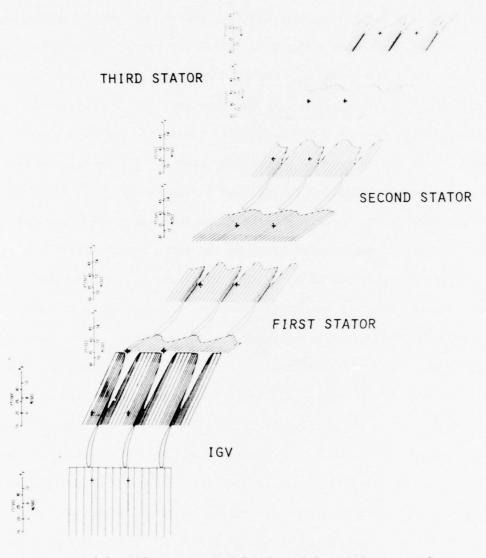
The results of the slow-response measurements were used to obtain a physical description of the time-average fluid flow field ahead and behind each of the blade rows of the research compressor for each of the conditions of minimum and maximum inlet noise. Blade-to-blade plane velocity vector plots were constructed to graphically depict the circumferentially varying average fluid flow field. In Figure 5.4, an example of one such

MEASUREMENT



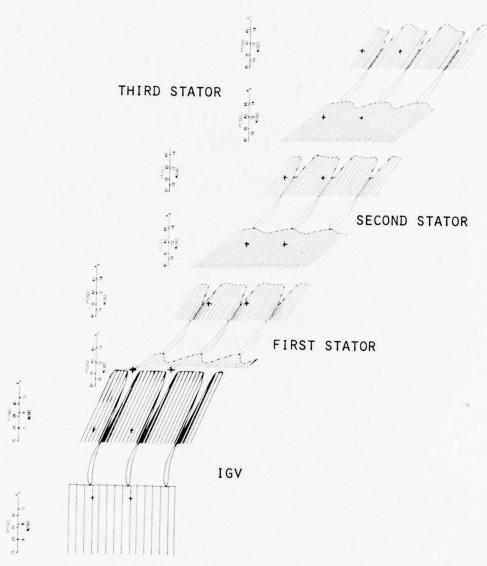
Figure 5.4. Blade-to-blade plane, time-average, velocity vector plot for first stator at mid-span (constructed from slow-response data).

vector plot is shown. This particular illustration represents the velocity flow field ahead and behind the first stator at 50% passage height for minimum sound. Although measurements were obtained over only one stator blade pitch distance, the flow pattern was periodically repeated over approximately three blade pitch intervals to aid in data interpretation. Also, although the data were obtained "in line" with respect to the axial direction as mentioned earlier, the plots were shifted relative to each other to better illustrate the fluid flow development. As can be seen in Figure 5.4, each circumferential survey measurement station location is depicted in the vector plots by a line extending through the two cross marks positioned one blade pitch apart. At each flow-field measurement point at the probe survey station, a velocity vector (represented by a line) was drawn at the circumferentially averaged absolute tangential flow angle. The length of each vector (or line) is related to the absolute velocity magnitude. The left-hand velocity scale specifies the axial velocity level. It should be noted that the magnitude of the velocity vectors are zero suppressed by the amount indicated on the axial velocity scale in order to amply display velocity level variations. Blade-to-blade vector plots similar to the one in Figure 5.4 were made for each of the four stationary blade rows at each of nine radial positions and were combined to represent the absolute timeaverage flow field through the three stages of the compressor at each of the nine constant passage height measurement locations. These combined velocity vector plots for the minimum and maximum noise blade-row position schedules are presented in Figures 5.5 and 5.6. In these figures, the axial and circumferential positions of the blade profiles as well as the



(a) 10% passage height from hub; minimum sound.

Figure 5.5. Blade-to-blade plane, time-average, velocity vector plots at constant passage height for the minimum sound blade-row schedule; constructed from slow-response data.



(b) 20% passage height from hub; minimum sound.

Figure 5.5. Continued.

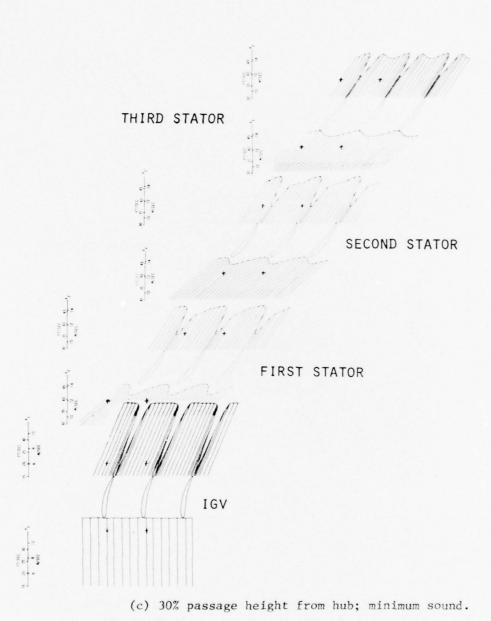
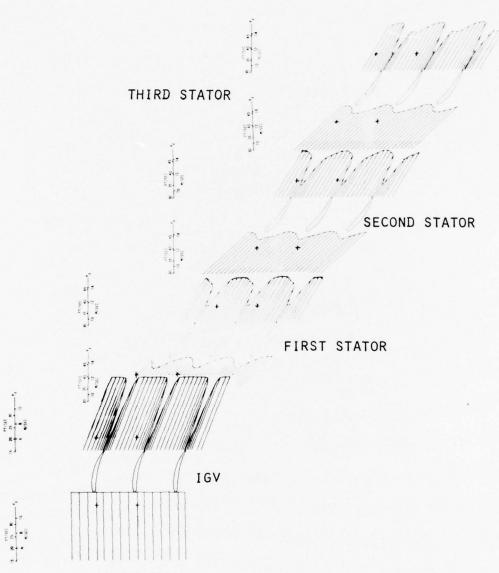
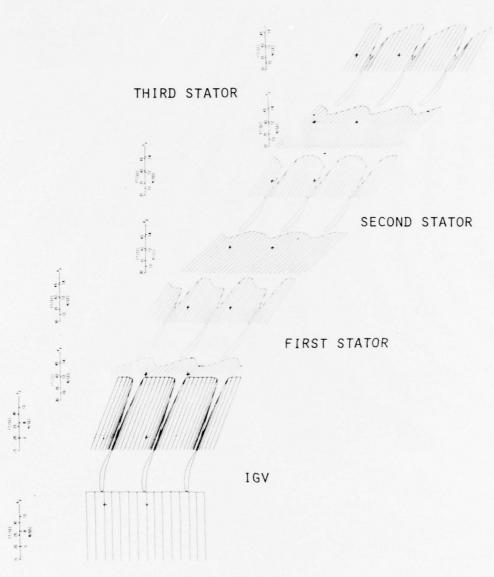


Figure 5.5. Continued.



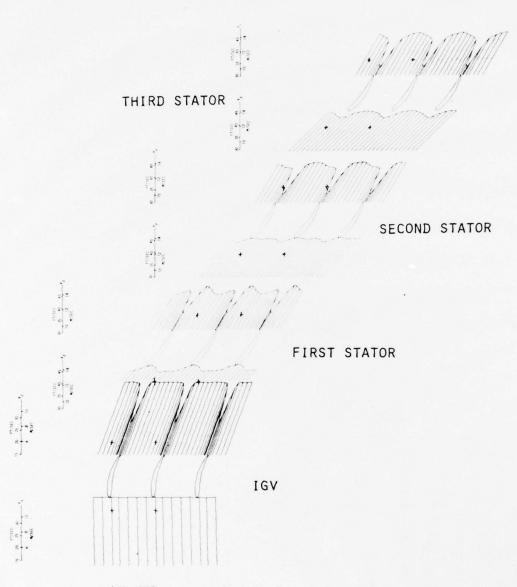
(d) 40% passage height from hub; minimum sound.

Figure 5.5. Continued.



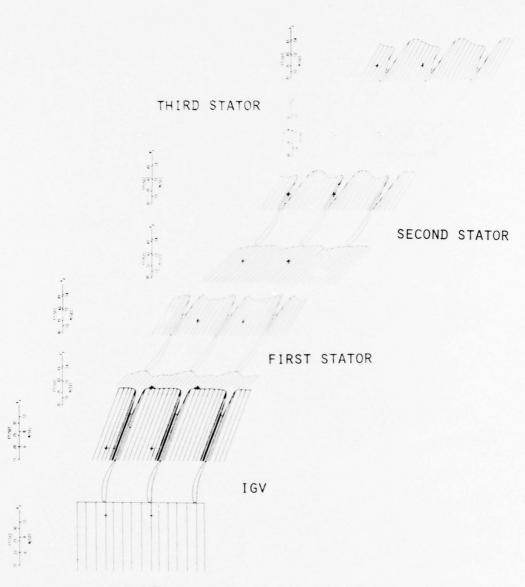
(e) 50% passage height from hub; minimum sound.

Figure 5.5. Continued.



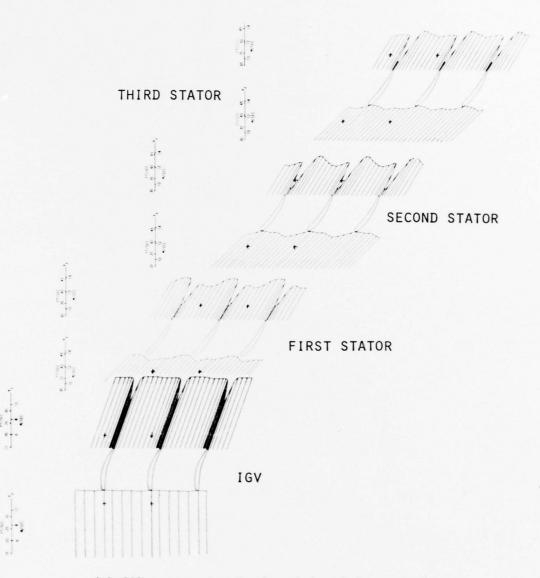
(f) 60% passage height from hub; minimum sound.

Figure 5.5. Continued.



(g) 70% passage height from hub; minimum sound.

Figure 5.5. Continued.



(h) 80% passage height from hub; minimum sound.

Figure 5.5. Continued.

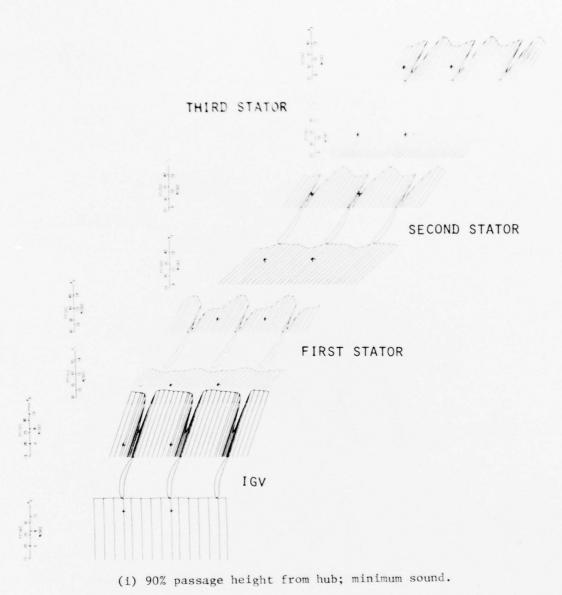
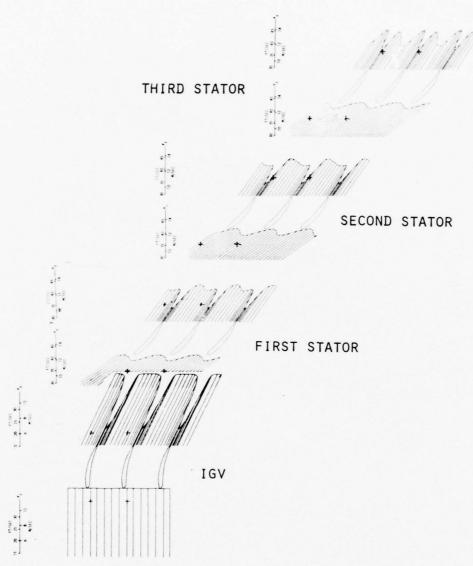
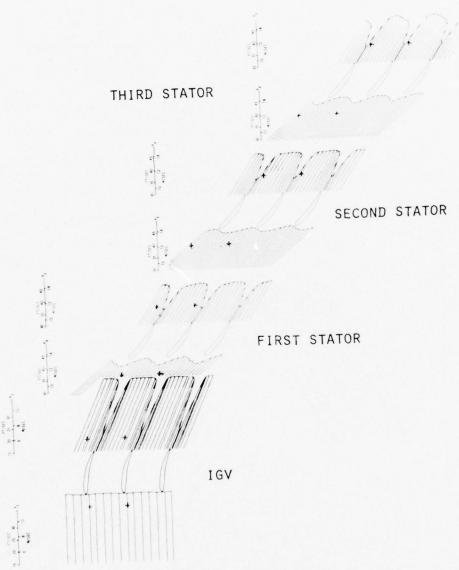


Figure 5.5. Concluded.



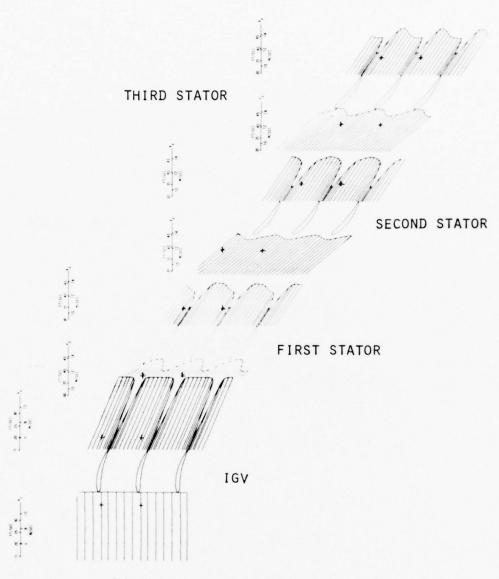
(a) 10% passage height from hub; maximum sound.

Figure 5.6. Blade-to-blade plane, time-average, velocity vector plots at constant passage height for the maximum sound blade-row schedule; constructed from slow-response data.



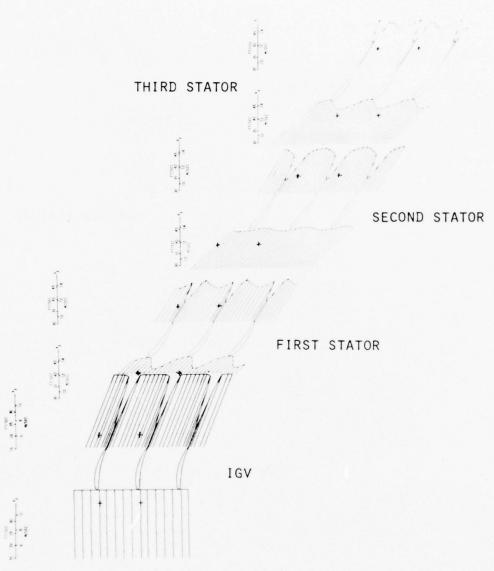
(b) 20% passage height from hub; maximum sound.

Figure 5.6. Continued.



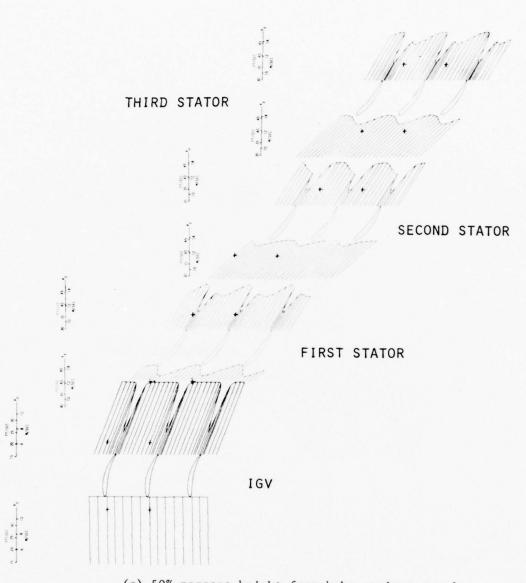
(c) 30% passage height from hub; maximum sound.

Figure 5.6. Continued.



(d) 40% passage height from hub; maximum sound.

Figure 5.6. Continued.



(e) 50% passage height from hub; maximum sound.

Figure 5.6. Continued.

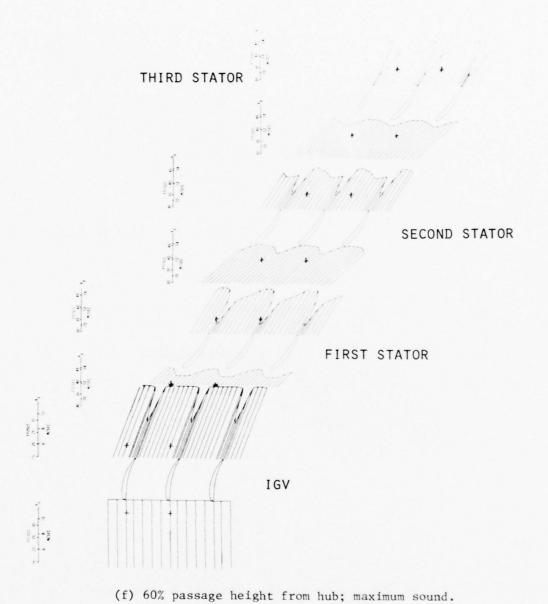
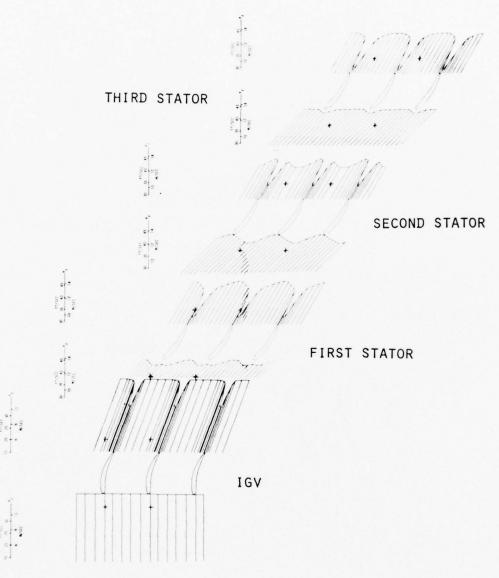
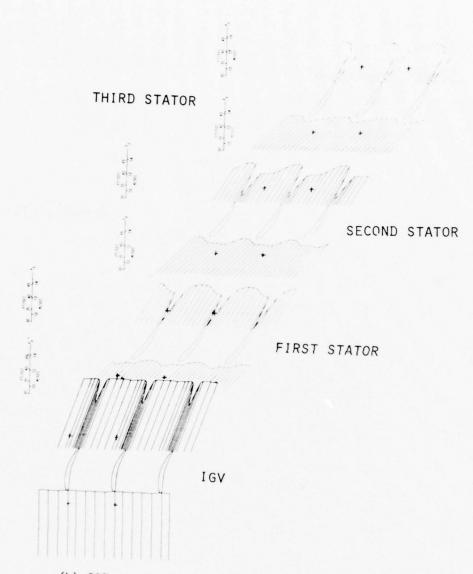


Figure 5.6. Continued.



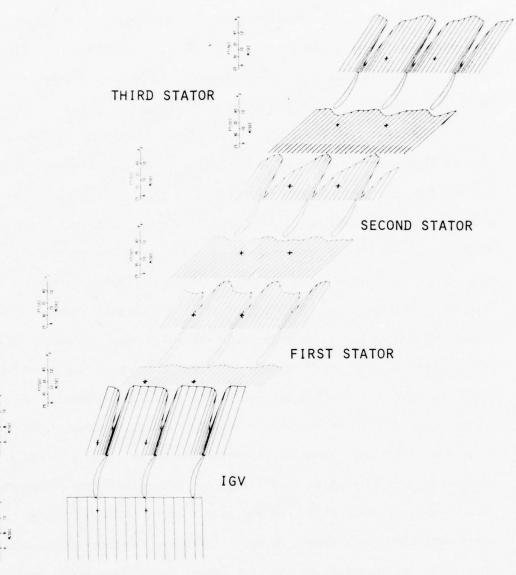
(g) 70% passage height from hub; maximum sound.

Figure 5.6. Continued.



(h) 80% passage height from hub; maximum sound.

Figure 5.6. Continued.



(i) 90% passage height from hub; maximum sound.

Figure 5.6. Concluded.

blade section size, shape, and angles are in scale with the actual blade configuration of the research compressor. Although the rotor blade profiles are not shown, the axial spacings between measurement stations are also scaled correctly. As indicated by the crosses, the vector plots were shifted circumferentially by one or more stator pitch distance increments to increase the effectiveness of the combined plots.

Some observations about the slow-response instrument average stationary flow patterns are apparent from the blade-to-blade velocity vector plots. The stationary flow pattern could be changed appreciably in regions of the compressor annulus by varying the circumferential positions of the stationary blade rows relative to each other. Figures 5.5 and 5.6 show that throughout a large portion of the compressor annulus, the wakes from the stationary blade rows influenced the flow downstream of the next rotor even though the stationary blade row wakes were attenuated to a large extent as they moved through the rotor blade row. As observed by Smith (2), this substantial attenuation is expected because of the unequal energy addition and the dispersive chopping action involved within the rotor rows. Further, these stationary blade row wake streets exiting from the rotors were attenuated very little as they passed through the next downstream stationary blade row and were a discernable influence on the stationary blade exit flow. In most instances, the shape of a stator exit flow field was dependent on the position of that stator blade leading edge relative to the incoming stationary periodic flow pattern, as can be seen, for example, when comparing the first stator exit flow fields in Figures 5.5d and 5.6d (40% span). In general, if a stator blade leading edge was positioned within the incoming stationary wake street, identified as the

region of lower velocity (see for example the first stator flow in Fig. 5.5c), that stator blade produced a deeper velocity wake ("wakes together" type profile) than if the stator blade leading edge was moved out of the wake street ("wakes apart" type profile). When a stator blade leading edge was positioned out of the incoming wake street region (see for example the first stator flow in Figure 5.6d), the velocity deficit at that stator inlet could be identified in the stator exit freestream region. Also, by changing the circumferential position of one blade row, the flow pattern could in some instances be modified more than one blade row downstream. For example, comparison of Figures 5.5f and 5.6f indicates a change in the flow field behind the second rotor due to a change in the relative circumferential position between the IGV and first stator blade rows. Further, this change in the flow field behind the second rotor affected the flow field of the second stator. The data also make evident the fact that stationary interaction patterns changed with radius. For example, the stationary circumferential position of the wake street at a rotor exit varied with blade span. In general, the circumferentially periodic flow patterns at the inlet to a stator row were in circumferential phase at two span locations resulting in similar stator exit flow profiles at those two spanwise positions (e.g., compare Figures 5.5b and 5.5g).

The spanwise distribution of circumferential-average flow field parameters ahead of and behind each of the blade rows are shown in Figures 5.7 through 5.11. These results should be interpreted with the uncertainty levels listed in Table 5.3 in mind. The parameter precision bounds were based on the uncertainties associated with determining total

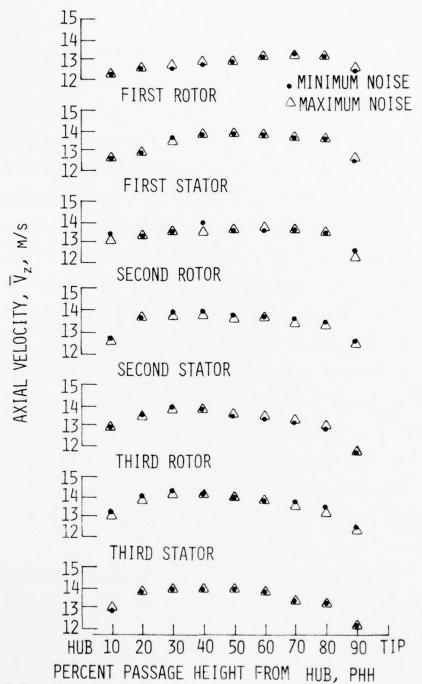
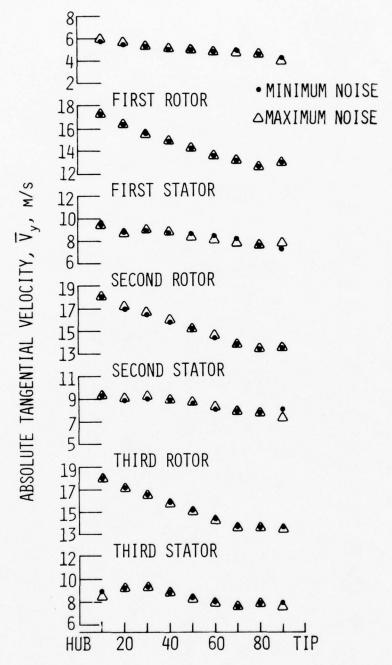


Figure 5.7. Circumferential-average axial velocity blade span distribution.



PERCENT PASSAGE HEIGHT FROM HUB, PHH

Figure 5.8. Circumferential-average absolute tangential velocity blade span distribution.

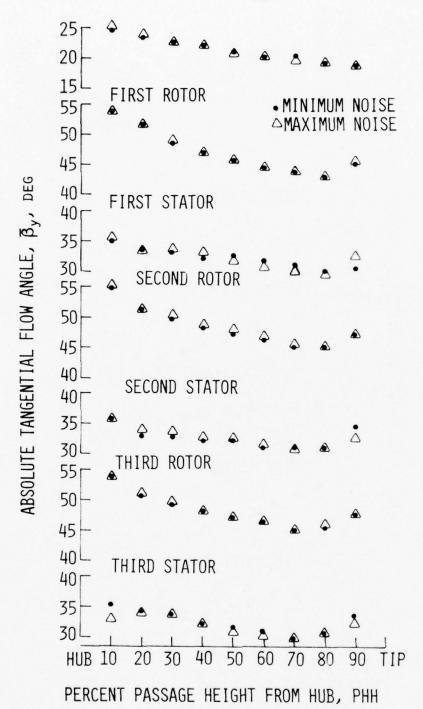
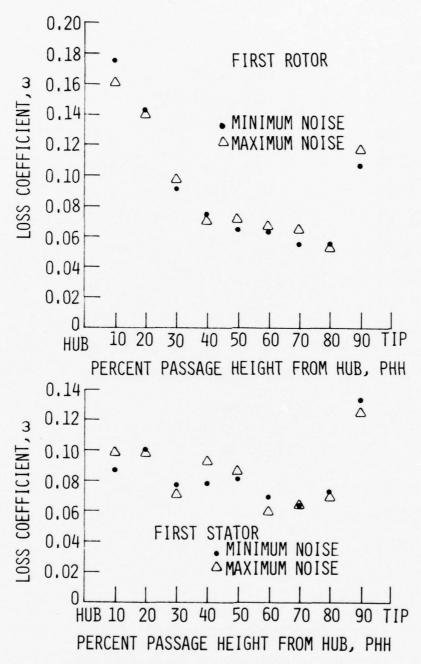
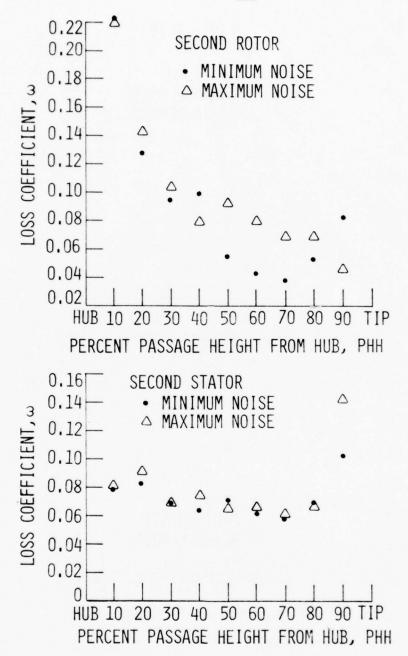


Figure 5.9. Circumferential-average absolute tangential flow angle blade span distribution.



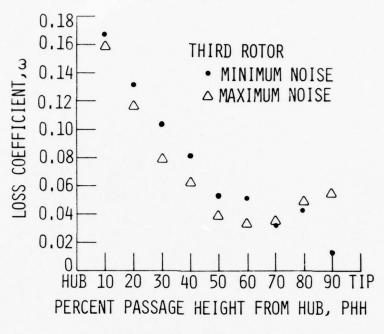
(a) First rotor and first stator.

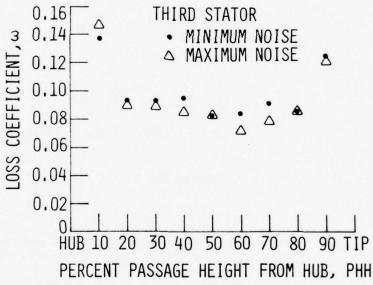
Figure 5.10. Blade span distribution of total-head loss coefficient for rotor and stator blade rows.



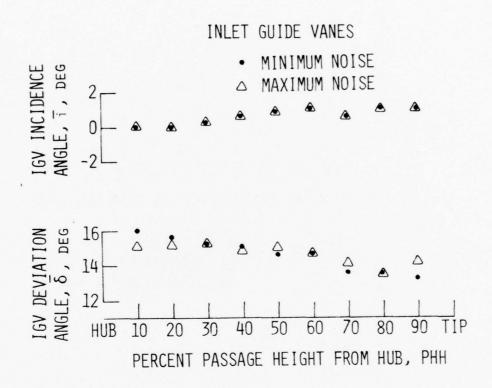
(b) Second rotor and second stator.

Figure 5.10. Continued.



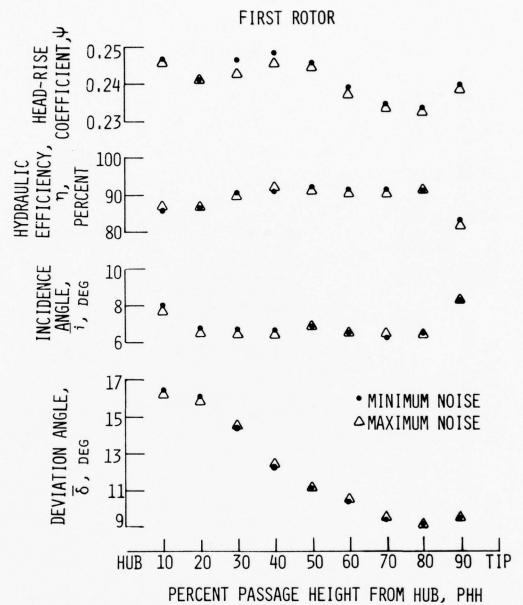


(c) Third rotor and third stator.
Figure 5.10. Concluded.



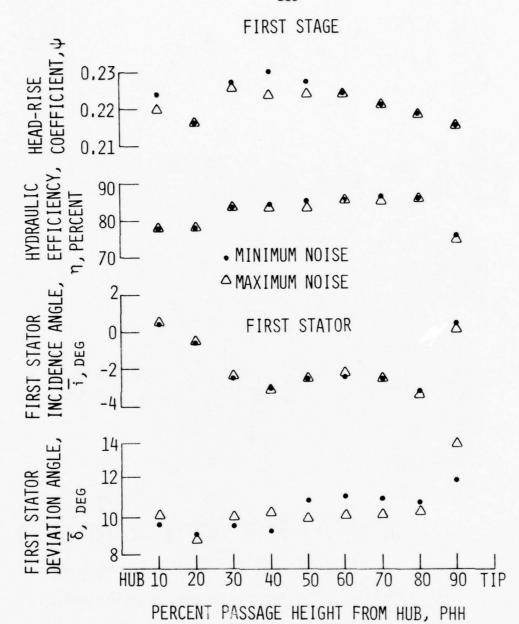
(a) Incidence and deviation angles for inlet guide vanes.

Figure 5.11. Blade span distribution of incidence and deviation blade angles, rotor and stage head-rise coefficient and hydraulic efficiency.



(b) Head-rise, efficiency, and incidence and deviation angles for first rotor.

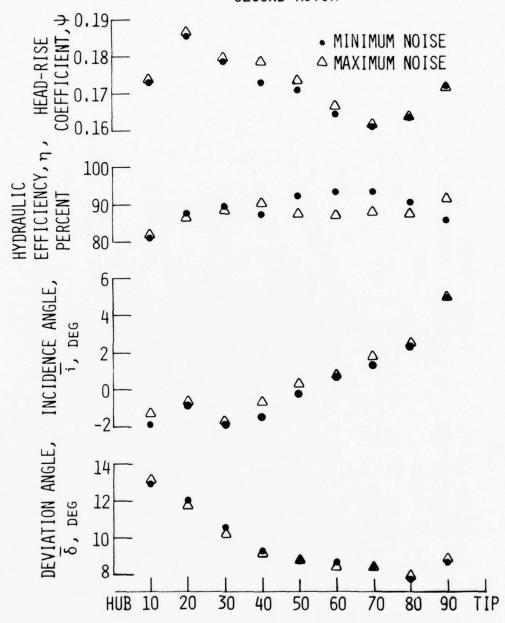
Figure 5.11. Continued.



(c) Head-rise and efficiency for first stage and incidence and deviation angles for first stator.

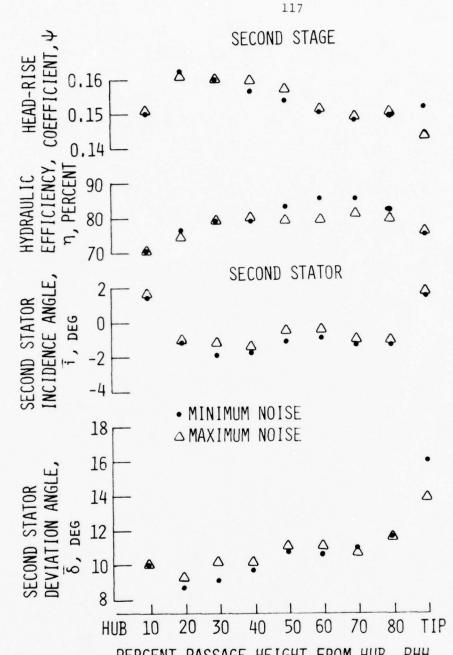
Figure 5.11. Continued.

SECOND ROTOR



PERCENT PASSAGE HEIGHT FROM HUB, PHH

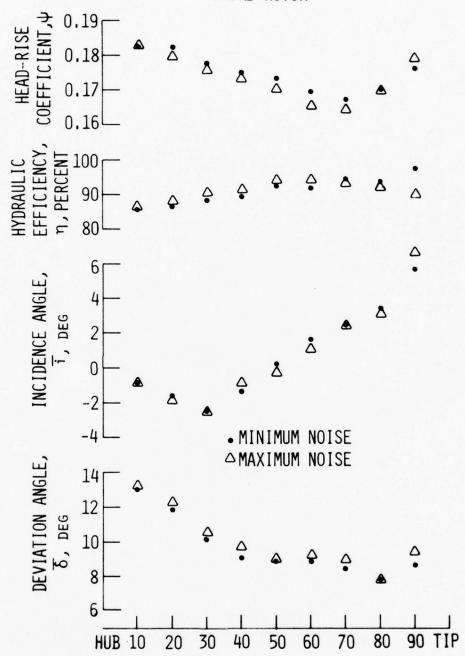
(d) Head-rise, efficiency, and incidence and deviation angles for second rotor. Figure 5.11. Continued.



PERCENT PASSAGE HEIGHT FROM HUB, PHH Head-rise and efficiency for second stage and incidence and deviation angles for second stator.

Figure 5.11. Continued.

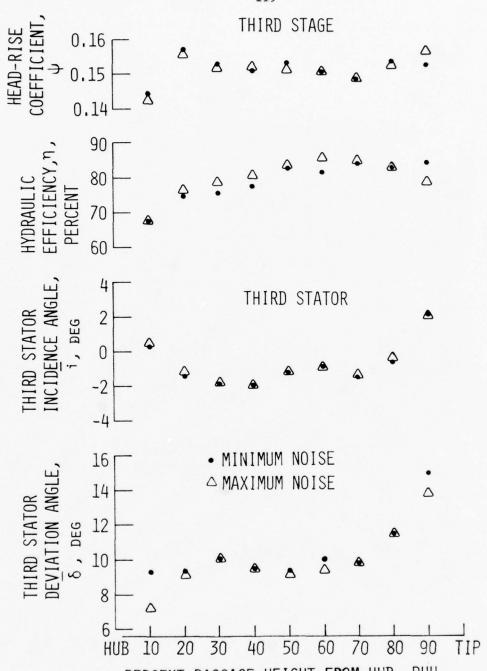
THIRD ROTOR



PERCENT PASSAGE HEIGHT FROM HUB, PHH

(f) Head-rise, efficiency, and incidence and deviation angles for third rotor.

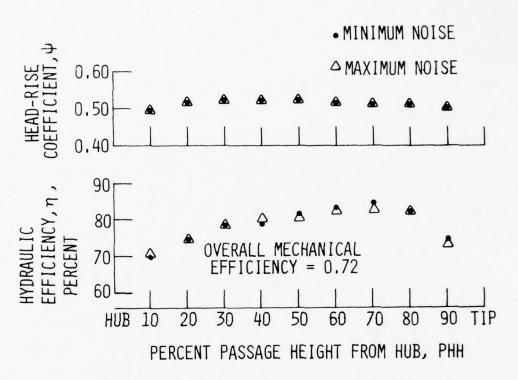
Figure 5.11. Continued.



PERCENT PASSAGE HEIGHT FROM HUB, PHH Head-rise and efficiency for third stage and incidence and deviation angles for third stator.

Figure 5.11. Continued.

ALL THREE STAGES



(h) Head-rise and efficiency for overall compressor.
Figure 5.11. Concluded.

Table 5.3. Uncertainty levels of slow-response parameters.

Flow Parameters	Symbol	Typical Values	Estimated Uncertainty (20 to 1 odds)
Absolute velocity	V	20.0 m/s	0.14 m/s
Absolute tangential flow angle	Ву	40.0 deg	0.5 deg
Axial velocity	Vz	14.0 m/s	0.20 m/s
Absolute tangential velocity	v _y	10.0 m/s	0.20 m/s
Relative tangential flow angle	B' _V	45.0 deg	0.5 deg
Head-rise coefficient	Ψ	0.24	0.003
Ideal head-rise coefficient	$^{\Psi}\mathbf{i}$	0.27	0.006
Hydraulic efficiency	η	0.85	0.05
Stationary row total-head- loss coefficient	ωs	0.08	0.015
Rotating row total-head- loss coefficient	$^{\omega}$ R	0.08	0.020

pressure, static pressure, and absolute flow angle. The bounds are generally consistent with the random scatter observed in the results. It should be noted that constant radius blade sections were involved in calculating the results instead of blade-elements formed by the intersection of approximate stream surfaces and the blades. The results of the comparison between the integrated flow rate at each station and the venturi flow rate is shown in Table 5.4 for both the minimum and maximum noise conditions. In the calculation of the integrated flow rates for each station, the annulus boundary layer was neglected, causing the integrated values to be greater than the venturi values. The flow rate

Table 5.4. Flow rate comparison between venturi and integrated measurement station flow rates.

Minimum Noise		Maximum Noise	
Station	Flow Rate Comparison Percent	Station	Flow Rate Comparison Percent
1	4.4	1	4.1
2	1.9	2	2.3
3	6.5	3	6.3
4	7.1	4	5.9
5	7.5	5	6.8
6	4.2	6	4.2
7	7.6	7	6.9
8	6.0	8	6.4

comparison values varied a great deal among the eight stations, but values between the same stations for minimum and maximum noise varied less than the axial velocity uncertainty noted in Table 5.3 (1.5%). Although the flow parameter differences between the minimum and maximum noise conditions were difficult to precisely ascertain due to the uncertainty involved, it was possible through careful interpretation of the velocity vector plots and the circumferential-average values to distinguish a few blade-row performance differences over limited regions of the blade span.

A comparison between the minimum and maximum noise values of axial velocity, absolute tangential velocity, and absolute tangential flow angle indicate only small differences (see Figures 5.7, 5.8, and 5.9) over the measured blade span region. However, even small differences in these

parameters could significantly affect the calculated values of blade losses and hydraulic efficiencies. Blade section loss coefficients are shown in Figure 5.10, while head-rise coefficients, hydraulic efficiencies, and blade incidence and deviation angles are presented in Figure 5.11.

Considerable flow losses through the IGV blade row occurred over a large portion of the blade span as made evident by the deep velocity wakes produced by the IGV (see Figures 5.5 and 5.6). These IGV wakes caused the first rotor incidence angle to vary by as much as 20 degrees. Over the region of blade span where the deepest IGV wakes occurred (10% to 50%), the circumferential variation in velocity behind the first rotor was the most pronounced. Since the upstream potential flow effects from the first stator on the first rotor were probably negligible at the blade row spacing involved, there was no reason to expect the performance of the first rotor to be different for minimum and maximum noise conditions. Any differences in blade loss, head-rise coefficient, hydraulic efficiency and flow angles for the first rotor (see Figures 5.10a and 5.11b) were thus interpreted as an indication of the measurement and data reduction precision involved. A significant local difference in first stator blade loss coefficient and first stage head-rise coefficient between the minimum and maximum noise conditions is indicated in Figures 5.10a and 5.11c at 40% passage height from the hub. Figures 5.5d and 5.6d suggest that at this passage height location the first stator exit wake patterns were considerably different. The wake pattern for minimum noise was of the deep "wakes together" type (lower loss), while the wake profile for

maximum noise was of the shallow "wakes apart" type (maximum loss). At 60%, the opposite trend in loss coefficient difference and stator exit flow patterns may be observed. Further, the first stator deviation angle data for the spanwise region from 40% to 70% passage height from the hub indicate that slightly higher (1 degree) deviation angles may be generally related to those instances when the inlet guide vane streets were not in line with the stator blade leading edges ("wakes apart" type profile).

The second stage rotor blade loss coefficients and hydraulic efficiencies (Figures 5.10b and 5.11d) were significantly different for minimum and maximum noise conditions over the blade span range from 40% to 90% passage height from the hub. Over this region, the local blade span hydraulic efficiencies differed by as much as 6% depending on whether the maximum or minimum noise configuration was used. These rotor performance differences were attributed to changes in the second rotor inlet (first stator exit) pattern produced by IGV and first stator wake interaction (see Figures 5.5 and 5.6). Rotor blade section losses were less and efficiencies were greater when the rotor inlet wake pattern was of the shallower "wakes apart" type profile rather than the deeper "wakes together" type. The shallower inlet wake patterns produced less variation in rotor incidence angle and blade loading. The opposite trends in wake pattern shapes at 40% and 60% passage heights for minimum and maximum noise resulted in consistently opposite trends in the loss and efficiency values. The second stage efficiency (Figure 5.11e) was greater for minimum sound over the blade span range from 50% to 80% passage height due to efficiency gains in the second rotor. The local stage efficiency at 90% passage height for minimum and maximum noise was approximately the same since the second rotor efficiency gain for maximum noise at this location was opposed by the high losses of the 90% span second stator blade section. It is apparent from Figure 5.6i that the high second stator losses were related to secondary flow in this region of the annulus. The second stator deviation angle at this location was about 2 degrees less for maximum sound than for minimum sound. This is one example where improper circumferential placement of the stationary blade rows relative to each other has lead to adverse flow conditions.

The most significant difference in the performance of the third stage rotor occurred at 90% passage height, as indicated in Figures 5.10c and 5.11f. Apparently, losses at 90% rotor blade span for maximum noise were considerably higher due to the large second stator wakes incurred at the rotor inlet. The large positive fluctuations in rotor incidence angle from the inlet flow variation caused a greater tendency for the flow to separate at the rotor suction surface. As indicated by Figure 5.10c, there was no significant third stator performance difference between minimum and maximum noise conditions. For the entire third stage, the efficiency was significantly better for minimum noise at 90% passage height and slightly better for maximum noise at 30%, 40% and 60% passage heights (see Figure 5.11g). As can be seen from Figures 5.5a and 5.6a, a secondary flow region was measured behind the third stator at 10% passage height from the hub. The hub surface at this location was stationary.

No measurable differences in overall hydraulic or mechanical efficiencies (Figure 5.11h) could be detected for the entire compressor.

C. Fast-Response Measurement Results

Fast-response results from three-dimensional hot-wire measurements of the periodic-average flow field between blade rows of the first two stages of the research compressor for the minimum noise condition are discussed in this section. These circumferential survey results are presented in the form of velocity scalar and vector plots. The scalar information includes the blade-to-blade distribution of axial velocity, absolute tangential velocity, radial velocity, absolute tangential angle, and radial angle. The vector plots involve the blade-to-blade plane distribution of individually measured velocities. As defined previously (see Figure 4.12), the radial velocity and radial angle are positive when directed outward toward the annulus outer surface.

The uncertainty and scatter associated with the determination of the fluid velocity and flow angle parameters were estimated and are indicated in Table 5.5. The uncertainty represents the accuracy associated with the flow field parameters, whereas the scatter reflects the point-to-point irregularity of the circumferentially varying parameter distributions. In estimating the uncertainty of each parameter, several factors were considered including: (1) velocity calibration accuracy, (2) calibration drift due to working fluid temperature variation and dirt accumulation on the wire, (3) number of periodic samples N (see Figure 4.7), (4) hot-wire angle alignment accuracy, and (5) comparison with slow-response results. A comparison of the slow-response and fast-response results is shown in Figure 5.12. The six hot-wire periodic-average axial velocity profiles obtained behind the first stator for six different instantaneous positions

Table 5.5. Uncertainty and scatter of periodic-average flow field parameters.

Flow Parameters	Symbol	Typical Values	Estimated Uncertainty (20 to 1 odds)	Estimated Scatter (20 to 1 odds)
Absolute velocity	v	18.0 m/s	0.8 m/s	0.15 m/s
Absolute tangentia angle	1 β _y	40.0 deg	1.5 deg	1.0 deg
Radial angle	βr	0.0 deg	2.0 deg	1.5 deg
Axial velocity	Vz	13.0 m/s	0.7 m/s	0.3 m/s
Absolute tangentia velocity		12.0 m/s	0.6 m/s	0.4 m/s
Radial velocity	v _r	0.0 m/s	0.5 m/s	0.4 m/s

of the rotor shaft are shown along with the corresponding slow-response circumferential distribution. The figure shows good agreement between the two sats of results with the largest velocity deviation (3%) being within the uncertainty limits set forth in Table 5.5. The predicted values of scatter in Table 5.5 were based on the typical random irregularity of the results and were determined by considering the deviation of the data points about a smooth gradual damped curve formed by the data points.

Hot-wire measurements made behind the first rotor at 50% passage height indicate that the rotor wake exit flow pattern changed dramatically with rotor blade circumferential position due to the influence of the upstream IGV blade row. From the slow-response results, the IGV wake street at the first rotor exit could be identified as a region of lower velocity as shown in Figure 5.13. Points A and B in Figure 5.13 corre-

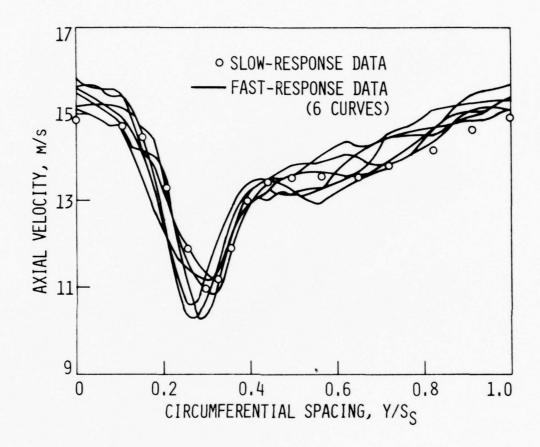
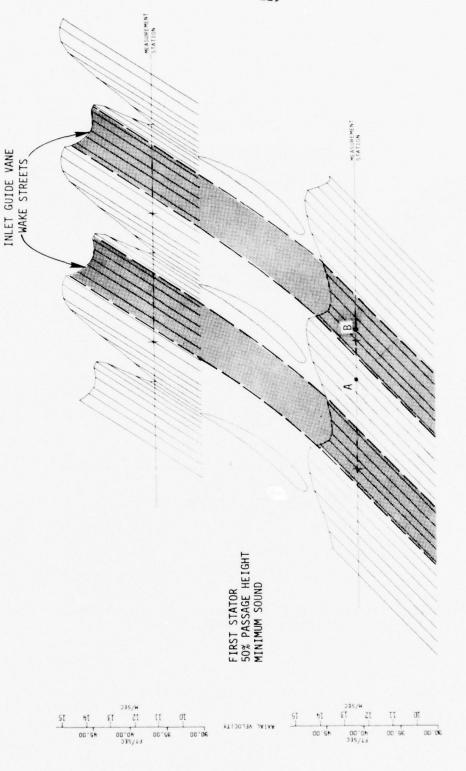


Figure 5.12. Comparison of slow-response and fast-response data behind the first stator.



variation for first stator with inlet guide vane wake streets Mid-span slow-response instrument averaged velocity vector shown. Figure 5.13.

passage height behind the first rotor. The multiple oscilloscope traces shown in Figures 5.14 and 5.15 represent the first rotor exit flow field at locations A and B. The traces were made using a single hot-wire sensor normal to the radial and average flow directions. The oscilloscope was synchronized to trace the wire signal as the same three rotor blades moved by the sensor. Comparison of the two traces indicate a larger amount of random unsteadiness and deeper rotor wakes in the IGV wake street (location B). The trend related to random unsteadiness is in agreement with the observations of Walker and Oliver (5). However, the deeper rotor wakes related to the IGV wake street noted in the ISU compressor do not agree with the shallower rotor wakes seen in the IGV street region by Walker and Oliver (5).

Three-dimensional periodic-average hot-wire results acquired at locations A and B with the passing rotor-blade flow-field survey method (see page 49) are shown in Figure 5.16. It should be noted that the wake profiles are circumferentially shifted due to the difference in the rotor blade setting position ${\rm YO_R/S_R}$ corresponding to the two distinct positions of the hot wire. The results clearly contrast the periodic-average first rotor wake profiles in and out of the IGV wake street. The wake produced by the rotor is much deeper, and the variation in absolute tangential flow angle is as much as 6 degrees greater within the IGV wake street (location B). However, the radial velocity and radial angle profiles are similar for both cases with centrifugation occurring in the wake region as expected. The general common trends in circumferential variation of flow quantities indicated by both sets of data in Figure 5.16 are in agreement

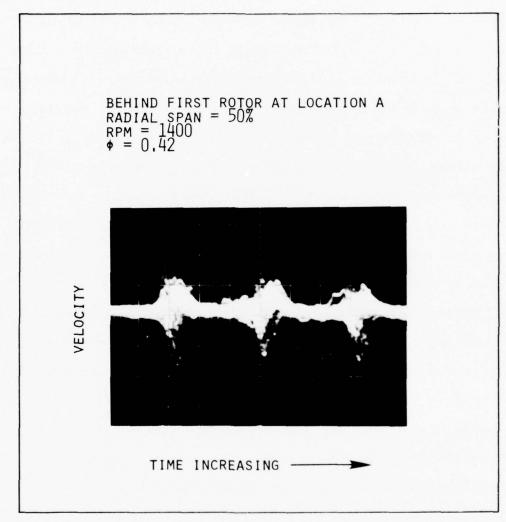


Figure 5.14. Multiple oscilloscope traces of hot-wire signal for location A.

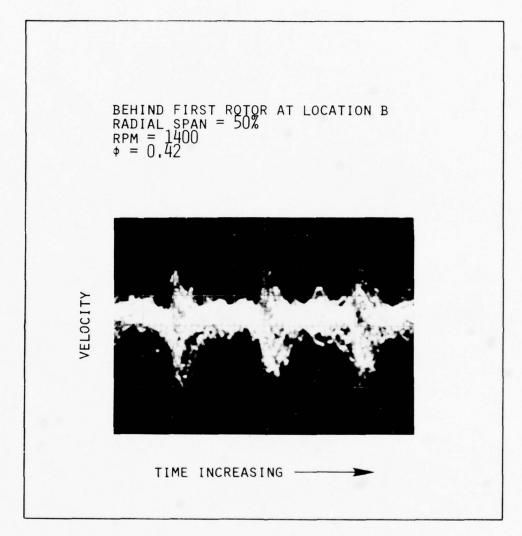


Figure 5.15. Multiple oscilloscope traces of hot-wire signal for location $\ensuremath{\mathtt{B}}.$

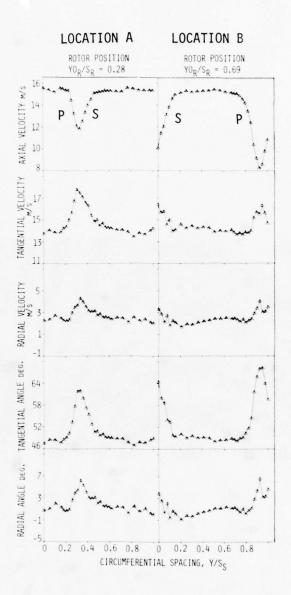
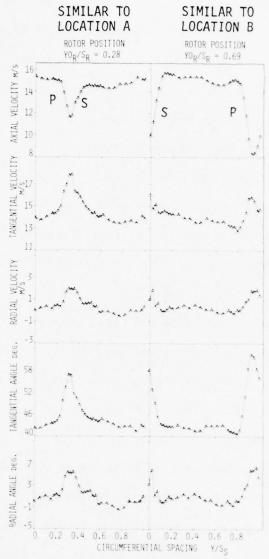


Figure 5.16. Circumferential distribution of periodic-average flow field parameters behind the first rotor at 50% passage height for locations A and B, obtained with passing rotor-blade survey method.

with those observed by others in the past (Hirsch and Kool (20), Raj and Lakshminarayana (13) and Evans (12)).

Measurements similar to those in Figure 5.16 behind the first rotor at 50% passage height were obtained using the frozen rotor-blade flowfield survey method (see page 49). The results, shown in Figure 5.17a, were acquired by effectively circumferentially moving the hot wire past the periodically frozen rotor and stationary blade row configuration. With the "frozen" rotor blade section position set at $YO_R/S_R = 0.69$, the rotor wake fell within the IGV wake street. With the rotor position set at $YO_R/S_R = 0.28$, the rotor wake was outside of the IGV wake street. These results are generally similar to those in Figure 5.16. However, the stationary flow pattern from the IGV wake street at the rotor exit is discernible only in the latter case, Figure 5.17a. In Figure 5.17a, the dip in the axial velocity level near a circumferential spacing of about 0.65 reflects the IGV row flow pattern upstream of the rotor. Since the frozen rotor-blade flow-field survey method appeared to provide a more detailed description of the flow field, it was used to obtain all further results as shown in the rest of Figure 5.17.

Data for four additional frozen rotor-blade section positions behind the first rotor at 50% passage height are shown in Figure 5.17b along with the results from the two rotor positions of Figure 5.17a. In general, the depth and width of the rotor wakes at each rotor position varied between the two profiles already discussed and shown in Figure 5.17a. At each rotor position, the slow moving fluid contributing to the IGV wake street can be consistently identified as a velocity deficit region near a circumferential spacing, Y/S_S , of 0.65. Further analysis of the general flow



(a) First rotor exit flow at 50% passage height, similar to results in Figure 5.16.

Figure 5.17. Circumferential distribution of periodic-average flow field parameters obtained at different rotor positions with frozen rotor-blade survey method.

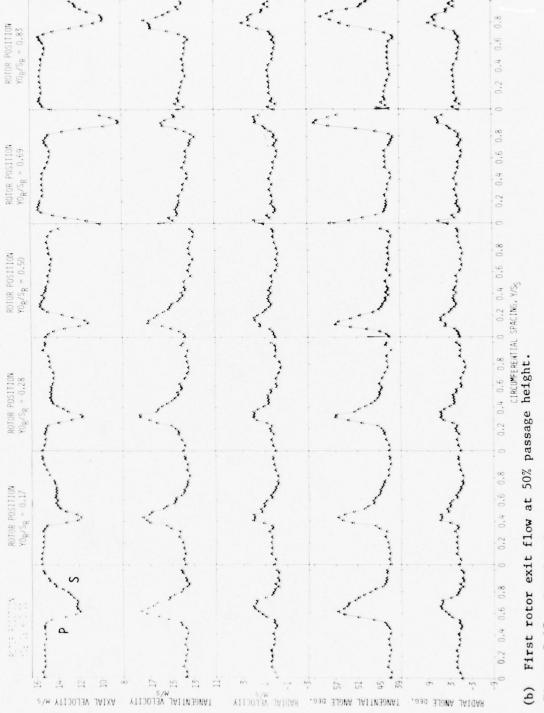
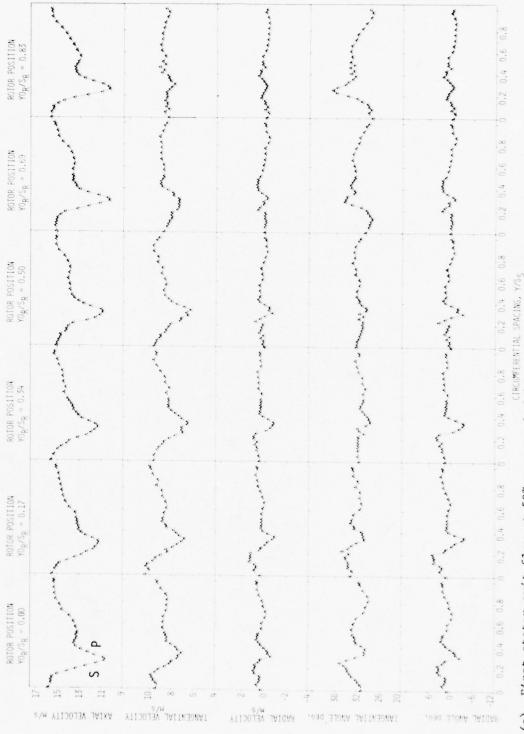
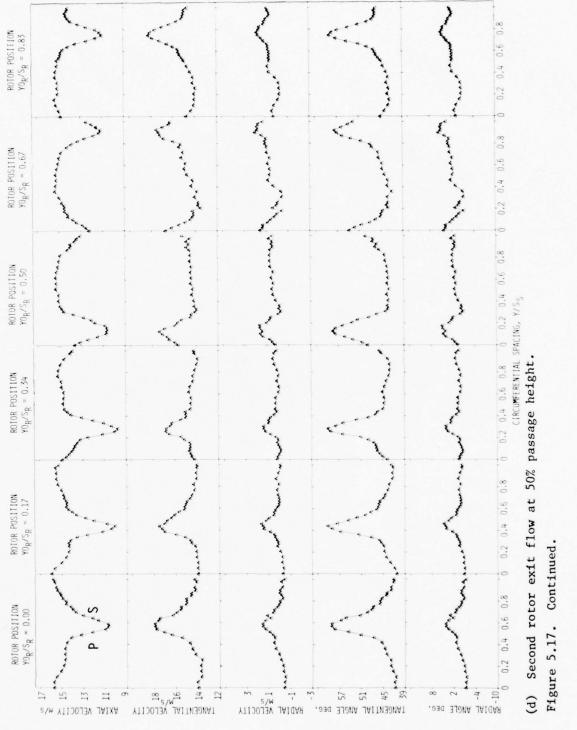
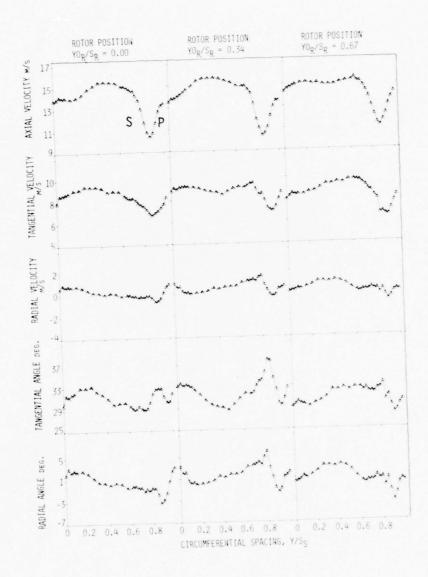


Figure 5.17. Continued.



(c) First stator exit flow at 50% passage height. Figure 5.17. Continued.





(e) Second stator exit flow at 50% passage height.

Figure 5.17. Concluded.

pattern development is expedited through the use of blade-to-blade velocity vector plots. Each velocity vector plot (see Figure 5.18) portrays the blade-to-blade view of the periodic-average flow field for a particular frozen rotor-blade position. Although these fast-response instrument velocity vector plots were constructed similarly to the slowresponse vector plots, it should be noted that each velocity vector measured with the hot wire was drawn with respect to the blade row shown at the locally measured absolute or relative flow angle. Also, although measurements were taken over only one stationary blade pitch spacing, the circumferentially varying flow pattern was periodically repeated over approximately three blade spacings of the blade row shown to enhance visualization. Actually, the velocity profiles should vary slightly from one blade spacing to another due to the difference in the blade pitch values of the rotating and stationary blade rows. The six vector plots for the first rotor at 50% passage height (Figures 5.18a and 5.18b) represent the cyclic flow field variation as the rotor blade sequentially moves over one blade spacing. The flow field at the inlet measurement station to the first rotor was assumed not to vary appreciably, and slowresponse data were used to represent the flow in the vector plots at this location. Due to the deep IGV wakes, the first rotor incidence angle varied by as much as 17 degrees at 50% passage height (see Figure 5.18a). The IGV wake streets have been sketched in Figure 5.18b to help clarify the flow development involved. The locations of these wake streets were based on the corresponding slow-response data. A step-by-step analysis of the rotor flow field as the rotor moves through its cyclic pattern indicates that when the rotor blade trailing edge is within the stationary IGV

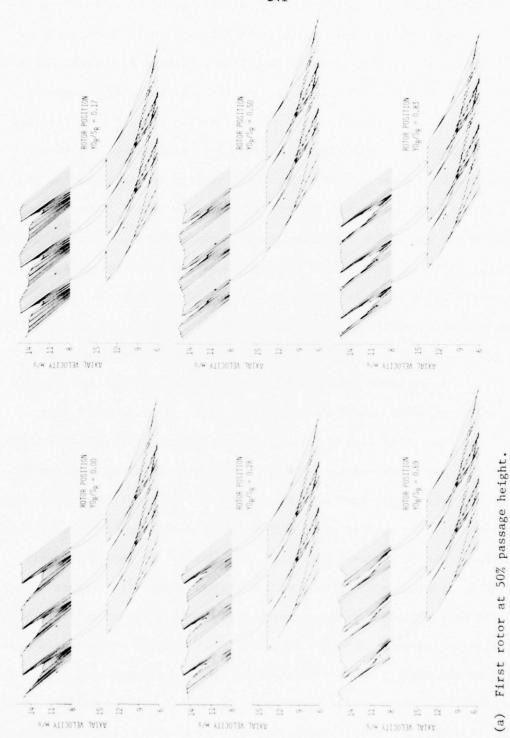
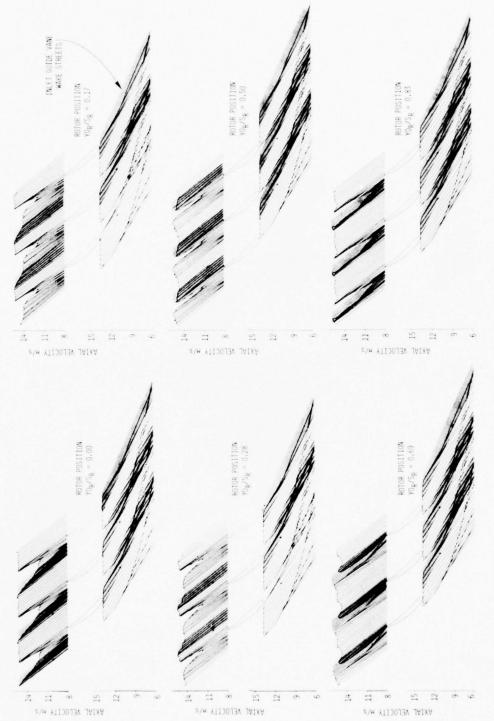
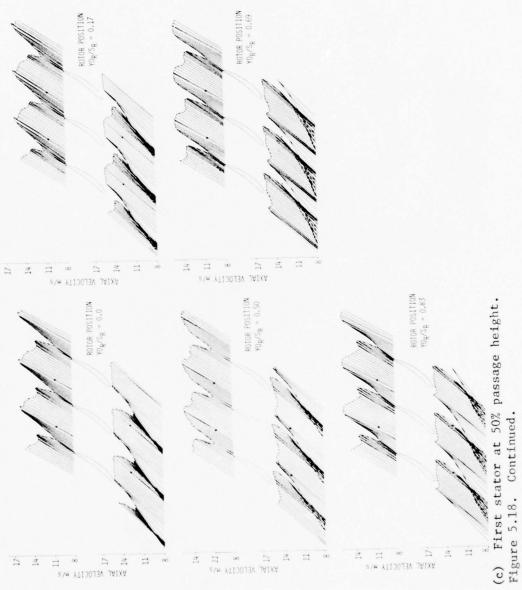
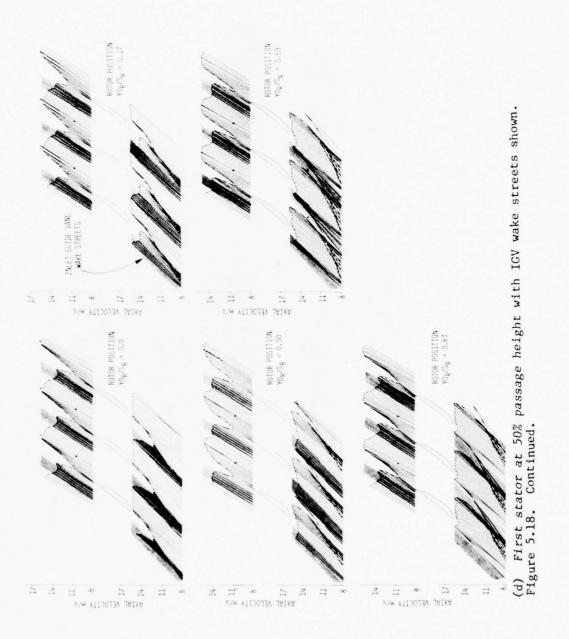


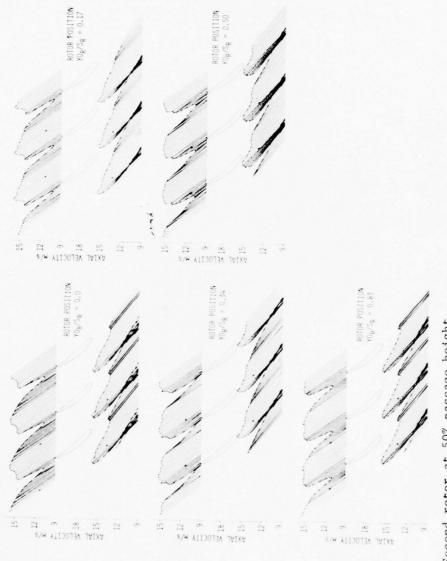
Figure 5.18. Blade-to-blade velocity vector plots obtained at different rotor positions with frozen rotor-blade survey method.



(b) First rotor at 50% passage height with IGV wake streets shown. Figure 5.18. Continued.

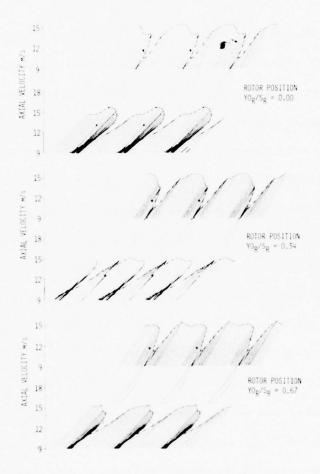






(e) Second rotor at 50% passage height.

Figure 5.18. Continued.



(f) Second stator at 50% passage height.

Figure 5.18. Concluded.

wake street, the depth and width of the rotor wake increases appreciably. Once the rotor trailing edge has passed beyond the stationary IGV wake street, a normal wake pattern is resumed.

First stator blade section discrete frequency noise is related to the surface pressure fluctuations of that blade section produced by the periodic unsteadiness of the first rotor exit flow. Larger variations in first rotor exit (first stator inlet) periodic unsteadiness (larger rotor wakes) probably result in higher stator noise levels. From the measurements at 50% span, it was observed that larger first rotor wakes occurred in the IGV wake street region. If the effect of the IGV wake street on the rotor is similar over the entire span of the first rotor, then the slow-response data (Figures 5.5 and 5.6) seem to indicate that conditions for maximum noise at most first stator blade sections and conditions for minimum noise at most first stator blade sections were present under maximum and minimum operation, respectively. The first stator fast-response vector plot at 50% passage height for minimum sound (Figure 5.18c) conclusively indicates that the rotor wakes flowing onto the leading edge region of the first stator blade section are smallest.

The results of the periodic-average hot-wire measurements behind the first stator at six rotor positions are shown in scalar form in Figure 5.17c. The rotor wake influence on the stator exit flow can be seen in the sequence of axial velocity profiles. Less obvious is the presence of the stationary IGV wake street influence which is more clearly indicated in the slow-response vector plot (see Figure 5.13). The IGV wake streets can be identified in the axial velocity profile for each rotor position near a circumferential spacing of 0.6, and its position is sketched in the

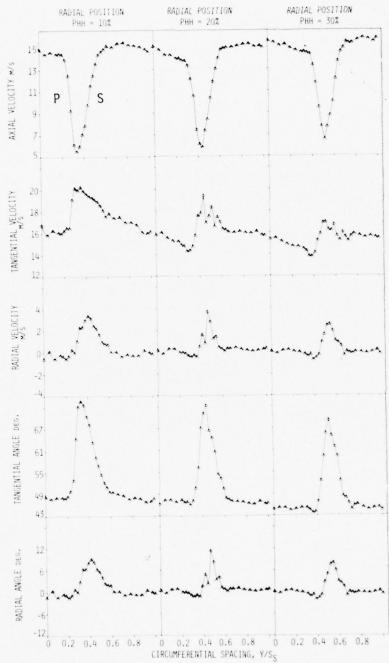
five blade-to-blade vector plots in Figure 5.18d. The absolute tangential velocity and radial velocity blade-to-blade variations are definitely smaller for rotor positions $\mathrm{YO}_R/\mathrm{S}_R=0.69$ and 0.83 (see Figure 5.17c). The tangential angle blade-to-blade differences are notably smaller for rotor positions $\mathrm{YO}_R/\mathrm{S}_R=0.34$ and 0.50. The general expected tendency for the slower moving stator wake fluid to move inward toward the hub is evident. The stator incidence angle varied as much as 20 degrees which is comparable to the range reported by Evans (12) and Hirsch and Kool (20). The velocity vector plots (Figures 5.18c and 5.18d) manifest the wake interaction involved between the IGV, first rotor and first stator. The significant changes in first stator exit flow with frozen rotor position might indicate that second rotor noise due to periodic unsteadiness can be varied with appropriate stator and rotor blade circumferential placement.

Although the second rotor exit flow field changed with rotor position (see Figures 5.17d and 5.18e), the variation was significantly less than that for the first rotor. This observation is consistent with the slow-response data trend indicated in Figure 5.5e and seems reasonable since the second rotor inlet velocity and incidence angle variation at 50% span was less than that for the first rotor. It should be noted that while the first stator wake street is evident, it is less discernible in the second rotor exit flow than that of the IGV wake street in the first rotor exit flow. As expected, centrifugation of the wake fluid is evident in the second rotor exit flow as indicated by the radial angle distributions. In addition, large (20 degrees) circumferential variations in absolute tangential flow angle are apparent at each rotor position while only small circumferential variations in the relative tangential flow angle are

evident in the velocity vector plots. The range of relative tangential flow angles was 33 to 41 degrees. In the case of the first rotor, the range in values of relative tangential flow angle was 32 to 50 degrees. The hot-wire data do not yield conclusive information related to second stator noise.

The second stator exit flow distributions at three rotor positions are shown in Figure 5.17e with the corresponding velocity vector plots in Figure 5.18f. There is a marked contrast in the freestream flow region. In addition, the variation of the absolute tangential angle in the region of the stator wake is significantly larger at the rotor position of 0.34. The rotor wake influence on the stator exit flow is noticeable. The first stator wake street is buried within the second stator wake at 50% span as shown in the slow-response data (Figure 5.5e) and therefore is not apparent in the fast-response data. It appears as if third rotor noise can be varied with appropriate stator and rotor blade circumferential placement. The slow-response data indicate an appreciably larger second stator wake at 90% span for the maximum noise condition than for the minimum noise one.

All hot-wire results thus far discussed were obtained at 50% passage height. Results from hot-wire measurements taken behind the first rotor at nine passage height locations (10% to 90% from the hub) and one rotor position (${\rm YO}_{\rm R}/{\rm S}_{\rm R}$ = 0.0) are presented in Figures 5.19 and 5.20. Slow-response data were again used to represent the first rotor inlet flow in the vector plots. The performance of the first rotor varied with radial position mainly because of the spanwise variation of inlet flow conditions produced by the IGV blade row. The larger variations in the average first



(a) First rotor exit flow at rotor position $\rm YO_R/S_R$ = 0.0 and passage heights 10%, 20%, and 30%.

Figure 5.19. Circumferential distribution of periodic-average flow field parameters obtained at different radial positions with frozen rotor-blade survey method.

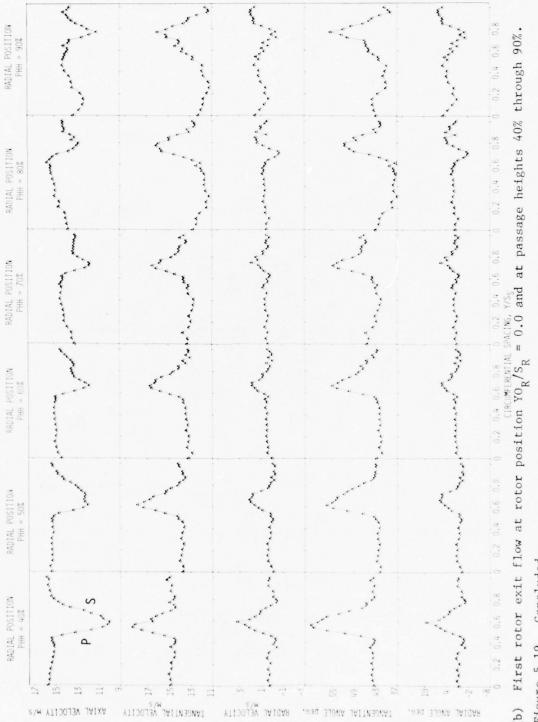
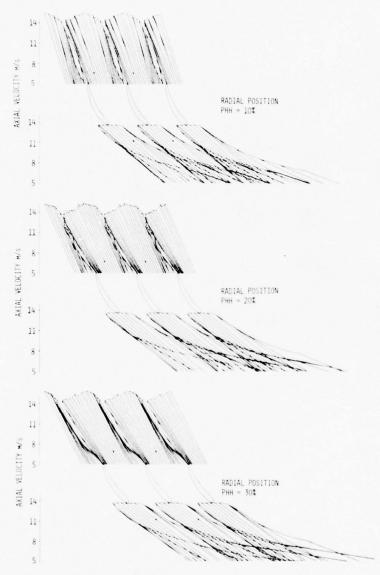
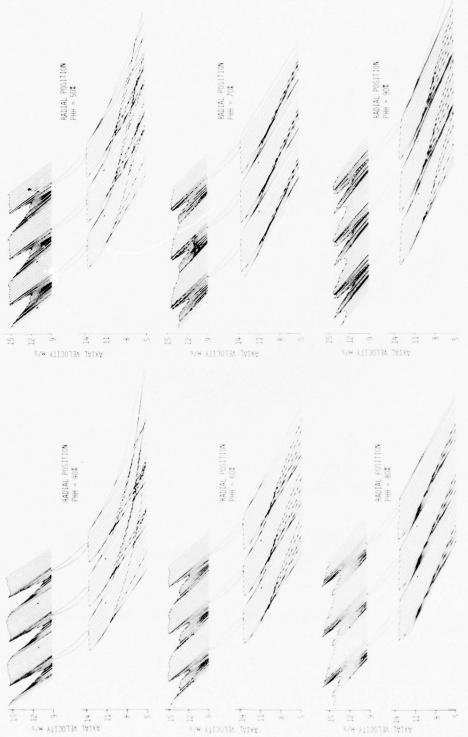


Figure 5.19. Concluded. (P)



(a) First rotor at rotor position YO $_{\rm R}$ /S $_{\rm R}$ = 0.0 and at passage heights 10%, 20%, and 30%.

Figure 5.20. Blade-to-blade velocity vector plots obtained at different radial positions with frozen rotor-blade survey method.



(b) First rotor at rotor position $\text{YO}_{R}/S_{R} = 0.0$ and at passage heights 40% through 90%. Figure 5.20. Concluded.

rotor exit flow field (slow response) and the periodically frozen first rotor-blade exit flow field at different frozen rotor positions (fast response) were related to the larger variation of IGV row exit (first rotor inlet) flow and occurred in the lower half of the annulus. For example, the variation in rotor exit (stator inlet) absolute tangential flow angle was as much as 27 degrees at 10, 20, and 30% of the passage height from the hub. The IGV wake street influence can be observed at each spanwise location. Near the tip (80 and 90% of the span from the hub) appreciable amounts of wake fluid appear to be moving toward the hub.

VI. CONCLUSIONS

Summarized below are the conclusions reached to date. Further data analysis and acquisition are being continued at Iowa State under AFOSR sponsorship.

The level of discrete frequency noise at the inlet of the ISU research compressor could be varied appreciably by relative circumferential positioning of the stationary blade rows when the spinning blade-row interaction pattern speed was above the Tyler and Sofrin (15) "cut-off" value. The details of the fluid flow physics associated with this variation in noise with blade row circumferential positioning are not entirely explainable yet because of insufficient evidence. However, the present detailed flow field data may be interpreted as showing that the pressure fluctuations incurred by the first stator due to wake interaction with the first rotor were generally smaller during minimum noise operation, and generally larger during maximum noise operation. Also, the data suggest that the second and third rotor noise levels might be affected more by stationary blade-row placement than the noise level of the second stator. More specific conclusions about the compressor flow field behavior based on slow- and fast-response instrument data are discussed below.

The stationary flow pattern within the compressor could be changed appreciably in regions of the compressor annulus by varying the circumferential positions of the stationary blade rows relative to each other. Stationary blade row wakes significantly affected the shape of the flow fields of the next rotor and stator rows. Further, the interaction flow pattern formed by two stationary blade rows subsequently influenced the next rotor and stator flow fields. The measured rotor and stator exit

flow fields were found to be periodically and randomly unsteady and dependent on instantaneous rotor blade circumferential position with the extent of variation of exit flow dependent on the intensity of the inlet flow periodic variation. For example, the data indicated that first rotor exit flow periodic and random unsteadiness was greatest in the IGV row wake street region. Because the flow was unsteady in both the absolute and relative reference frames due to the interaction between the rotating and stationary blade rows, the velocity field sensed by a stationary hotwire behind a rotor blade periodically sampled at different circumferential positions was found to vary from the field sensed by a hot wire traversed circumferentially relative to a rotor blade section periodically frozen at the same circumferential position. The latter method appears to provide more detail and to be a more viable means for measuring unsteady flow phenomena. The amount of influence and location of wake streets varied over the annulus span. In general, the three-dimensional stationary wake streets approached a stator leading edge at an angle relative to the radial direction with two adjacent wake streets intersecting the stator leading edge over the annulus height. Hub to tip distributions of circumferentially averaged (meridional plane) quantities indicated some variation of blade section loss coefficient, head-rise coefficient, hydraulic efficiency, and incidence and deviation angles for a few blade sections with change in stationary blade row placement. However, no difference of overall head-rise coefficient or hydraulic efficiency could be detected between the maximum and minimum noise operation conditions.

It is true that the large variation in ISU research compressor inlet noise with appropriate blade row positioning was possible mainly because the same number of blades was used in each stationary row, and the number of blades in each row allowed the pressure interaction patterns to move forward. However, what is observed about the noise (surface pressure fluctuations) of all the blades in a particular row of the ISU research compressor is probably generally applicable to fewer blades (maybe only one) in a more typical turbomachine. In the latter case reduction of periodic blade lift force variation rather than noise would be important, and the present results may be used to learn more about how the fluctuating lift force pattern for any blade in a practical multistage axial-flow turbomachine depends on factors which include the location of that blade relative to upstream blades and/or other flow distorters in that machine.

VII. RECOMMENDATIONS FOR FUTURE RESEARCH

This research program has established the foundation of a long range program at Iowa State University with the following general technical objectives:

- 1. To develop a better understanding of the fluid flow physics related to multistage, axial-flow turbomachines. In particular, the details of the production, transport, and interaction of rotor and stator wakes including the effects of main and secondary flows and boundary layers on these wakes will be examined and modeled.
- To assess the influence of circumferential positioning of the rows of blades in a multistage, axial-flow turbomachine on the aerodynamic performance, acoustic characteristics and aeromechanical interactions involved.
- 3. To improve turbomachine fluid flow measuring techniques and equipment.
- 4. To incorporate research results of the above mentioned objectives into turbomachine design procedures.

Several specific suggestions for the continuation of research in this area follow.

Further detailed flow field measurements utilizing the hot-wire anemometry measurement technique developed during the present investigation should be made ahead of and behind each blade row of the research compressor. In order to complement the data already acquired, periodicaverage circumferential survey data should be obtained at the same

compressor operating condition at spanwise increments of 10% from hub to tip for several periodic frozen rotor positions. The use of both frozen rotor-blade and passing rotor-blade flow field survey methods should be considered. After a complete set of data has been obtained at the minimum noise condition, further data at the maximum noise condition would be useful for assessing the influence of circumferential positioning of the blade rows.

Continual development in data presentation technique would facilitate data interpretation. Although the velocity vector graph technique is an effective blade-to-blade plane flow visualization technique, three-dimensional display methods similar to those used by Hirsch and Kool (20) and Whitfield, Kelly and Barry (18) should be considered. In addition, the movie sequence approach of Peacock and Overli (34) appears to be an excellent technique for visualizing unsteady rotor and stator wake behavior.

In order to supplement the cobra probe and hot-wire anemometer data, instantaneous and periodic-average total-pressure data obtained with a fast-response total-pressure probe could be used to determine the unsteady loss and static pressure distribution.

The feasibility of determining a minimum noise rotor-row circumferential placement schedule should be considered based on the data related to minimum and maximum noise stationary blade row circumferential placement.

Once a sufficient amount of data has been obtained at the one compressor operating condition, further data at other operating conditions such as near stall or stall would be of value. The following modifications and additions to the research compressor and related instrumentation would enhance the research capabilities of the facility:

The present scope of the three-dimensional hot-wire anemometer technique should be further developed so that random unsteadiness levels and spectra within the research compressor flow field can be measured.

The probe measurement stations between the blade rows should be modified to allow axial development surveys. This would make possible the study of the development of the flow between the blade rows in the flow direction and permit the individual effects of potential flow and viscous wake interaction to be appreciated.

The mounting of miniature, fast-response, surface pressure transducers on the stator and rotor blade surfaces would allow the acquisition of blade surface fluctuation data (random and periodic) and provide valuable information about the flow within the blade rows.

Finally, in order to further study the compressor blade vibration characteristics, strain gages should be mounted on the rotor blades and measurements made to supplement stator blade strain-gage data.

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SYMBOLS AND NOTATION

A	compressor flow passage annulus area, m ²
Ā	unit vector along hot-wire sensor axis (Fig. 4.8)
b ₀ , b ₁ , b	effective cooling velocity/actual velocity ratio correlation coefficients
c	blade chord length (Fig. 3.3), m
E _l	linearized anemometer bridge voltage, volts
FRC	comparison of integrated and venturi volume flow rates (Eq. 12.46), percent
g	local acceleration of gravity, m/s^2
g _c	gravitational constant, 1.0 kgm/Ns ²
Н	total head with respect to barometric pressure (Eq. 12.6), Nm/kg
h	static head with respect to barometric pressure, Nm/kg
h _{hg}	barometric pressure, m of Hg
í	incidence angle (Fig. 12.1; Eqs. 12.24, 12.26, and 12.28), deg
m	constant hot-wire probe turning measurement angle increment (Fig. 4.10), deg
MP	mechanical shaft power (Eq. 12.47), watt
N	number of samples per periodic average
n	random component of hot-wire signal
p	periodic component of hot-wire signal
P ₁	cobra probe indicated total pressure with respect to barometric pressure, \boldsymbol{m} of water
P_2	cobra probe side-tube pressure with respect to barometric pressure, m of water
P ₃	cobra probe side-tube pressure with respect to barometric pressure, m of water

Patm	barometric pressure (Eq. 12.1), N/m ²
P _s	static pressure with respect to barometric pressure, m of water
Pt	total pressure with respect to barometric pressure, m of water
P _w	annulus-outer surface static wall pressure with respect to barometric pressure, \boldsymbol{m} of water
РНН	percent passage height from hub (Eq. 12.4), percent
$Q_{\mathbf{a}}$	integrated volume flow rate at probe-traversing measurement stations (Eq. 12.44), $\rm m^3/\rm s$
$Q_{\mathbf{v}}$	venturi volume flow rate (Eq. 12.42), m^3/s
R	gas constant, Nm/kg°K
r	radius from compressor axis, m
R _{cb}	cable resistance, ohms
Roh	hot-wire sensor resistance overheat ratio
R _{ph}	probe holder resistance, ohms
R _{p1}	probe lead resistance, ohms
R _{s,c,d}	cold resistance read off anemometer resistance deck, ohms
Rs,op,d	sensor operating resistance anemometer deck setting (Eq. 4.28), ohms
RPM	rotor rotational speed, rpm
R,Y,Z	compressor coordinate system (Fig. 4.12)
S	circumferential space between blades, blade pitch (Fig. 3.3), $\ensuremath{\text{m}}$ or deg
S	general hot-wire signal composed of periodic and random components
SPL	sound-pressure level, decibels
T	period of periodic component of hot-wire signal corresponding to rotor blade passing period, sec
t	time, s; temperature, °K

tbaro	barometer ambient temperature, °K
t	blade section maximum thickness/chord ratio (Fig. 3.3)
U	rotor blade velocity (Eq. 12.14), m/s
V	absolute velocity (Figs. 4.12 or 12.1; Eq. 12.12), m/s
v'	relative velocity (Eqs. 12.21 or 12.59), m/s
v_e	hot-wire effective cooling velocity (Eq. 4.13), m/s
v _r	radial component of fluid velocity (Fig. 4.12; Eq. 12.57), m/s
v _y	tangential component of absolute fluid velocity (Figs. 4.12 or 12.1; Eqs. 12.17 or 12.56), m/s
v'y	tangential component of relative fluid velocity (Eqs. 12.19 or 12.58), $\ensuremath{\text{m/s}}$
v _z	axial component of fluid velocity (Figs. 4.12 or 12.1; Eqs. 12.15 or 12.55), m/s
x,y,z	hot-wire probe coordinates fixed to probe (Fig. 4.8)
Y	circumferential traversing position, degree
Υ0	circumferential blade-row setting position when Y is equal to zero, circumferential distance from probe-traversing measurement stations to blade stacking axis, positive in direction of rotor rotation, degree
WT	torque meter dead weight, kg
α	sensor yaw angle, angle between velocity vector and hot-wire sensor axis (Fig. 4.8; Eq. 4.12), degree
β_{mv}	approximate tangential flow angle (Fig. 4.10), degree
βr	radial flow angle (Fig. 4.12; Eq. 4.29), degree
βy	absolute tangential flow angle with respect to axial direction (Figs. 4.12 or 12.1; Eqs. 12.8, 12.9 or 12.53), degree
β'y	relative tangential flow angle with respect to axial direction (Eqs. 12.23 or 12.60), degree
Υ	blade stagger angle (Fig. 3.3; Table 3.1), degree

$\gamma_{\rm H_2O}$	specific weight of water manometer fluid (Eq. 12.3), N/m^3
γ _{hg}	specific weight of mercury, N/m ³
ΔP_n	differential pressure between calibration nozzle plenum pressure and atmospheric pressure, m of water
$^{\Delta P}$ vent	differential pressure across venturi, m of water
δ	deviation angle (Fig. 12.1; Eqs. 12.25, 12.27, and 12.29), degree
n	hydraulic efficiency (Eqs. 12.37, 12.38, and 12.39)
θ ₀	hot-wire sensor angle with respect to a plane normal to the probe axis (Fig. 4.8), degree
^θ off	measurement off-set angle (Fig. 4.10), degree
$\theta_{\mathbf{p}}$	probe pitch angle (Figs. 4.2 or 4.8), degree
$\theta_{\mathbf{y}}$	probe yaw angle (Figs. 4.2 or 4.8), degree
к	blade angle, angle between tangent to blade camber line and axial direction (Fig. 3.3; Table 3.1), degree
р	density of air (Eq. 12.2), kg/m^3
σ	standard deviation of periodic-sample averages, m/s
$\sigma_{\mathbf{n}}$	standard deviation of random velocity fluctuation, m/s
ф	flow coefficient (Eq. 12.30)
^ф а	integrated flow coefficient at probe-traversing measurement stations (Eq. 12.45)
φ _v	venturi flow coefficient (Eq. 12.43)
Ψ	head-rise coefficient (Eqs. 12.31 through 12.36)
ω	total-head loss coefficient (Eqs. 12.40 and 12.41)
	Additional General Subscripts
a	hot-wire probe measurement position a
ь	hot-wire probe measurement position b

hot-wire probe measurement position c

h	annulus inner surface, hub
i	ideal
IGV	inlet guide vane
me	mechanical
overall	overall compressor
R	rotor
S	stator
stage	stage
t	annulus outer surface, tip
1	blade-row inlet
2	blade-row outlet
1R	first rotor
2R	second rotor
3R	third rotor
18	first stator
28	second stator

third stator

3S

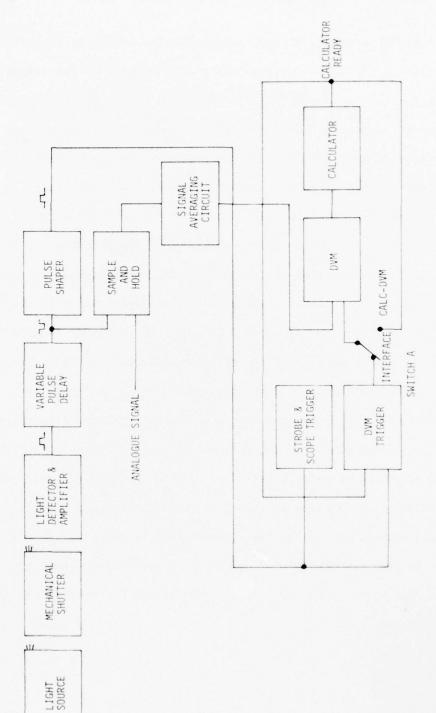
Superscripts

→	vector
•	relative to rotor
-	average; blade-to-blade circumferential average valu
~	periodically sampled and averaged

mass-averaged in the radial direction

X. APPENDIX A: PERIODIC-SAMPLING CIRCUIT DESIGN

The periodic-sampling circuit design details including a general block diagram of the logic involved, a circuit diagram of the triggering and sample-and-hold components, and a sketch of the interfacing cable connections are presented in Figures 10.1 through 10.4. The general scheme of circuit operation can be inferred from the block diagram in Figure 10.1. The circuit can be used in two modes of operation. In both cases, a 5 µsec sample of the input analog signal is obtained each time an electric pulse is received from the photoelectric triggering circuit. Switch "A" controls the manner in which the digital voltmeter and calculator interact with the triggering and sample-and-hold circuits. With the switch thrown to "CALC-DVM," the digital voltmeter is read by the calculator independently of the triggering circuit at the moment specified by the calculator. With switch "A" thrown to "interface," the digital voltmeter and calculator are synchronized with the triggering of the sample-and-hold circuit. If the signal averaging circuit is removed, and if the sampling circuit is used in the mode "A," the periodic samples can be individually retained in the calculator memory, and average and RMS values can be calculated. For this investigation, however, the signal averaging circuit was always used, and only the periodic-average signal was obtained. The fluctuating component of the signal was lost in the averaging process.



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Figure 10.1. Block diagram of periodic-sampling circuit.

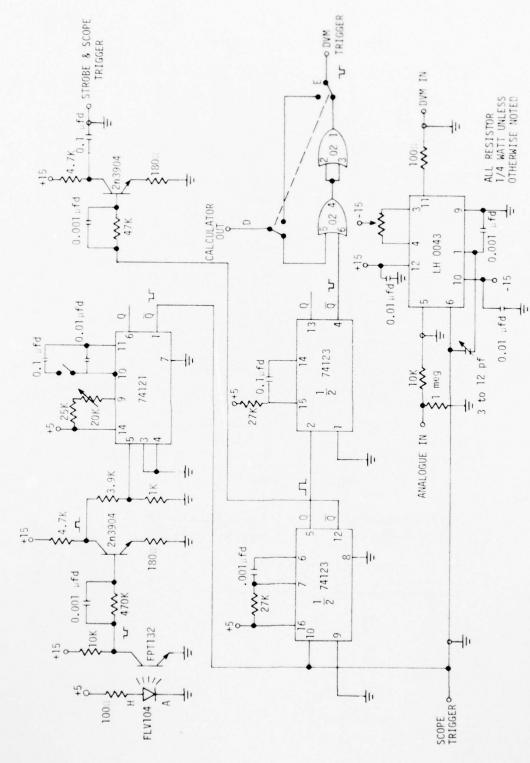


Figure 10.2. Circuit diagram of triggering and sample-and-hold circuits.

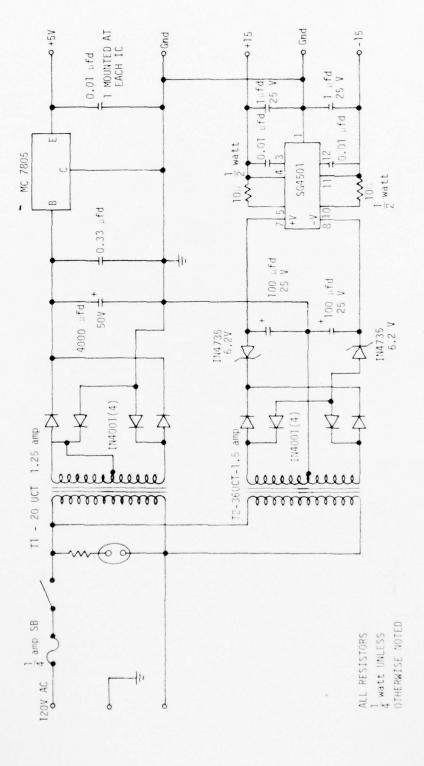


Figure 10.3. Power supply for triggering and sample-and-hold circuits.

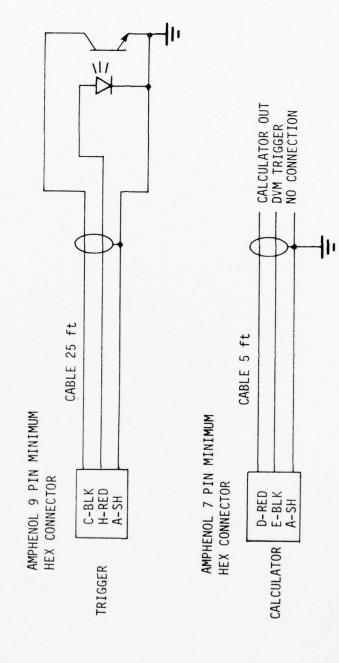


Figure 10.4. Interfacing cable connections.

XI. APPENDIX B: CALCULATOR PROGRAMS AND DATA STORAGE

The data acquisition and reduction calculator programs used in this investigation are listed in this section. These programs and all experimental data are stored on magnetic cassette tapes and are indexed according to cassette and file numbers as specified below. Due to a limitation of available calculator memory space, it was necessary in many cases to subdivide the larger programs and individually store the program parts in separate magnetic tape files.

- Flow coefficient program Calculation of compressor overall flow coefficient from flow rate venturi meter data; cassette 4C, file 16.
- Actuator position correlation program

 Linear least squares

 correlation between actuator potentiometer voltage readout and
 actuator motion for probe and circumferential positioning
 actuators; cassette 4C, file 3.
- Slow-response probe survey acquisition program Acquisition of slow-response total-pressure and flow-angle circumferential probe survey data; cassette 4C, file 4.
- Wall static pressure acquisition program Acquisition of outer annulus surface static pressure circumferential survey data; cassette 4C, file 76.
- Slow-response data reduction program
 response data to obtain point flow-field parameters, average
 flow-field parameters, and rotor, stator, and stage performance parameters; cassette 4C, files 0-2, 5-15, 18-75.
- Slow-response data for minimum sound Storage of circumferential survey data including probe data, outer annulus surface static-pressure data, and station 8 hub surface static-pressure data; cassette 6, files 1-79, 97-105.
- Slow-response data for maximum sound

 Storage of circumferential survey data including probe data and outer annulus surface static-pressure data; cassette 7, files 1-79, 97-104.

- Hot-wire effective cooling velocity/actual velocity ratio calibration program

 Calibration of hot wire with respect to sensor yaw angle, pitch angle and velocity for the determination of the ten coefficients in Equation 4.16; consists of two parts: (1) calibration data acquisition and (2) least squares calibration data correlation; cassette 8A, file 8, 9, 11-13; cassette 8B, file 8, 9, 11-13.
- Hot-wire linearizer velocity calibration program Velocity calibration to determine the four polynomial coefficients required by the anemometer linearizer through a least squares correlation of calibration data; cassette 11A, files 2-4; cassette 11B, files 2-4.
- Hot-wire second order velocity calibration program Velocity calibration to determine the three coefficients in the second order velocity calibration Equation 4.13 through a least squares correlation of calibration data; cassette IIA, file 5; cassette IIB, file 5.
- Fast-response hot-wire data acquisition program Acquisition of hot-wire, periodic-average, three-dimensional, circumferential survey data; cassette 11A, files 5-7; cassette 11B, file 5-7.
- Fast-response hot-wire data reduction program Reduction of fast-response hot-wire data to obtain three-dimensional point flow-field parameters and circumferential blade-to-blade average flow-field parameters; cassette 11A, files 8-18; cassette 11B, files 8-18.
- Fast-response hot-wire data Storage of periodic-average hot-wire data obtained with the single inclined hot-wire sensor in the research compressor; cassette 11A, files 30-52; cassette 11B, files 30-38.

XII. APPENDIX C: PARAMETER EQUATIONS

The equations used in calculating the slow-response and fast-response parameters are presented. The symbols used in the equations are defined in the symbols and notation section and the sign conventions are generally shown in Figures 4.12 and 12.1 for the fast-response and slow-response parameters, respectively. For the fast-response parameters, the sign conventions for the relative velocity, relative tangential velocity, and relative tangential flow angle are similar to those of the slow-response parameters. Parameters averaged circumferentially or radially were obtained using a spline-fit integration technique (Ref. 30).

A. General Parameters

1. Basic fluid properties

Barometric pressure, N/m²:

$$P_{atm} = h_{hg@t_{baro}} (1.0-0.00018 (t_{baro}^{-273.15})) \gamma_{hg@273°K}$$
 (12.1)

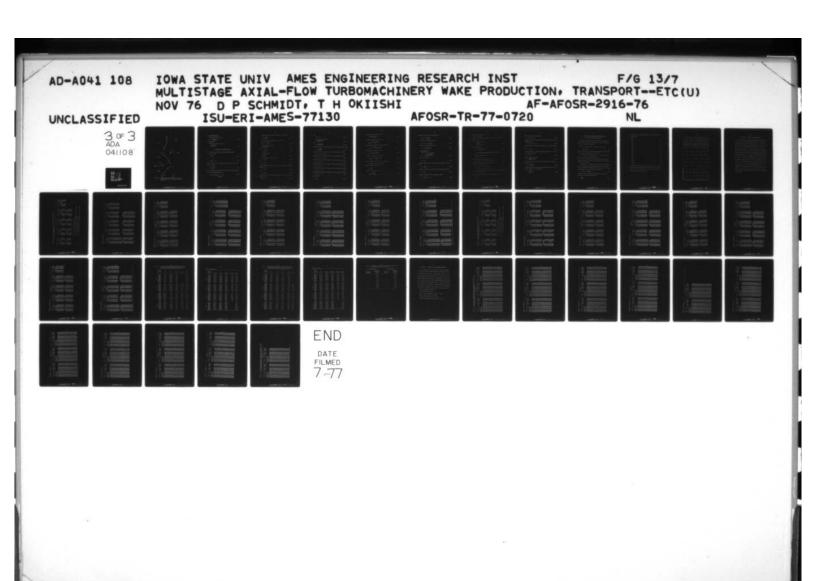
Density of air, kg/m3:

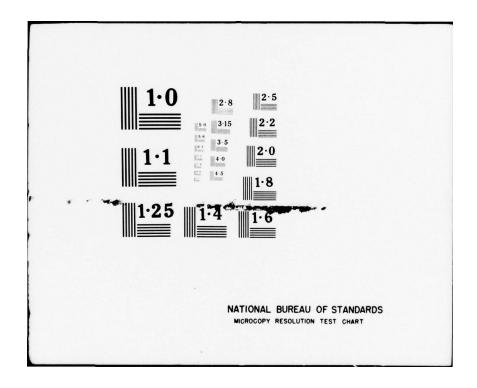
$$\rho = \frac{P_{atm}}{R t}$$
 (12.2)

Specific weight of water, N/m3:

$$\gamma_{\text{H}_2\text{O}} = \frac{g}{g_c} \left(996.86224 + 0.1768124 \left(\frac{9}{5} \text{ t} - 459.67 \right) - 2.64966 \times 10^{-3} \right)$$

$$\left(\frac{9}{5} \text{ t} - 459.67 \right)^2 + 5.00063 \times 10^{-6} \left(\frac{9}{5} \text{ t} - 459.67 \right)^3 \right)$$
(12.3)





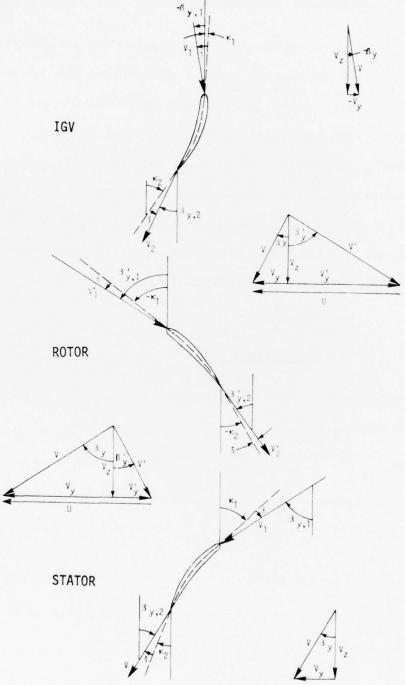


Figure 12.1. Sketch showing nomenclature, sign convention, and velocity triangles for slow-response instrument parameters.

2. Blade-element quantity

Percent passage height from hub:

$$PHH = \left(\frac{r - 0.14224}{0.06096}\right) \times 100$$
 (12.4)

3. Miscellaneous

Calibration nozzle jet velocity, m/s

$$V = \sqrt{\frac{2g_c \gamma_{H20} \Delta P_n}{\rho}}$$
 (12.5)

B. Slow-Response Instrument Parameters

1. Point and circumferential-average blade-element quantities

Total head, Nm/kg:

$$H = \frac{P_t \gamma_{H2O}}{\rho} \tag{12.6}$$

and

$$\overline{H} = \frac{1}{S_S} \int_0^{S_S} H dY$$
 (12.7)

Absolute tangential flow angle behind rotors (see Figure 12.1 for sign convention), degrees:

$$\overline{\beta_{\mathbf{y}}} = \frac{1}{S_{\mathbf{S}}} \int_{0}^{S_{\mathbf{S}}} \beta_{\mathbf{y}} d\mathbf{Y}$$
 (12.8)

Absolute tangential flow angle behind stationary blade rows (see Figure 12.1 for sign convention), degrees:

$$\overline{\beta}_{y} = \frac{1}{Y_{\text{freestream}}} \int_{\substack{\text{across} \\ \text{freestream}}} \beta_{y} dY$$
(12.9)

the state of the s

Annulus outer surface static wall pressure, meters of water:

$$\overline{P}_{w} = \frac{1}{S_{S}} \int_{0}^{S_{S}} P_{w} dY \qquad (12.10)$$

Static head (radial equilibrium equation), Nm/kg:

$$\frac{d\overline{h}}{dr} = \frac{2 \sin^2 \overline{\beta}_y (\overline{H} - \overline{h})}{r}$$
 (12.11)

Absolute fluid velocity, m/s:

$$V = \sqrt{2 g_c(H - \overline{h})}$$
 (12.12)

and

$$\overline{V} = \frac{1}{S_S} \int_0^{S_S} V \, dY \tag{12.13}$$

Blade velocity, m/s:

$$U = \frac{\mathbf{r}\pi RPM}{30.0} \tag{12.14}$$

Axial component of fluid velocity, m/s:

$$V_z = V\cos \overline{\beta}_y$$
 (12.15)

and

$$\overline{V}_z = \overline{V} \cos \overline{\beta}_y$$
 (12.16)

Tangential component of absolute fluid velocity (see Figure 12.1 for sign convention), m/s:

$$V_y = V \sin \overline{\beta}_y$$
 (12.17)

and

$$\overline{V}_{y} = \overline{V}\sin \overline{\beta}_{y}$$
 (12.18)

Tangential component of relative fluid velocity (see Figure 12.1 for sign convention), m/s:

$$V_{\mathbf{y}}^{\bullet} = \mathbf{U} - V_{\mathbf{y}} \tag{12.19}$$

and

$$\overline{V}_{y}' = U - \overline{V}_{y}$$
 (12.20)

Relative fluid velocity, m/s:

$$V' = \sqrt{(V'_{V})^2 + (V_{Z})^2}$$
 (12.21)

and

$$\overline{V}' = \sqrt{(\overline{V}'_{\underline{V}})^2 + (\overline{V}_{\underline{Z}})^2}$$
 (12.22)

Relative tangential flow angle (see Figure 12.1 for sign convention), degrees:

$$\overline{\beta}_{y}' = \sin^{-1}\left(\frac{\overline{V}_{y}'}{\overline{V}'}\right) \tag{12.23}$$

Incidence angle for IGV (see Figure 12.1 for sign convention), degrees:

$$\overline{i}_{IGV} = \kappa_{1, IGV} - \overline{\beta}_{v, 1, IGV} \tag{12.24}$$

Deviation angle for IGV (see Figure 12.1 for sign convention), degrees:

$$\overline{\delta}_{IGV} = \kappa_{2,IGV} - \overline{\beta}_{y,2,IGV}$$
 (12.25)

Incidence angle for rotors (see Figure 12.1 for sign convention), degrees:

$$\overline{i}_{R} = \kappa_{1,R} + \overline{\beta}_{V,1,R}^{\dagger}$$
(12.26)

Deviation angle for rotors (see Figure 12.1 for sign convention), degrees:

$$\overline{\delta}_{R} = \kappa_{2,R} + \overline{\beta}'_{v,2,R} \tag{12.27}$$

Incidence angle for stators (see Figure 12.1 for sign convention), degrees:

$$\overline{i}_{S} = \overline{\beta}_{y,1,S} - \kappa_{1,S}$$
 (12.28)

Deviation angle for stators (see Figure 12.1 for sign convention), degrees:

$$\overline{\delta}_{S} = \overline{\beta}_{y,2,S} - \kappa_{2,S} \tag{12.29}$$

Flow coefficient:

$$\overline{\phi} = \frac{\overline{V}_z}{U_L} \tag{12.30}$$

Actual head-rise coefficient for rotor:

$$\Psi_{R} = \frac{g_{c}(\overline{H}_{2,R} - \overline{H}_{1,R})}{U_{t}^{2}}$$
(12.31)

Actual head-rise coefficient for stage:

$$\Psi_{\text{stage}} = \frac{g_c(\overline{H}_{2,S} - \overline{H}_{1,R})}{U_t^2}$$
 (12.32)

Actual head-rise coefficient for overall compressor:

$$\Psi_{\text{overall}} = \frac{g_{c}(\overline{H}_{2,3S} - \overline{H}_{1,IGV})}{U_{t}^{2}}$$
(12.33)

/ Ideal head-rise coefficient for rotor:

$$\Psi_{i,R} = \frac{U(\overline{V}_{y,2,R} - \overline{V}_{y,1,R})}{U_{+}^{2}}$$
 (12.34)

Ideal head-rise coefficient for stage:

$$\Psi_{i,stage} = \frac{U(\overline{V}_{y,1,S} - \overline{V}_{y,1,R})}{U_t^2}$$
 (12.35)

Ideal head-rise coefficient for overall compressor:

$$\Psi_{i,\text{overall}} = \Psi_{i,1R} + \Psi_{i,2R} + \Psi_{i,3R}$$
 (12.36)

Hydraulic efficiency for rotor:

$$\eta_{R} = \frac{\Psi_{R}}{\Psi_{i,R}} \tag{12.37}$$

Hydraulic efficiency for stage:

$$\eta_{\text{stage}} = \frac{\Psi_{\text{stage}}}{\Psi_{\text{i,stage}}}$$
 (12.38)

Hydraulic efficiency for overall compressor:

$$\eta_{\text{overall}} = \frac{\Psi_{\text{overall}}}{\Psi_{\text{i,overall}}}$$
 (12.39)

Total-head loss coefficient for rotor:

$$\omega_{R} = 2(\Psi_{1,R} - \Psi_{R}) \frac{U_{t}^{2}}{(V_{1,R}^{\prime})^{2}}$$
(12.40)

Total-head-loss coefficient for stator:

$$\omega_{S} = -2g_{c} \frac{(\overline{H}_{2,S} - \overline{H}_{1,S})}{(\overline{V}_{1,S})^{2}}$$
(12.41)

2. Global parameters

Venturi volume flow rate, m³/s:

$$Q_{v} = 0.05229 \sqrt{\frac{2g_{c}\gamma_{H_{2}0}^{\Delta P} \text{vent}}{\rho}}$$
 (12.42)

Venturi flow coefficient:

$$\phi_{\mathbf{v}} = \frac{Q_{\mathbf{v}}}{A U_{\mathbf{t}}} \tag{12.43}$$

Integrated volume flow rate at probe-traversing measurement stations,

 m^3/s :

$$Q_a = 2\pi \int_{r_h}^{r_t} \overline{V}_z r dr \qquad (12.44)$$

Integrated flow coefficient at probe-traversing measurement stations:

$$\phi_{\mathbf{a}} = \frac{Q_{\mathbf{a}}}{A U_{\mathbf{t}}} \tag{12.45}$$

Integrated and venturi flow-rate comparison, percent:

$$FRC = \frac{Q_a - Q_v}{Q_v} \times 100$$
 (12.46)

Mechanical shaft power, watts:

$$MP = 0.2589 \text{ WT} \cdot \text{RPM}$$
 (12.47)

General radial mass-average parameter equation (let ξ be any general

parameter): $\frac{\dot{\xi}}{\xi} = \frac{\int_{0.148}^{0.197} \xi \, \overline{V}_{z,2} \, r \, dr}{\int_{0.148}^{0.197} \overline{V}_{z,2} \, r \, dr}$ (12.48)

Mechanical efficiency:

$$\eta_{\text{me}} = \frac{\rho \left(\overline{H}_{2,3S} - \overline{H}_{1,1GV} \right) Q_{\text{v}}}{MP}$$
 (12.49)

C. Three-Dimensional Fast-Response Hot-Wire Parameters

Effective cooling velocity, m/s:

$$V_{p} = K_{1} + K_{2}E_{\ell} K_{3}E_{\ell}^{2}$$
 (12.50)

Sensor yaw angle relationship (see Figure 4.12):

$$\cos \alpha = \cos \theta_0 \cos \theta_p \cos \theta_y + \sin \theta_0 \sin \theta_p$$
 (12.51)

Effective cooling velocity/actual velocity ratio:

$$\frac{v_e}{v} = b_0 + b_1 \alpha + b_2 \theta_p + b_3 v + b_4 \alpha^2$$

$$b_5 \theta_p^2 + b_6 v^2 + b_7 \alpha \theta_p + b_8 \alpha v + b_9 \theta_p v \qquad (12.52)$$

Absolute tangential flow angle (see Figure 4.12 for sign convention), degrees:

$$\beta_{y} = \beta_{mv} + \theta_{a,off} + \theta_{y}$$
 (12.53)

Radial flow angle (see Figure 4.12 for sign convention), degrees:

$$\beta_{r} = -\theta_{p} \tag{12.54}$$

Axial component of fluid velocity, m/s:

$$V_{z} = V \cos \beta_{r} \cos \beta_{y}$$
 (12.55)

Tangential component of absolute fluid velocity (see Figure 4.12 for sign convention), m/s:

$$V_{y} = V \cos \beta_{r} \sin \beta_{y}$$
 (12.56)

Radial component of fluid velocity (see Figure 4.12 for sign convention), m/s:

$$V_{r} = V \sin \beta_{r} \tag{12.57}$$

Tangential component of relative fluid velocity (similar to sign convention in Figure 12.1), m/s:

$$V_{y}' = U - V_{y}$$
 (12.58)

Relative fluid velocity, m/s:

$$V' = \sqrt{(V_V')^2 + (V_Z)^2}$$
 (12.59)

Relative tangential flow angle (similar to sign convention in Figure

12.1), degrees:

$$\beta_{y}' = \sin^{-1} \left(\frac{V'}{y} \right)$$
(12.60)

General blade-to-blade circumferential integrated average (let ξ be any general parameter) for a blade element:

$$\bar{\xi} = \frac{1}{S_S} \int_0^{S_S} \xi \, dY$$
 (12.61)

XIII. APPENDIX D: LEAST SQUARES EMPIRICAL CORRELATION FOR EFFECTIVE COOLING VELOCITY RATIO

The effective cooling velocity to actual velocity ratio, V_e/V , as a function of sensor yaw angle α , pitch angle θ_p , and velocity V, was predicted with the empirical relationship

$$\frac{V_{e}}{V} = b_{0} + b_{1}\alpha + b_{2}\theta_{p} + b_{3}V + b_{4}\alpha^{2} + b_{5}\theta_{p}^{2} + b_{6}V^{2} + b_{7}\alpha\theta_{p} + b_{8}\alpha V + b_{9}\theta_{p}V$$
(13.1)

where the coefficients b_0 through b_9 were determined from a least squares fit of effective cooling velocity calibration data

$$((v_e/v)_1, \alpha_1, \theta_{p1}, v_1), ((v_e/v)_2, \alpha_2, \theta_{p2}, v_2), \dots, ((v_e/v)_n, \alpha_n, \theta_{pn}, v_n)$$

where n = the number of calibration data points.

In this section, the least squares technique and related equations required to determine the ten coefficients in Equation 13.1 from the calibration data are developed.

Corresponding to each calibration data point, there are two values of V_e/V : the experimentally measured value $(V_e/V)_{exp}$, and the value predicted by the empirical relation Equation 13.1, $(V_e/V)_{pre}$. The difference between these two values is defined as the deviation, ϵ

$$\varepsilon = (V_e/V)_{pre} - (V_e/V)_{exp}$$
 (13.2)

The method of least squares requires that the sum of squares of the deviations for all calibration data points

$$F = \sum_{i=1}^{i=n} \varepsilon_i^2$$
 (13.3)

be a minimum. This is accomplished by solving the following ten simultaneous equations:

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_0} = 0 \tag{13.4}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_1} = 0 \tag{13.5}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_2} = 0 \tag{13.6}$$

$$\frac{\partial F}{\partial b_3} = 0 \tag{13.7}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b_4}} = 0 \tag{13.8}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_5} = 0 \tag{13.9}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_6} = 0 \tag{13.10}$$

$$\frac{\partial \mathbf{F}}{\partial \mathbf{b}_7} = 0 \tag{13.11}$$

$$\frac{\partial F}{\partial b_8} = 0 \tag{13.12}$$

$$\frac{\partial F}{\partial b_9} = 0 \tag{13.13}$$

The ten simultaneous linear equations, which were obtained by carrying out the required partial differentiation, are displayed in matrix form in Equation 13.14. The ten coefficients, b_0 through b_9 , in Equation 13.1 can be obtained by solving this matrix set.

	ΣVe/V	Ve/V	ve/v	v _e /v	v _e /v	ve/v	2 _{Ve/V}	n/and	We/V	Σθ vve/v
1	ΣΛ	Σα	26	20	Σα	26.	Λ3	Σα	Σα	θ3
T	PO	b ₁	b ₂	ь э	P4	P ₅		b ₇		6 q
1										
	$\mathbf{A} \mathbf{G} \mathbf{A} \mathbf{A}$	$\Sigma\theta_{\mathbf{p}}V\alpha$	$\Sigma\theta_p^2 v$	$\Sigma_\theta \ v^2$	Σθ Vα ²	$\Sigma \theta^{3}_{p}$	$\Sigma_{p} v^{3}$	$\Sigma\theta_{\mathbf{p}}^2V\alpha$	$\Sigma_{\rm p} {\rm v}^2_{\rm o}$	$\Sigma\theta_p^2 v^2$
								$\Sigma \alpha^2 \theta_p V$		
	$\Sigma \alpha \theta$	$\Sigma \alpha^2 \theta$	$\Sigma \alpha \theta_{\mathbf{p}}^2$	$\Sigma \alpha \theta V$	$\Sigma \alpha^3 \theta$	$\Sigma^{\alpha\theta}$	$\Sigma\alpha\theta_{p}v^{2}$	$\Sigma\alpha^2\theta^2_{p}$	$\Sigma \alpha^2 \theta V$	$\Sigma\alpha\theta_p^2v$
	Σv^2	$\Sigma v^2 \alpha$	$_{\Sigma}v^{2}{}_{\theta}$	Σν3	$\Sigma v^2 \alpha^2$	$\Sigma v^2 \theta^2_P$	⁴ ν2	$\Sigma v^2 \theta_{p} \alpha$	$\Sigma V^3 \alpha$	Σv^3_p
	Σθ ² P	$\Sigma\theta^2_{p}$	$\Sigma\theta^3$	$\Sigma\theta^2_{p}V$	$\Sigma\theta_p^2\alpha^2$	φ ₀ γ	$\Sigma\theta_p^2 v^2$	$\Sigma \theta_{\mathbf{p}}^{3}$	$\Sigma\theta^2_{p}\alpha V$	$\Sigma \theta^3_p$
	$\Sigma \alpha^2$	Σ^{α}	$\Sigma\alpha^2\theta_p$	$\Sigma \alpha^2 V$	τα γ	$\Sigma \alpha^2 \theta^2$	$\Sigma\alpha^2 v^2$	2α3 P	Σ^{α}	$\Sigma \alpha^2 \theta_p V$
13.14.	ΣΛ	ΣVα	$\Sigma V \Theta_{\mathbf{p}}$	Σv ²	$\Sigma V \alpha^2$	$\Sigma V \theta^2_{p}$	203	Σναθ ρ	$\Sigma v^2 \alpha$	$\Sigma v^2\theta_p$
Equation 13.14	δ d b	$\Sigma\theta^{\alpha}$	$\Sigma\theta_{\mathbf{p}}^{2}$	$\Lambda^{\mathbf{d}}$ Θ \Im	$\Sigma\theta_{\mathbf{p}}^{2}$	Σθ ³	$\Sigma\theta_p v^2$	$\Sigma\theta^2_{\mathbf{p}}$	$\Sigma\theta^{\alpha}$	$\Sigma\theta_p^2v$
- 1	Σα	Σ^{α}	$\Sigma \alpha \theta$	ΣαΛ	Σ^{α} 3	$\Sigma \alpha \theta^2$	$\Sigma \alpha V^2$	$\Sigma \alpha^2 \theta$	$\Sigma\alpha^2 V$	$\Sigma \alpha \theta \frac{V}{p}$
Table 13.1.	а	Σα	ν δ δ	ΣΛ	Σ^{α}	Σ_{θ}^2	Σv ²	Σαθ	ΣαΛ	ν _q σ

XIV. APPENDIX E: TABULATION OF SLOW-RESPONSE DATA

The slow-response data for minimum and maximum noise conditions obtained at stations ahead of and behind each blade row for each of nine passage height locations are tabulated in this section. All data were obtained at a rotor speed of 1400 rpm and a flow coefficient of 0.42. The measured point-by-point circumferential distributions of total head are listed in Tables 14.1 and 14.2. In Tables 14.3 and 14.4 the blade-toblade circumferential-average values of total head, static head, absolute tangential flow angle, and incidence and deviation angles are tabulated for each blade span location. Finally, the circumferential-average outerannulus-surface static head values measured with the outer wall taps are given in Table 14.5 for each measurement station. The axial locations of the measurement stations with respect to the blade rows are depicted in Figure 3.1. Total head and static head are given with respect to atmospheric pressure. The sign conventions for tangential flow angle, incidence angle, and deviation angle are specified in Figure 12.1. The definitions of the Fortran variables used in the computer output listing of Tables 14.1 and 14.2 are listed at the beginning of the two tables. A complete listing of mathematical symbols is presented in the symbols and notation section.

Table 14.1. Point-by-point circumferential distributions of total head for minimum noise condition.

N*H X KG	×//8	N* H	\$57.4	N * K 6	4/58	N*M/KG	55/4	N*MYK G
	11	20.00	PHH=3	0.0	нны	0	I	0
96		96	11	86.9	SI	0	115	86.9
.43	00000	0.43	00000	0	0000	0	00000	0.21
0.43	0.213	0.43	21		-		-	3
00.	0.420	-	42	0	.42		.42	.2
00	0.622	~	62	0	• 62		.63	
643	0.832	0	83	2	.83		.82	0
00.	1.000	0.43	1.000	8	• 00	•	00.	0
0	HHd	00.07	BHHH	0.0	HHI	0.06		
76		-86.94	H8H	86.9		0		
00.0- 000	0000	0000-	00000	-1.7	0000	-8.6		
.22	.213	00.01	. 21	3.2	.21	.5		
000		00.0-	0.425	-2.59	0.421	-		
00.	.620	-0.22	.62	.5	.62	-		
00.	.833	00.0-	. 83	6	. 84	.5		
000	000	00.0-	00.	5	000			

 $Y/SS = Circumferential spacing, Y/S_S$.

HT = Total head with respect to atmospheric pressure, H, N·m/kg.

PHH = Percent passage height from hub, PHH.

HS = Static head with respect to atmospheric pressure, h, N·m/kg.

Table 14.1 Continued.

High	HH=10	14W/KG	¥.55	Ο ¥ X Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ Σ	\$5/	Z X X	55	N X X	55	N* M/K
1	5=-11	00	I	0.0	II T	0.0	I	40.00	I	0
7000 7000		3.3	1 8 8	11.03	1	40.00	II UI	108.78	III.	74 · LO
10 0 0 0 0 0 0 0 0 0	000	0	00.	4.0	000.	0.0	00.	0	000	4.0
4 1 1	101	0	• 10	4.	• 10	0.0	-	•	-	4.
######################################	211		. 20	4.	• 50	0	• 50	0	• 50	7.0
4412 4442 44	316	0.	• 30	4.0	- 31	0.0	. 31	•	• 30	7.
#### 0.545	412	0	. 41	4.0	. 41	0.0	. 41	0	.41	0.4
### 34	444	4	4 4 0	2.5	. 51	1.0	. 54	-1.0	.51	4.0
5518 - 332.03 5529 - 47.53 5	434 -	a .	.51	8.6	. 55	13.4	. 50	10.8	.59	2.1
645 - 472.14	518	0	. 56	47.5	.60	47.1	.63	44.3	.64	4.2
589 - 465.87 3 0.6627 - 96.40 0.6558 - 25.35 5 3 0.6677 - 55.5 6 4 3 0.6677 - 96.40 0.6558 - 25.5 5 6 4 3 0.6573 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 4 3 0.6758 - 25.5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	556 -	-	50	71.2	.63	77.9	99.	79.0	.67	3.0
617 - 96.92 617 - 96.92 617 - 96.92 618 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 619 - 96.92 610 - 96.92 610 - 96.93 610 -	580	۵.	.62	96.4	.65	95.1	.60	0.20	690	5.7
643 - 33.66 643 - 33.66 644 - 33.66 645 - 36.56 647 - 36.65 648 - 36.66 648 -	617	0	49.	91.8	. 70	73.5	.71	5000	.71	5.5
F 5 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	649	9	67	75.6	73	a	.75	47.6	.76	6.3
649 - 57, 36	673	0	1	42.1	10	0	170	14.0	.78	-
716 - 47.81	- 669	7	. 7.3	28.0	0	4	4 H 4	7	a	3.4
760 - 26.07 1.000	716 -	α	4	10	0	4	0	4.0	. P.S	3.0
PO2 - 10.43	760	C	0		0	4	0	0	00	
PHH=60.07 HNH=70.00 HNH=70.00 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.19 HN=106.10	- 000	4		1					0	4
PHH=60.00 PHH=60.00 HS==106.3P HS==106.3P HS==106.3P HS==106.42 HS==106.43 HS==106.42 HS==106.43 HS==106.43 HS==106.42 HS==106.43 HS==106.	D 47	1		•)	
PHH=60.00 PHH=70.00 HS=-106.3P HS=-105.42 HS=-105.42 HS=-106.3P HS=-105.42 HS=-106.42 HS=-106.43 HS=-106.	000	4								
PHH=60.00 PHH=50.00 HS=-106.38 HS=-106.39 HS=-106.34 C00 C00 C00 C00 C00 C00 C00 C	000	4								
РНН=60.00 HS=-106.38 HS=-106.38 COO 0.00 COO 0.000	000	0								
HS==106.3P HS==106.3P HS==106.3P HS==106.3P HS==106.3P HS==106.3P HS==106.3B HS==106.3B HS==106.3B HS==106.3B HS==106.3B HS==106.3B HS==106.4B	OY HH		I	0	I	0	I	0.00		
104	0-110	10	1 1 0	-	110	7 2 0	. 11	104-7		
210						-4-3	000	1 3 3 0		
219	100	0		4	-	4 9	- 10	110		
308	210	~	200	9.0	20	4.3	. 20	10.8		
409 -0.43	308	2	31	0	. 31	2.6	05.	10.8		
514 -0.43	604	4	. 41	0	. 41	2.1	. 41	1.6-		
608 -1.08 0.626 -2.16 0.6611 -2.60 0.616 -2.60 0.656 -11.2 0.656 -2.16 0.669 -10.39 0.666 -11.2 0.669 -10.39 0.666 -11.2 0.668 -11.2 0.701 -33.50 0.666 -11.2 0.701 -33.50 0.713 -44.40 0.714 -42.22 0.725 -46.5 0.725 -42.22 0.725 -44.40 0.735 -43.31 0.725 -46.5 0.725 -42.5 0.725 -42.23 0.725 -43.31 0.725 -72.7 0.725 -7	514	4	.51	4.0	. 51	2.3	.51	5.0		
649 -10.63 0.656 -6.66 0.669 -10.33 0.666 -11.2 680 -34,22 0.668 -31.40 0.701 -33.55 0.706 -26.55 731 -64.99 0.743 -45.49 0.735 -43.31 0.746 -65.5 771 -48.73 0.764 -42.23 0.751 -32.48 0.773 -72.7 798 -32.47 0.780 -21.66 0.735 -43.31 0.773 -72.7 815 -12.95 0.833 -4.33 0.812 -7.56 0.831 -36.9 7919 -1.08 0.923 -1.08 0.912 -7.56 0.950 -24.9 790 -4.33 0.950 -13.6	608	0	.62	2.1	.61	2.6	.61	9.0		
680 -34,22	- 649	a	.65	8.6	.66	10.3	· 6P	11.2		
707 -555.23	683	2	6.68	31.4	.70	33.5	.70	26.5		
731 -64.99 0.749 -44.40 0.735 -43.31 0.746 -65.55 771 -48.73 0.764 -42.23 0.751 -32.42 0.773 -72.7	707	2	.71	45.4	.71	42.2	.72	46.0		
771 -486.73 06.764 -42.23 06.751 -32.48 06.773 -72.77 -79.8	731 -	0	. 74	44.4	. 73	43.3	.74	65.5		
798 -32.42 0.780 -21.66 0.774 -22.73 0.705 -59.7 816 -12.09 0.811 -9.66 0.704 -14.07 0.816 -39.0 863 -2.16 0.833 -4.33 0.812 -7.56 0.831 -36.9 919 -1.08 0.923 -1.03 0.855 -4.33 0.855 -24.9 0.00 -0.43 1.000 -1.08 0.656 -3.3 0.957 -13.6	771 -	1	. 76	42.2	.75	32.4	.77	72.7		
816 -12.09 0.811 -3.66 0.704 -14.07 0.816 -39.0 863 -2.16 0.833 -4.33 0.812 -7.56 0.831 -36.9 919 -1.08 0.923 -1.02 0.856 -24.33 0.856 -24.9 000 -0.43 1.00 -1.06 0.950 -13.6 1.00 -4.33 0.961 -13.6	7 99 -	4	47.	9.	.77	22.7	.70	50.7		
P63 -2.16 0.833 -4.33 0.812 -7.56 0.831 -36.9 919 -1.08 0.923 -1.02 0.856 -4.33 0.856 -24.9 000 -0.43 1.000 -1.06 0.850 -13.4 1.000 -4.33 0.961 -13.4 1.000 -4.33 0.961 -13.4	- 619	0	.81	3.6	. 70	14.0	.81	39.0		
919 -1.08 0.923 -1.08 0.919 -4.33 0.859 -24.9 000 -0.43 1.000 -1.08 0.919 -3.90 0.902 -15.6 1.000 -4.33 0.961 -13.4	P 63	-	. P 3	4 . 3	a .	7.5	.83	36.9		
000 -0.43 1.000 -1.08 0.919 -3.90 0.902 -15.6	616	0	.92	0.1	· P5	4.3	. 85	54.0		
1.000 -4.33 0.961 -13.4	000	4	00.	1.0	0.01	3.0	05.	15.6		
					00.	4.3	90.	13.4		

ve it.i. continued.	STATIO	

HH=10.00 HH=10.00 HH=20.00 HH=20.									-	
PHH=10.00 HS= -30.10 H	47.88	×	1188	ĭ¥ X×	1788	SX/W*Z	¥7.88	N*N N*N	×/88	N*M/KG
HS= -30.10	Ŧ	10.0	HH H	20.0	I	0.0	I	40.0	II.	0.0
103 199.94 0.000 208.36 0.000 225.47 0.000 216.71 0.000 199.94 0.000 208.36 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.52 0.208 213.53 0.208 222 222 0.208 0.213 190.28 0.208 182.04 0.208 221.53 0.208 222 222 213.52 0.213 190.28 0.208 182.04 0.208 192.52 0.214.95 0.214 192.52 0.215.52 0.215.52 0.215.52 0.215.52 0.215.52 0.208 0.208 196.30 0.208 192.52 0.214.95 0.212 192.58 0.212 192.58 0.212 193.72 0.225 214.95 0.212 193.72 0.225 214.95 0.212 193.72 0.225 214.95 0.212 193.72 0.225 214.95 0.212 193.72 0.208 193.72 0	3:	-30.1	3=	-18.6	S	-8.6	S	0.0	S	7.7
103 191.83 0.111 197.84 0.110 221.52 0.105 225.48 0.103 206 212 185.91 0.206 225.91 0.209 219 212 185.91 0.305 188.62 0.306 225.91 0.30	00	199.9	00 .	08.3	00.	25.4	00.	16.7	000	5.96
212 185.91 0.205 188.62 0.208 213.84 0.206 225.91 0.209 219.33 1.182.04 0.314 2013.54 0.308 221.53 0.308 221.53 0.311 182.04 0.414 2013.54 0.415 1214.95 0.308 221.53 0.308 221.53 0.415 190.38 0.515 182.48 0.517 204.42 0.514 214.51 190.38 0.513 190.38 0.515 182.48 0.517 204.42 0.518 190.38 0.518 182.48 0.517 204.42 0.518 190.38 0.518 182.48 0.517 204.42 0.518 190.38 0.518 190.38 0.515 182.04 0.517 192.58 0.518 190.38 0.515 182.04 0.517 192.58 0.518 190.38 0.518 192.58 0.518 192.58 0.518 190.38 0.515 190.33 0.822 215.29 0.518 190.38 0.518 190.39 0.518 190.00 0.822 219.33 0.822 213.72 0.926 20.817 190.00 190.86 0.000 225.91 1.000 225.91 1.000 225.91 1.000 195.78 191.39 0.518 192.58 0.518 192.58 0.518 190.38 190.38 0.518 190.38	.10	91.8	. 11	97.8	. 11	21.5	.10	25.4	.10	06.8
315 185 25 0 311 182 04 0 314 203 54 0 308 221 53 0 308 222 51 51 51 51 51 51 51 51 51 51 51 51 51	.21	85.9	. 20	88.6	. 20	13.8	. 20	25.9	.20	19
410 191.83 0.415 183.14 0.414 191.25 0.411 214.95 0.415 183.14 0.414 191.25 0.411 214.95 0.415 183.14 0.414 191.25 0.417 204.42 0.411 220 618 211.26 0.617 202.48 0.617 192.88 0.618 214 20 0.617 192.88 0.618 20 0.618 20 0.618 20 0.618 20 0.618 193.71 0.618	.31	95.2	.31	82.0	. 31	03.5	. 30	21.5	.30	22.8
\$14 199.50	.41	91.8	.41	83.1	. 41	91.2	. 41	14.9	.41	20.0
618 211 56 0.617 202.88 0.619 182.04 0.617 192.58 0.618 204	.51	99.5	.51	90.3	.51	82.4	.51	04.4	.51	14.7
## 193 218 14 0 718 216 04 0 718 196 30 0 724 186 44 0 718 197 193 219 33 0 925 214 51 0 925 193 219 33 0 925 223 72 0 926 208 37 0 926 193 193 219 215 215 38 0 925 223 72 0 926 208 37 0 926 193	.61	11.5	.61	02.8	.61	82.0	.61	92.5	.61	9.40
925 215.29 0.823 219.33 0.822 214.51 0.822 193.01 0.823 193 925 207.17 0.925 215.38 0.925 223.72 0.926 208.37 0.926 193. 925 207.17 0.925 215.38 0.925 223.72 0.926 208.37 0.926 193. 925 207.17 0.925 215.38 0.925 223.72 0.926 208.37 0.926 193.48	.72	18.1	.71	16.0	.71	96.3	.72	86.4	.71	01.0
PHH=60.00 PHH=70.00 PHH=70.00 PHH=70.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PH=90.00 P	8 2	15.2	.82	19.3	. 82	14.5	.82	63.0	.82	93.6
PHH=60.00 PHH=70.00 PHH=80.00 PHH=80.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PHH=90.00 PH=90.00	.92	07.1	.92	15.3	.92	23.7	. 92	08.3	.92	93.2
PHH=60.00 HS= 14.61 HS= 20.70 HS= 26.20 HS= 31.39 103 195.04 0.000 199.86 0.000 196.52 0.000 195.72 31.39	00.	01.6	00.	4.60	000	25.9	00.	17.1	000	96.5
HS= 14.61 HS= 20.70 HS= 26.20 HS= 31.39 103 197.68 0.000 199.86 0.000 196.52 0.000 195.7 205 198.78 0.205 193.71 0.204 193.66 0.210 195.7 4.11 217.01 0.413 209.08 0.410 197.17 0.413 192.0 512 216.35 0.512 212.60 0.514 205.95 0.514 193.5 615 210.42 0.617 211.28 0.613 208.59 0.616 197.9 322 197.68 0.822 203.10 0.822 203.10 0.820 202.3 924 198.10 0.822 203.10 0.922 203.10 0.922 203.10 0.925 197.01	Ī	0.09	I	0.0	III	0.0	I	0.06		
.000 197.68 0.000 199.86 0.000 196.52 0.000 195.7 .103 195.04 0.104 196.56 0.106 197.61 0.102 193.5 .205 198.78 0.205 193.71 0.204 193.66 0.210 195.7 .310 210.86 0.315 199.42 0.308 191.03 0.318 191.3 .512 210.86 0.410 197.17 0.418 191.03 0.418 191.3 .512 216.35 0.512 212.60 0.514 205.95 0.514 193.5 .615 210.42 0.514 20.519 20.514 193.5 .722 202.07 0.719 204.25 0.719 208.59 0.516 197.9 .922 197.68 0.924 198.10 0.9822 203.10 0.922 203.10 .000 195.04 1.000 197.61 1.000 197.61 1.000 192.77	S	14.6	S	20.7	II S	26.2	S	31.3		
103 195.04 0.104 196.56 0.106 197.61 0.102 193.55 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5 3.5	000	97.6	00.	8.66	000.	96.5	00.	28.1		
205 198.78	.10	0.56	.10	96.5	. 10	91.6	.10	93.5		
309 210.86 0.315 199.42 0.308 191.03 0.318 192.0 411 217.01 0.413 209.08 0.410 197.17 0.415 191.3 512 216.35 0.512 212.60 0.514 205.95 0.514 193.5 512.5 210.42 0.517 211.28 0.613 208.59 0.616 197.9 202.07 0.719 204.25 0.719 208.59 0.616 197.9 203.0 0.822 203.10 0.822 203.0 202.0 203.0 0.924 199.10 0.929 197.61 1.000 192.7	.20	98.7	. 20	93.7	.20	93.6	.21	28.1		
•411 217.01 0.413 209.08 0.410 197.17 0.415 191.33 •512 216.35 0.512 212.60 0.514 205.95 0.514 193.57 •615 210.42 0.617 211.28 0.613 208.59 0.616 197.99 •722 202.07 0.719 204.25 0.719 208.59 0.720 203.0 •922 197.68 0.822 203.10 0.820 202.30 •924 198.10 0.929 197.61 0.920 202.43 •00 195.04 1.000 199.42 1.000 197.61 1.000 192.77	.30	10.8	.31	7.66	. 30	91.0	.31	95.0		
*512 216*35 0*512 212*60 0*514 205*95 0*514 193*5 *615 210*42 0*617 211*28 0*613 208*59 0*616 197*9 *722 202*07 0*719 204*25 0*719 208*59 0*720 203*0 *922 197*68 0*822 203*10 0*820 202*3*0 *924 198*10 0*929 197*61 0*920 202*3*0 *000 195*04 1*000 199*42 1*000 197*61 1*000 192*7	. 41	17.0	.41	0.00	. 41	97.1	. 41	91.3		
*615 210.42 0.617 211.28 0.613 208.59 0.616 197.9 *722 202.07 0.719 204.25 0.719 208.59 0.720 203.0 *922 197.68 0.822 198.10 0.822 203.10 0.820 202.3 *926 197.24 0.924 199.42 1.000 197.61 1.000 192.7	.51	16.3	.51	12.6	. 51	6.50	.51	93.5		
.722 202.07 0.719 204.25 0.719 208.59 0.720 203.0 .822 197.68 0.822 198.10 0.822 203.10 0.820 202.3 .926 197.24 0.924 198.10 0.929 197.61 0.925 196.4-	19.	10.4	.61	11.2	.61	08.5	.61	6.16		
*822 197.68 0.822 198.10 0.822 203.10 0.820 202.3 *926 197.24 0.924 198.10 0.929 197.61 0.925 196.4- *000 195.04 1.000 199.42 1.000 197.61 1.000 192.7	.72	05.0	.71	04.2	.71	08.5	.72	03.0		
.926 197.24 0.924 198.10 0.929 197.61 0.925 196.44	.82	91.6	.82	98.1	.82	03.1	.82	02.3		
-000 195.04 1.000 199.42 1.000 197.61 1.000 192.7	.92	97.2	.92	98.1	.92	94.6	.92	4.96		
	000	050	000	4.66	00.	94.6	00.	92.7		

The real Persons named in column 2 is not the owner, where the owner, which is the owner, where the owner, which is the owner, which is the owner, where the owner, which is the owner									
X/ SS	N*M/KG	¥//\$	N*MYKG	¥/88	N X X S	*/SS	N * H + G	¥7.85	N# MYK G
H	0	I	0	I	0	I	40.0	H	0
5=	46.8	S	50.1	S	53.2	S	56.2	25	58.6
0	73.6	00.	86.3	00.	85.2	00.	6.90	000	13.1
0	51.7	.04	73.2	. 07	76.4	.06	00.3	.10	12.4
0	42.1	60.	55.6	.13	57.8	. 14	75.1	.15	06.5
660 0	141.68	0.129	144.72	0.176	142.48	0.215	145.62	.21	83.6
-	49.5	• 15	39.2	. 21	41.3	. 27	43.4	.25	58.4
-	69.3	• 19	40.1	• 24	53.4	.31	57.6	.29	43.8
2	80.9	. 25	9.99	. 30	86.3	• 36	10.5	.32	47.5
3	85.9	.31	80.9	• 36	00.5	.46	63.7	.35	57.3
.3	95.3	• 42	85.2	• 44	0.90	• 56	98.8	.39	77.4
4.	81.5	. 50	85.2	. 55	04.0	• 62	03.5	.43	86.2
.5	77.6	. 60	84.2	• 66	01.6	• 69	08.0	640	87.9
9.	80.2	. 71	85.2	• 75	00.5	. 80	14.1	• 26	86.8
	89.7	. 80	87.4	. 84	63.6	16.	14.5	• 65	88.4
8	399	. 91	88.5	00.	87.4	00	080	.72	92.3
0	92.6	00.	96.68					.82	000
•	88.6							1.000	215.95
HHA	0.09	HH	0	I	0	I	90.0		
IVI	6105	U	3.8	U	65.0	S	67.A		
	198.79		189.89	00000	183.85		172.85		
-	07.5	. 11	93.8	.10	83.1	.10	67.4		
-	08.2	. 21	00.8	. 20	87.1	. 20	67.4		
0.235	. 26	9	98	0	86.	1	65.		
	74.7	. 31	80.0	• 34	12.9	.33	28.8		
.3	9.64	. 34	64.7	.38	24.0	• 36	20.0		
.3	50.3	. 37	51.0	. 41	45.3	.40	35.6		
.3	57.2	• 39	20.6	• 43	47.5	.42	29.3		
4.	84.5	. 42	63.7	.46	63.6	.45	43.9		
4.	9.96	. 46	90.3	.51	0.46	.47	59.8		
.5	7.86	.50	2.66	. 55	02.3	.51	76.1		
.5	96.6	• 56	01.8	.61	03.4	.61	87.4		
9.	4.46	.61	00.8	.72	02.3	69.	89.5		
1.	0.06	.71	96.4	. 82	97.5	.77	2.96		
.0	88.9	. 82	95.5	. 91	89.7	.83	63.6		
0	,			•	-				
	0	7	6.06	000	82.7	.93	82.6		

Table 14.1. Continued.

				STAT	ATION S				
Y/85	N*M/KG	¥7.85	N*M/KG	×/88	N*M/KG	Y/SS	N*M/KG	* /\$\$	N# WYK G
	10.0	I	20.0	I	30.0	I	40.0	# H	0.0
S	87.4	S	6.66	S	6.0	(1)	0.7	S=	4.6
00.	39.2	00.	37.0	00.	32.9	00.	340.4	000	49.3
100	44.3	10	43.4	. 11	2	0.112	330.81	. 1.1	339.74
. 20	44.3	- 20	49.2	. 21	45.7	.20	29.7	.21	32.2
.30	39.2	30	52.6	. 31	56.4	. 31	40.4	.32	29.0
4 1	32.8	. 41	50.5	. 41	61.7	. 42	52.2	.41	35.4
.51	24.7	51	46.6	. 51	59.69	. 52	57.5	.52	42.9
19	20.4	.62	42.3	.61	54.3	.62	59.7	.62	48.3
.72	21.5	.72	33.8	.72	46.8	.72	56.5	.72	50.4
.8	28.9	.82	31.6	83	41.4	. 82	50.0	. 82	52.6
.02	39.2	.92	35.5	.92	36.1	.92	43.6	.92	52.6
1.000	345.00	1.000	340.68	1.000	33.9	00.	37.2	1.000	46.3
I	0.09		70.0	I	80.0	I	90.0		
S	137.1	S	3.8	U	6.5	S	5.6		
000000	342.0		336.8		341.40		333.2		
-	42.	0	34.	0	37.	-	28.		
.20	37.8	. 20	34.7	.21	30.7	. 20	21.4		
.32	29.5	.32	29.4	. 31	25.3	. 32	17.1		
. 41	28.1	. 41	24.0	.42	22.1	. 41	19.3		
.52	37.8	.52	30.4	.51	26.4	. 51	25.7		
19.	41.0	.62	36.8	.62	32.8	.62	30.0		
.72	39.9	.71	37.9	.72	37.1	.71	31.0		
83	37.8	.82	37.9	.82	36.0	.82	31.0		
6	38.8	.93	34.7	.93	39.2	.92	33.2		
00	41.0	00.	34.7	000	40.3	00.	33.2		

Table 14.1. Continued.

HT Y/SS HT Y/SS HT Y/SS HT HT Y/SS HT HT H=10.00 H=10.00 HS= 199.00 HS= 199		
966-00 917-79 918-79	*N 88.7*	* M/KG
HSE 40 HSE 189 75 HSE 40 HSE 189 75 HSE 40 HSE 189 75 HSE 189 75 HSE 189 75 HSE 189 75 HSE 192 84 HSE 189 75 HSE 192 84 HSE 193 85 HSE 19	нн=50	0
312-87 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-79 317-99 318-42	S= 19	8.6
317.79 325.28 326.28 327.28 327.28 328.37 328.38 338.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 388.37 38	.000	20.4
329.28 329.528 329.528 329.528 320.663 0.419 330.663 0.423 331.91 0.527 330.664 0.419 331.91 0.529 330.664 0.419 331.91 0.527 331.91 0.662 308.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.36 0.752 208.66 0.752 208.66 0.752 208.66 0.752 208.66 0.752 0.811 0.052 0.752 0.812 0.062 0.752 0.813 0.762 0.811 0.062 0.066 0.0	.117 3	29.0
329.556 330.6310 330.634 330.637 330.637 330.637 330.637 330.637 331.911 0.529 335.13 0.529 335.13 0.529 333.2 274.99 0.759 285.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.759 286.89 0.815 286.89 0.816 0.820 0.82	.222 3	36.5
330.63 324.21 277.22 292.11 0.529 335.13 0.529 336.84 0.529 336.84 0.640 330.84 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.91 0.652 331.92 0.72 0.73 0.815 0.92 0.815 0.92 0.93	0.319 34	40.83
324.21 0.529 335.13 0.527 3311.1 277.13 0.529 335.13 0.527 3311.1 274.99 0.759 286.95 0.713 286.00 288.90 0.759 281.59 0.775 286.95 0.815 290.0 312.44 0.928 327.63 0.929 343.99 312.44 0.928 327.63 0.929 343.99 313.51 0.000 328.27 313.51 0.000 328.27 315.21 0.000 295.58 0.000 274.9 325.00 0.000 325.142 0.000 274.9 332.36 0.000 322.7 333.13.93 0.000 323.42 0.000 32.18.90 333.13.93 0.000 332.9 0.000 323.9 0.0000 323.9 0.000 323.9 0.000 3	.420 3	44.0
292 11 0 590 330 84 0 640 326 8 8 31 2 2 4 4 9 9 0 752 288 8 3 6 9 8 4 0 759 288 8 3 6 9 0 7 13 300 0 0 7 13 300 0 0 7 13 300 0 0 7 13 300 0 0 7 13 300 0 0 7 13 3 3 0 0 0 7 13 2 8 6 9 5 0 0 7 13 3 3 0 0 0 0 2 2 8 6 9 5 0 0 8 15 2 9 0 0 7 13 3 2 9 0 0 7 13 3 2 1 3 9 1 3 9 1 3 0 0 0 1 2 1 2 8 8 9 1 3 0 0 1 2 1 2 8 8 9 1 3 1 3 9 1 1 2 8 1 3 1 3 1 2 1 2 8 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1 3 1	.523 3	44.0
277-13 274-99 206-2 308-36 306-99 0.759 285-87 0.752 285-87 0.752 285-87 0.752 285-87 0.752 285-97 0.845 311-57 0.928 313-94 1.000 295-95 0.929 343-99 1.0000 1.0000 1.0	.621 3	41.9
298.90 0.712 285.87 0.752 285.00 2306.02 0.759 281.59 0.778 280.73 2312.94 0.928 311.657 0.959 281.59 0.778 280.73 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 313.99 0.928 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 312.28 0.918 313.99 0.928 271.2	.734 3	34.4
298.90 306.02 306.02 312.44 0.984 286.95 0.815 290.4 312.44 0.984 311.57 0.985 313.99 313.91 1.000 328.77 63 313.99 1.000 328.77 1.000 328.77 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.000 328.79 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1	.794 3	10.8
312.44 0.845 311.57 0.815 290.4 312.44 0.928 321.57 0.858 313.99 313.99 313.51 50.00	.82e 2	88.3
312.44 0.845 311.57 0.858 313.99 312.44 0.928 327.63 0.929 343.99 201.08	.865 2	73.3
312.44 0.928 327.63 0.929 343.99 313.51 1.000 328.70 0.929 343.99 313.51 0.000 328.70 0.929 343.99 315.21 0.000 328.70 0.929 343.99 325.50 0.000 328.70 0.929 343.99 0.929 343.99 0.929 343.99 0.920 323.42 0.920 323	.894 2	76.5
313.51 1.000 328.70 1.000 350.40 2010.00	.934 2	8.95
PHH=70.00 201.08 315.21 325.50 325.50 325.50 325.50 0.000 327.28 0.032 331.93 331.93 0.000 327.28 0.003 334.1 337.28 0.003 337.28 0.003 337.28 0.003 337.28 0.003 337.28 0.003 337.28 0.003 337.28 0.003 337.38 0.003 338.42 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003 338.43 0.003	•000	22.6
315.21 0.00 295.58 0.000 274.99 327.00 0.000 274.99 327.00 0.000 274.99 327.00 0.000 274.99 327.28 0.000 274.7 327.28 0.000 274.7 327.72 0.198 327.28 0.207 324.7 327.72 0.207 320.5 337.72 0.207 327.28 0.207 320.5 337.72 0.510 323.42 0.510 323.42 0.510 323.42 0.510 323.42 0.510 323.42 0.510 323.42 0.510 323.42 0.510 323.42 0.708 337.65 337.75 337.75 337.75 337.75 337.75 337.75 337.75 337.75 3		
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25.50 27.00 27.00 28.07 28.07 32.36 0.198 327.28 0.102 324.42 32.36 0.198 323.42 0.207 320.53 31.28 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 324.73 0.207 323.42 0.207 323.42 0.207 323.42 0.207 323.42 0.207 323.42 0.207 323.42 0.207 323.42 0.207 323.42 0.207 0.		
27.00 0.050 325.14 0.078 324.1 28.07 0.078 324.1 32.36 0.198 323.42 0.207 320.5 337.28 0.102 324.7 320.5 336.65 0.412 324.49 0.412 318.4 324.49 0.412 318.4 324.49 0.412 318.4 320.4		
28.07 0.088 327.28 0.122 324.77 32.36 0.198 323.42 0.207 320.55 337.72 0.314 321.28 0.305 316.6 337.72 0.517 332.42 0.507 320.55 336.65 0.611 337.35 0.613 329.9 337.99 0.708 337.99 0.715 337.6 0.613 329.1 0.867 336.70 0.782 339.1 0.867 312.28 0.911 285.30 0.980 271.2 337.99 0.995 252.02 1.000 274.2		
32.36 0.198 323.42 0.207 320.55 337.72 0.314 321.28 0.305 316.65 389.79 0.507 332.42 0.412 318.3 389.79 0.507 332.42 0.507 323.49 0.507 332.42 0.507 323.49 0.507 332.42 0.507 323.49 0.507 332.42 0.507 332.42 0.507 332.42 0.507 332.42 0.507 332.42 0.507 332.42 0.507 332.28 0.509 334.81 97 0.911 285.30 0.949 281.3 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 274.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.980 271.2 334.87 0.946 270.31 0.946		
37.72 0.314 321.28 0.305 316.6 399.86 0.412 324.49 0.412 318.3 36.65 0.611 337.35 0.613 329.9 318.9 0.708 337.99 0.715 337.6 0.827 329.9 0.715 337.6 0.827 329.8 0.910 304.2 0.81.97 0.867 312.28 0.910 304.2 74.47 0.946 272.02 1.000 274.2		
39.86		
38.79 0.507 332.42 0.510 323.44 336.65 0.611 337.35 0.613 329.9 18.42 0.708 337.99 0.715 337.6 18.42 0.827 329.85 0.782 339.1 81.97 0.867 312.28 0.910 304.2 74.47 0.946 270.31 0.980 271.2 36.26 0.9965 272.02 1.000 274.2		
36.65 0.611 337.35 0.613 329.9 31.93 0.708 337.99 0.715 337.6 18.42 0.765 336.70 0.782 339.1 61.97 0.827 312.28 0.839 334.8 74.47 0.911 285.30 0.949 281.3 36.26 0.946 270.31 0.980 271.2		
31.93 0.708 337.99 0.715 337.66 18.42 0.765 336.70 0.782 339.10 0.782 0.		
186.42 0.765 336.70 0.782 339.1 03.41 0.827 329.85 0.839 334.8 81.97 0.867 312.28 0.910 304.2 73.39 0.911 285.30 0.949 281.3 74.47 0.946 270.31 0.980 271.2 36.26 0.965 272.02 1.000 274.2		
03.41		
81.97 0.867 312.28 0.910 304.2 73.39 0.911 285.30 0.949 281.3 74.47 0.946 270.31 0.980 271.2 36.26 0.965 272.02 1.000 274.2		
73.39 0.911 285.30 0.949 281.3 74.47 0.946 270.31 0.980 271.2 36.26 0.965 272.02 1.000 274.2		
36.26 0.965 272.02 1.000 274.2		
36-26 0-965 272-02 1-000 274-2		
13 06 1 000 303 01		
13.00		

Table 14.1. Continued.

Y/88 N		-							
	HT #M/KG	¥7.88	N*M/KG	¥788	N*IH * W X K G	¥/55	N*M/KG	¥7.88	N* M/KG
HH=1	0	I	0.0	II	0.0	I	40.0	I	0.0
5= 2	6.9	= S	9.3	"S	0.3	S	0.2	S	8.9
0000	83.7	0000	491.9	0000	501.3	00.	492.6	000	480.7
.105	77.2	.10	7.06	60.	01.3	60.	01.7	600	88.8
503	67.6	.21	88.1	. 20	98.6	.20	03.2	.20	.50
.306	62.3	. 30	77.4	.30	87.5	. 30	68.86	.30	6.96
.415	63.4	. 41	68.5	040	82.1	.40	91.1	.40	95.6
.511	70.8	.51	6.89	. 50	78.5	.50	83.0	.50	84.9
609	78.3	.60	77.4	.60	77.2	. 60	77.7	.60	77.7
1	85	0.702	487.07	0.718	480.69	0.701	473.45	0.698	470.69
.823	88.6	.80	93.4	. 80	85.8	.79	71.9	.80	65.3
.922	35.8	06.	98.6	06 .	93.8	.89	77.0	06.	66.4
0000	82.2	00.	9.96	00.	8.65	• 00	89.8	00.	75.6
HH=60	0	I	0.0	I	0.0	I	0.00		
27	6.5		283.17	HSH	289.21	HS=	295.07		
.000	66.3	0000	461.2	0000	467.8	00.	465.2		
4 00	73.	600.0	65	60	68	0	68		
.203 4	79.2	. 20	67.2	• 19	71.0	. 20	68.4		
.303 4	85.8	.30	67.6	.30	67.8	.31	64.1		
4 05 4	85.0	.40	71.9	.40	64.6	.40	6.09		
.500 4	83.9	. 50	76.6	. 50	70.6	.50	63.0		
• 606 4	81.3	.60	70.3	.59	75.3	.61	67.3		
• 705 4	75.3	.70	80.8	69.	78.4	.70	4.69		
4 662.	65.7	.80	76.1	. 79	78.4	.80	70.5		
4 E68.	60.3	68.	6.59	05.	71.0	06.	5.99		
4 000	8.99	000	61.6	000	65.7	00	64.1		

850.00 4885.77 4885.77 4885.77 4865.83 4865.83 4866.83 4866.83 4886.83 4886.83 4886.83 4886.83 4886.83 MIKG S 000000000000 N K K Om 4444444444 ii 11 0 00 4 0 M 01 00 0 4 0 8 0 0 M 01 0 0 Y/55 0000000000000 00000000000000 320.00 466.30 466.30 466.30 475.30 475.30 477.30 427.30 427.11 427.11 427.11 427.11 427.11 427.11 427.11 427.11 PHH × 80 · 00 HS = 337 · 03 111 458 · 61 205 4 60 · 82 310 460 · 82 406 460 · 82 508 460 · 82 508 463 · 69 508 463 · 69 739 466 · 67 739 466 · 67 739 466 · 67 739 466 · 67 739 468 · 86 813 459 · 27 903 461 · 66 MIKG 0 ATION X/S 000000000000000 000000000000000 N*M/K X/S 00000000000000 0000000000000 Concluded *M/KG 14 OM H 0000112844016160 25 Table 010-0M40000FF000 0000000000000

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Table 14.2. Point-by-point circumferential distribution of total head for maximum noise condition.

				STATION 1					
×/ SS	N*M X K G	Y/SS	N*MXKG	Y/SS HT		88/7	1 × × × × × × × × × × × × × × × × × × ×	\$57.	N* M X K G
I	=10.00	!! 	0	HH=30.00		4 = H	00	I	00 00
100	0.4	000	4.0	0.00 000		0000	0.0	0000	C
0.217	0.43	0.213		17 0.2	2 0	217		-	
4		42	0	425 -0.0		425	0	.42	•
0		62	0	.621 -0.0		.624	0	.63	
00		83	0	834 0.2		833	0	.82	
0		00	4	.000 0.2		000	0	000	•
I	60.09	HHd	70.00	H=80.0		OHHHA	0		
II S	10	11	86.0	S= -86.5		1 118	LO.		
000	-0.00	0.000	00.0	.000 -1.7		000	8.6		
N	-	21	0	.212 -3.2		-	.5		
		43		25 -2.5	0 6	N	8.2		
6	-	62	2	.625 -2.5		N	.2		
00	-	83	0	.834 -1.9		4	.5		
0		1.000	0	.000 -2.5		0			
		-		The state of the s			-		

 $Y/SS = Ctrcumferential spacing, Y/S_S$.

HT = Total head with respect to atmospheric pressure, H, N.m/kg.

PHH = Percent passage height from hub, PHH.

HS = Static head with respect to atmospheric pressure, h, N·m/kg.

				STATI	10N 2				
XX 88	N*MYK G	×7.55	N*H WXX BXX	*/SS	N*M/KG	×/88	N*MYKG	Y/SS	N*M/KG
	10.0	I	20.0	HH	0.0	I	40.0	HI	00.00
S	1111.8	S	110.4	5=-	.2	U	108.1	5=-	.2
000	0.0-	00.	0.0-	0000	0.0-	00.	0.0-	000	0.0-
.10	0.0	.10	0.0	. 10	0.0	.10	0.0	.10	0.0
.21	0.0	.21	0.0	. 21	0.0	. 20	0.0	.20	0.0
.32	0.0	. 32	0.0	. 32	0.0	.31	0.0	.32	0.0
.46	2.1	.42	0.0	. 43	0.0	.41	0.0	• 4 1	0.0
.49	0.6	.48	1.7	.52	1.7	.55	1.1	.51	0.0
.54	7.3	.51	6.1	. 55	11.4	.63	36.2	•61	6.5
0.578	-75.32	0.559	-31.79	0.616	-52.65	0.665	-66.93	0.643	-20.84
.61	79.6	.61	72.3	• 65	75.0	69.	81.1	•67	53.7
.65	5.0	.63	5.4	• 67	87.3	•73	61.4	.71	6.7
.68	75.3	.68	70.1	• 70	74.5	.77	35.9	•75	61.4
.73	37.6	. 74	24.1	• 73	35.1	.82	4.3	.82	13.1
.77	19.3	.77	7.6	• 78	7.6	. 93	0.0	•86	3.5
.83	4.7	.82	1.7	.82	1.7	00.	0.0	16.	0
.92	1.0	· 94	0.0	.93	0.0			000	0.0
00.	4.0	00.	0.0	• 00	0.0				
Ī	0.09	I	70.0	HH	0.0	I	0.06		
HS=-	106.3	S	105.5	S=-	0	S	104.2		
	0.0		-0.4	0000	-3.9		-10.9		
-	0	• 15	0.4	• 16	4 . 3	• 15	8.7		
8	0	. 32	0.4	. 31	2.6	.31	8.3		
.3	0	. 48	0.4	• 46	5.6	.47	7.6		
4.	•	.61	1.1	.61	5.6	.62	6.5		
.5	0	• 65	8.3	99.	2.4	69.	12.7		
• 6	2.1	• 68	23.0	• 68	19.7	.72	41.6		
.6	20 . 8	.71	43.8	. 71	39.4	. 74	63.5		
• 6	40.5	.72	47.1	.73	43.8	• 76	72.3		
0.729	•	9	3	9	6	9	2		
	51.5	. 80	15.3	. 78	16.4	. 82	20.4		
. 8	12.0	. 81	2.6	. 81	7.6	.86	21.9		
.8	3.2	.86	5.6	. 84	3.9	. 92	14.2		
0	•	• 94	1 • 1	. 92	3.2	00.	10.9		
		00.	4.0	00.	3.9				

Table 14.2. Continued.

				STATION	10N 3				
¥7.88	N#M/KG	X//S	N*M/KG	*/SS	N * K 6	¥7.88	HT N*M/KG	* /\$\$	HT N*M/KG
"HH a	10.0	I	20.0	I	30.0	HH	40.0	I	00
HSH	0.2	S	18.6	U)	8.6	S	0.0	S	7.7
0	01.9	00.	11:11	00.	25.3	00.	11.3	000	91.7
0	94.8	60.	06.2	60.	24.3	60.	25.2	.10	08.8
2	87.6	. 20	94.4	. 20	17.9	. 20	27.3	.20	23.1
3	86.9	. 30	86.9	.30	09.3	.30	24.6	.30	25.8
4.	91.2	. 40	85.4	.40	9.46	.40	18.8	.40	22.0
5	01.9	. 50	4. 46	640	83.2	. 50	09.2	640	14.5
5	07.7	. 59	96.5	. 59	78.3	.59	95.3	.59	08.1
0.693	213.27	269.0	206.20	0.692	182.00	0.694	185.33	0.693	198.56
1	11.9	.79	13.2	. 79	000	.79	84.6	.78	0.16
0	10.4	.89	16.8	. 89	15.7	.89	24.7	.89	86.8
	03.0	00.	10.4	00.	26.8	000	13.0	00.	04.5
I	60.03	I	C	I	C	I	0		
U	14.5	ISI	20.6		26.1		31.2		
0	7.16	00.	98.4	00.	9.96	00.	94.5		
0	92.1	60.	95.9	. 10	7.86	60.	93.6		
.2	03.8	.19	94.1	. 20	93.0	• 19	95.1		
.3	15.2	. 30	02.3	. 30	91.5	. 30	64.1		
5	18.1	.40	10.8	. 40	98.3	.40	91.5		
4.	15.6	64.	12.3	640	04.7	. 50	93.6		
5	10.9	.59	10.2	. 59	07.3	.59	97.3		
.6	02.8	69.	04.8	69.	07.3	69.	01.5		
162.0	94.	9	. 16	0	04.	9	01.		
00	92.1	.88	95.2	. 88	96.2	. 89	4.66		
0.	91.7	.00	0.86	00.	9.96	00.	91.5		

And the second

00 • 00 60 • 00 20 • 00 20 • 00 21 3 • 00 10 0 MYKG * 5 (V) > 000000000000000 0.00 9 N*M/K 00-----X/S 0000000000000 0000000000000 00.00 00 MIKG 4 ō ATI 11 X/S 00000000000000 000000000000000 20.00 180.00 180.00 190 70.00 65.21 1182.32 1198.32 1205.72 2007.88 2007.88 190.72 1181.34 1140.83 1141.85 9 N*M/K S X/S 0000000000000 00000000000000 =60.00 63.00 183.63 208.93 213.73 207.19 199.65 193.66 182.11 170.11 154.41 141.32 168.37 80.00 90 N*M/KG 04---11 SS rable > 00000000000000

10-1-1-1-1-1

Continued

14.

Table 14.2. Continued.

¥7.85	N*N N*N	1/55	N*M/KG	* /\$\$	N*NYKG	¥7.88	N*W/KG	¥7.88	N*N NXK
1	10.01	I I	0.0	I	0.0		40.0	I	0.0
15	000	115	0.5	S	1.7	S	121.7	S	0.5
0	25.7	0000	352.6	00.	353.4	000	345.1	000	349.7
0	10.	. 08	48.9	. 10	57.8	60.	49.5	.08	51.9
-	16.5	. 19	42.3	0	355.64	0.191	352.79	0.192	351.97
3	20.2	. 29	37.3	.29	52.3	. 29	53.8	.29	49.7
M	9.60	39	36.4	. 39	49.0	.39	52.7	.39	47.5
4	39.9	640	35.8	.49	44.7	. 48	48.4	.48	43.2
5	46.4	. 59	39.5	. 59	39.2	.58	45.1	.58	37.7
9	47.1	.68	46.1	. 68	38.1	.68	41.8	.68	31.1
	42.	. 78	52.2	.77	40.3	.78	40.7	.78	31.1
00	36.6	. 88	54.8	. 88	45.7	000	41.8	. 88	39.9
1.000	327.91	1.000	353.99	0	54.5	00.	47.3	000	51.9
	,		,		(:			
III	0.0	III	0000	HII	0000	I	00.06		
115	8.4	II S	5.2	Sil	1.3	S	7.15		
000.	337.6	0000	318.9	00.	24.6	00.	26.5		
.08	45.3	.08	23.3	60.	23.5	· 09	24.3		
0.188	347.56	0.188	328.78	0.203	326.82	0.205	325.86		
62.	49.7	. 29	34.2	. 29	26.8	.30	24.7		
39	51.9	. 39	40.8	040	26.3	.40	22.5		
4 8	40.7	.48	47.4	640	33.4	640	21.4		
.58	44.2	. 58	48.5	. 59	41.7	.59	26.9		
.68	33.3	.68	44.1	69.	45.4	69.	33.9		
.78	22.3	. 78	34.2	. 79	45.4	.79	35.7		
888	23.4	.87	23.3	. 89	35.5	. 89	34.6		
1									

And the second

	STATION
Continued.	
Table 14.2.	

			STAT	9 NOI				
H 55/A	KG Y/SS	N*H N*M/KG	\$5/A	Z * Z X Z	*/ \$\$	N# I H	¥7.85	N * K / K G
0.01=11	I	0.0	I	30.0	HHI	0 0	I	0.0
1.661 =5	HS=	188.5	S	1.8	II S	6.4	S	7.8
.101 .000	8 0.00	325.0	00.	336.7	00.	41.7	000	47.1
.027 789.	3 0.04	05.3	.05	25.1	.06	37.3	.11	42.
.058 276.	7 0.10	81.2	. 10	02.1	.10	28.1	61.	20.8
.177 460.	1 0.13	74.6	. 16	80.2	.16	04.9	.25	50.5
0.123 276,	57 0.167	278.40	0.186	276.98	0.209	282.15	0.285	279.28
.164 234.	6 0.23	06. 8	. 22	83.5	. 24	76.0	.34	69.1
.200 109.	7 0.30	26.1	. 27	07.6	.27	83.6	.40	17.6
.254 113.	8 0.36	31.5	. 31	25.1	.33	12.1	.42	20.8
.311 512.	1 0.42	33.7	. 36	35.4	.39	20.6	.52	26.3
.410 112.	1 0,50	34.8	. 43	40.4	44	34.0	.62	32.0
.507 114.	3 0.61	34.8	. 50	44 . B	.52	38.4	.72	41.7
.602 119.	0.10	33.7	.60	47.7	.62	43.9	.82	48.2
.700 .123.	7 0.80	33.1	.70	40.8	.72	47.8	.92	48.2
.798 127.	06.00	32.6	. 80	47.0	.82	47.E	000	47.1
.001 100.	00 1 0	28.8	06.	43.3	.92	45.0		
.054 124.			00.	37.6	00.	41.7		
.000 112.								
HH=60.0	I	0.0	I	80.0	III	0.0		
S= 200.3	H	2.6	S	4.6	-S	6.5		
.000 340.	0	319.3		319.3	0000	304.2		
.113 144.	2 0.10	24.1	-11	15.4	.10	97.2		
.203 142.	2 0.20	32.	0	17.	-	84.		
.256 125.	1 0.24	31.1	• 26	16.5	.28	70.3		
.304 296.	4 0.28	19.7	. 29	11.0	. 35	58.5		
.334 283.	0 0.32	0.00	• 33	8.96	• 38	51.5		
.382 234.	5 0.35	86.4	• 36	77.7	• 42	9.29		
.423 319.	3 0.38	81.4	• 39	71.6	• 45	0.56		
.457 326.	0 0 0	8.06	• 43	84.3	• 40	21.7		
.521 324.	1 0.44	24.1	.46	14.3	• 56	27.9		
624 321.	2 0.48	37.7	.51	37.7	.62	32.2		
.729 324.	1 0.54	39.5	. 59	40.6	.71	30.5		
. A 31 131.	8 0.61	35.1	. 70	39.5	.81	23.9		
.026 138.	5 0.71	28.1	. 81	32.9	.91	11.9		
.000 340.	4 0.81	21.5	. 91	24.1	00.	03.8		
	0.91	18.6	00.	20.2				
	00.	20.8						

Table 14.2. Continued.

				STATION	10N 7				
*/ SS	N * M K G	×/58	N*M/KG	×/58	N# H	×/58	N*MYKG	×/88	N*M/KG
HHO	10.0	I	0.0	I	0.0	I	40.0	I	0.0
HSH	7.8	S	0.1	S	1.1	S	0.0	S	4.6
0	479.1	00.	477.3	00.	472.7	00.	474.0	00.	483.2
-	86.0	. 10	86.4	.10	72.7	.10	67.0	.10	73.0
2	87.1	. 20	-	. 20	79.9	. 20	5		
3	85.6	.30	94.0	• 30	90.1	.30	74.0	.30	63.2
4	A1.3	.40	93.4	. 40	99.5	040	84.8	.40	70.1
.5	73.0	64.	90.3	.49	02.5	640	95.7	.50	81.0
9.	64.4	.59	83.8	.59	6.66	.59	02.2	.59	91.0
9	9.69	69.	74.5	69.	91.2	69.	01.8	69.	9.55
1.	62.2	.79	6.99	.79	83.0	.79	95.3	.79	97.5
8	8 69	. 89	65.8	. 89	78.2	.89	83.7	689	92.5
1.000	479.15	1.000	72.3	1.000	473.43	1.000	72.2	000	83.2
-	(-	(-	(0		20
I	00.09	I	000	I	000	I	00.00)3
S	77.0	IN	83.60	H	86.64	S	95.48		
000	85.8	00.	70.8	00.	75.2	000	62.1		
60.	78.4	. 10	70.8	• 10	70.2	.10	53.4		
.20	71.5	. 20	2.69	. 20	67.2	. 20	49.0		
.30	62.8	. 30	64.3	. 30	62.2	.30	53.4		
.40	9.09	. 40	58.4	.40	58.9	040	61.0		
.50	68.0	.50	65.4	64.	69.59	.50	70.8		
.59	73.0	. 59	71.9	. 59	77.4	.60	71.9		
.70	78.4	69.	72.3	69.	78.5	69.	68.6		
.79	91.7	e 79	73.0	.79	78.5	.79	67.5		
0.896	483.27	0.890	471.49	0.889	478.54	0.895	468.65		
000	92.4	00.	68.6	00.	73.7	000	63.2		

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EX. in m S S 9338.000
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944865.0000 0 201010110011000 ¥ X × X/55 0000000000000 00000000000000 N*M/KG 0 ATION ST S 000000000000000 000000000000000 N*M/KG X/85 00000000000000 000000000000000 Concluded N*M/KG 0.00 14.2 310 44444444 33 11 Table 58

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Table 14.3. Blade-to-blade circumferential-average values of total head, static head, tangential flow angle, and incidence and deviation angles for minimum noise condition.

	Percent Pass.Ht. From Hub	H N•m/kg	h N•m/kg	β _y degrees	i degrees	δ degrees
Station 1	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	0.23 0.83 0.11 0.07 0.16 0.05 -0.04 -2.54 -7.99	-86.95 -86.95 -86.95 -86.95 -86.95 -86.94 -86.94 -86.94	-0.01 0.07 -0.37 -0.65 -0.88 -1.12 -0.66 -1.05 -1.08		0.01 -0.07 0.37 0.65 0.88 1.12 0.66 1.05
Station 2	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	-18.32 -13.85 -13.10 -11.87 -10.89 - 7.82 - 5.72 - 6.93 -17.16	-112.33 -111.03 -109.34 -108.78 -107.84 -106.98 -106.18 -105.43 -104.79	24.75 23.81 22.96 22.00 21.29 20.34 20.30 19.43 18.91	8.03 6.78 6.75 6.74 6.91 6.61 6.24 6.49 8.36	16.02 15.66 15.27 15.08 14.76 14.69 13.64 13.49
Station 3	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	200.61 200.21 205.10 208.85 207.30 204.39 202.25 200.15 196.12	-30.10 -18.61 - 8.69 0.01 7.77 14.61 20.70 26.20 31.39	53.92 51.77 48.89 47.27 45.96 44.76 44.14 43.17 45.99	0.44 -0.60 -2.54 -2.98 -2.60 -2.37 -2.51 -3.19 0.40	16.31 16.15 14.42 12.33 11.26 10.47 9.57 9.00 9.57
Station 4	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	180.39 178.24 188.52 192.44 191.17 191.18 190.61 187.43 174.24	46.82 50.17 53.24 56.20 58.95 61.55 63.89 65.99 67.82	35.26 33.78 33.26 32.03 32.62 31.87 31.10 30.14 30.63	-1.99 -0.84 -1.86 -1.41 -0.29 0.63 1.33 2.35 4.99	9.59 9.10 9.52 9.26 10.90 11.11 11.09 10.79 12.02

Table 14.3. Concluded.

	Percent Pass.Ht. From Hub	H N•m/kg	h Nam (ka	βу	i	δ
	FIOR HUD	N°m/kg	N·m/kg	degrees	degrees	degrees
	10.00 20.00	333.54 342.63	87.42 99.95	54.89 51.22	1.41 -1.14	12.92 12.11
5	30.00	347.08	110.92	49.56	-1.87	10.45
Station	40.00	346.04	120.74	48.57	-1.69	9.36
t.	50.00	343.01	129.46	47.51	-1.04	8.80
ta	60.00	337.45	137.13	46.30	-0.84	8.72
0,1	70.00	333.65 332.57	143.85 149.93	45.40 45.14	-1.25	8.27
	80.00	326.94	155.68	47.19	-1.23 1.60	7.76 8.71
	90.00	320.94	133.00	47.13	1.00	0.71
	10.00	313.91	186.40	35.71	-0.88	10.04
	20.00	322.40	189.75	33.44	-1.61	8.76
9	30.00	330.58	192.86	32.92	-2.23	9.18
	40.00	331.64	195.85	32.50	-1.38	9.73
Station	50.00	327.85	198.60	32.56	0.23	10.84
at	60.00	325.09	201.08	31.42	1.62	10.66
St	70.00	322.35	203.26	31.05	2.59	11.03
	80.00	319.86	205.28	31.07	3.41	11.73
	90.00	309.44	207.27	34.80	5.79	16.18
	10.00	/76 10	226 00	F2 75	0.07	10.01
	10.00 20.00	476.12 484.20	226.90 239.35	53.75 50.96	0.27	13.01
~	30.00	488.29	250.37	49.49	-1.41 -1.94	11.88
7 7	40.00	487.02	260.21	48.33	-1.94	10.19 9.18
Station	50.00	481.82	268.91	47.43	-1.12	8.92
at	60.00	475.43	276.53	46.27	-0.86	8.94
St	70.00	471.28	283.17	45.11	-1.54	8.54
	80.00	471.30	289.21	45.65	-0.71	7.85
	90.00	466.43	295.07	47.71	2.12	8.76
	10.00	442.10	317.91	35.03		9.37
	20.00	461.52	321.35	34.08		9.40
∞	30.00	466.03	324.77	33.84		10.10
on	40.00	465.42	327.90	32.33		9.55
Station	50.00	464.35	330.59	31.15		9.43
ta	60.00	458.73	332.98	30.85		10.10
S	70.00	454.27	335.08	29.88		9.87
	80.00	455.80	337.03	30.93		11.59
	90.00	444.97	339.05	33.66		15.04

Table 14.4. Blade-to-blade circumferential-average values of total head, static head, tangential flow angle, and incidence and deviation angles for maximum noise condition.

	Percent Pass.Ht. From Hub	H N•m/kg	h N•m/kg	βy degrees	i degrees	δ degrees
Station 1	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	0.23 0.83 0.11 0.07 0.16 0.05 -0.04 -2.54 -7.99	-86.51 -86.51 -86.51 -86.50 -86.50 -86.50 -86.50	-0.01 0.07 -0.37 -0.65 -0.88 -1.12 -0.66 -1.05 -1.08	0.01 -0.07 0.37 0.65 0.88 1.12 0.66 1.05	
Station 2	10.00	-17.22	-111.85	25.66	7.70	15.11
	20.00	-12.87	-110.47	24.25	6.58	15.22
	30.00	-11.55	-109.25	22.99	6.42	15.23
	40.00	-10.39	-108.17	22.24	6.43	14.83
	50.00	-10.02	-107.22	21.03	6.83	15.02
	60.00	- 7.20	-106.37	20.34	6.60	14.68
	70.00	- 5.87	-105.59	19.84	6.41	14.09
	80.00	- 6.87	-104.86	19.46	6.57	13.46
	90.00	-15.95	-104.25	17.96	8.34	14.14
Station 3	10.00	200.79	-30.24	53.98	0.50	16.21
	20.00	201.18	-18.66	51.94	-0.42	15.88
	30.00	203.81	- 8.67	49.11	-2.31	14.61
	40.00	207.85	- 0.01	47.19	-3.06	12.52
	50.00	207.08	7.72	46.02	-2.54	11.29
	60.00	203.45	14.57	44.92	-2.21	10.62
	70.00	201.96	20.66	44.16	-2.48	9.60
	80.00	199.71	26.15	43.03	-3.33	9.06
	90.00	196.13	31.29	45.72	0.13	9.53
Station 4	10.00	178.04	48.51	35.87	-1.30	10.20
	20.00	179.62	51.82	33.50	-0.72	8.83
	30.00	188.69	54.88	33.79	-1.70	10.05
	40.00	188.47	57.90	33.13	-0.72	10.36
	50.00	189.63	60.59	31.73	0.28	10.01
	60.00	192.12	63.00	30.91	0.88	10.16
	70.00	190.33	65.21	30.14	1.73	10.13
	80.00	187.62	67.19	29.68	2.57	10.34
	90.00	175.69	69.08	32.65	4.97	14.03

Table 14.4. Concluded.

	Percent Pass.Ht. From Hub	H N•m/kg	h N•m/kg	βy degrees	i degrees	δ degrees
Station 5	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	332.45 344.77 347.79 347.22 343.50 340.32 334.16 332.95 327.87	88.00 100.59 111.72 121.72 130.58 138.41 145.26 151.37	55.10 51.36 50.28 48.97 43.15 46.86 45.75 45.44 47.44	1.63 -1.01 -1.15 -1.29 -0.40 -0.27 -0.90 -0.92 1.85	13.12 11.80 10.22 9.22 8.81 8.44 8.43 7.93 8.83
Station 6	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	312.48 322.44 331.20 330.43 329.57 326.93 322.75 320.84 303.31	185.12 188.55 191.83 194.98 197.81 200.39 202.64 204.66 206.53	35.76 34.04 33.95 33.01 32.85 31.95 30.89 31.08 32.55	-0.85 -1.89 -2.62 -1.41 -0.21 1.13 2.38 3.18 6.77	10.09 9.36 10.21 10.24 11.13 11.20 10.88 11.73 13.93
Station 7	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	474.94 482.18 486.92 484.07 481.16 474.10 468.73 471.29 462.62	227.81 240.18 251.14 260.92 269.49 277.03 283.60 289.64 295.48	53.89 51.13 49.73 48.32 47.32 46.22 45.32 46.02 47.64	0.41 -1.23 -1.70 -1.93 -1.23 -0.91 -1.33 -0.34 2.05	13.30 12.27 10.46 9.77 9.14 9.23 9.00 7.94 9.43
Station 8	10.00 20.00 30.00 40.00 50.00 60.00 70.00 80.00 90.00	438.72 460.48 466.08 465.12 463.67 460.24 454.25 456.04 442.30	317.69 320.91 324.33 327.47 330.14 332.48 334.55 336.51 338.46	32.95 33.78 33.88 32.33 30.86 30.19 29.88 30.81 32.48		7.28 9.10 10.14 9.56 9.14 9.43 9.87 11.47 13.87

Table 14.5. Circumferential-average outer-annulus-surface static head for minimum and maximum noise conditions.

Minimum	n Noise	Maximum	m Noise
Measurement Station	Outer Wall Static Head N·m/kg	Measurement Station	Outer Wall Static Head N·m/kg
1	- 86.94	1	- 86.50
2	-104.23	2	-103.67
3	36.82	3	36.85
4	69.20	4	70.78
5	161.53	5	162.75
6	208.96	6	207.94
7	300.68	7	301.17
8	340.67	8	340.04

XV. APPENDIX F: TABULATION OF FAST-RESPONSE HOT-WIRE DATA

The fast-response, hot-wire, circumferential survey data obtained over the first two stages of the compressor for the minimum noise condition are tabulated in this section. This data were obtained at a rotor speed of 1400 rpm and a flow coefficient of 0.42. The periodic-average three-dimensional velocity vector at each flow-field measurement point is completely specified by the listing of velocity magnitude, tangential flow angle, and radial flow angle. Frozen rotor-blade survey data for various rotor blade positions are tabulated in Table 15.1. Passing rotor-blade survey data are listed in Table 15.2. The sign convention for the tangential and radial flow angles is given in Figure 4.12. The definitions of the computer output variables used in the table headings are as follows:

 $Y/SS = circumferential spacing, Y/S_S$

V = absolute velocity, V, m/s

BETA Y = absolute tangential flow angle, β_{v} , degrees

BETA R = radial flow angle, β_r , degrees

PHH = percent passage height from hub, PHH

 $YOR/SR = circumferential rotor blade position, <math>YO_R/S_R$

Fast-response circumferential survey data obtained with frozen rotor-blade survey method at minimum noise condition. Table 15.1.

					STA	ATION 3					
X . SS	> × ×	BETA Y	BETA R	X/SS	> w <	BETA Y	BETA R	¥7.88	× × × × × × × × × × × × × × × × × × ×	BETA Y	BETA R
PHH=1	0.00 R=0.00			PHH=20 YOR/SR	00 00 00 8 = 0 0 00			PHH=30	00.0=		
0.000	22.434	48.357 47.655 48.022	0.285	0.052	21.859	46.198	0.468	0.000	21.844	44.665 45.111 45.089	0.159
	1.52	8.03	.99	. 20	0.88	6.85	0.86	. 20	1.33	4.65	.52
30	1.67	8.32	1.64	23	0.44	6.68	0.07	. 25	0.75	4.93	0.15
100	0.58	2.87	0.67	30	9.86	5.97	93	.33	0.37	3.66	.21
m m	1.03	3.12	.86	33	9.06	0.58	0.85	.38	9.89	3.83	2.12
200	1.22	3,56	.35	38	9.05	7.05	1 . 49	.43	9.21	2.48	0.84
4.	1.36	8.13	0.00	443	0.54	3.27	225	4 4 8	8 6 6 1	5.47	80 0
44	2.53	9.09	.19	440	9.61	0 4 0 4 4 1 8 0 1	200	53	80.11	4.79	960
40	3.25	4,36	.03	.54	90.10	4 . 38	. 97	.59	9 4 6	5.12	000
S. R.	3.43	2.21	.32	.56	1.99	3.25	.09	.61	9.76	2.41	. 33
.0	2.94	9.63	.85	.61	2.01	7.81	. 1.1	99	1.59	7.69	.05
0 0	2.96	9.04	0.0	• 66	1.93	6.94	80	. 72	1.65	4.52	0.25
1.	3.26	8.59	66.0	.71	1.90	6.79	.02	74	1.86	5.55	0.46
- 0	2.76	8.00	93	.82	2.07	6.32	.37	.82	2.12	5.07	001
00	2.54	7.75	.78	.87	2.07	6.12	.13	.87	2.13	4.46	0.34
0.0	1.96	7.00	• 43	0.0	1.802	6.18	53	200	1.89	5.12	0.38
0	1.71	7.73	.45	000	1 . 66	6.39	.80	000	2.05	4.38	. 53

Table 15.1. Continued.

***	> %	BETA Y DEG	BETA R DEG	X/SS	> \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	BETA Y	BETA R DEG	*/ss	> \	BETA Y DEG	BETA S
PHH=40 YOP/SR=	00.0=			PHH=50 YOR/SR	00 00 = 0			PHH=50 YOR/SP	-00		
000	21.618	43.466	0.551	0.001	20.545	41.928	-0.362	-0.000	20.640	41.854	0.527
103	1.62	010	.56		0.65	2.66	.02		0.62	1.89	-11
.154	1.38	3.72	66.	• 15	0.53	2.24	600	• 15	0.65	2.37	• 02
050	1.31	4.09	200	200	0.50	2.09	984	000	70.0	3.31	000
308	0.93	3.76	81	30	0.59	2.20	45	30	0.94	2.96	7.3
.360	1.19	4.56	1.26	.35	0.38	2.32	.27	.33	1.38	4.97	.84
.386	66.0	3.71	19	14.	0.33	1.77	.63	35	1.52	6.04	000
4 37	1.1	3.39	0.86	4 4	0.73	2.76	.37	. 41	1.24	5.06	.68
.463	1.07	7.02	.15	.51	99 .0	3.28	.32	.43	1.35	6.33	• 19
.489	1.10	1.43	.12	.54	1.15	6.41	. 25	• 46	1.08	4.47	. 59
.515	6001	6.35	• 29	.556	0.93	0.68	98	. 48	1.43	1.96	300
566	0.83	0.77	78	.61	1.53	6.38	.26	53	48.0	8.03	81
.592	9.51	8.86	. 52	.64	1.18	4.78	. 25	.56	0.46	6.37	00.
•617	9.81	7.65	• 95	• 66	0.83	3.78	.70	• 59	0.26	6.57	• 37
.643	9.49	6.42	99	690	0 - 20	3.40	· 04	19.	0.36	5.95	8 6
699	9.50	3.14	200	770	70.6	1 • 5 • 5 • 6 • 6 • 6 • 6 • 6 • 6 • 6 • 6	970	604	9.93	2000	200
722	62.6	6.63	67	77	9.52	9.19	03	69	9.75	4.61	40
.745	0.37	5.53	. 25	.79	9.22	7.45	99.	.71	9.64	4.05	50.0
.771	16.0	5.54	1.21	.82	44.6	6.02	. 25	. 74	9.63	3.71	0.75
.798	16.0	3.95	.10	.84	09.5	3.99	69.	.77	89.6	3.50	• 49
.823	1.08	3.25	0.29	.87	9.57	3.29	0.20	.82	9.81	2.31	0.40
.874	1 . 45	3.77	0.28	.89	0.07	3.04	0.88	.87	0.19	2.28	0.01
925	1.48	3.25	. 86	. 92	0.16	2.92	640	92	0.31	1.69	33
	1000	3.41	200		000	2000	0.0		0.00	2003	200

ETA F 8 > G BETA DE(69.0= >> 58 SR X/S PHH= TA P 86 000-4 W W W 4 V N H O H H O H O H O O O O O O O O × 5 TA ATION BE. > × 20 000 . 11 PHH=50 YOR/SR: 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.0000 0.000 0.00 Ś 1 BETA R DEG 5 BETA 0mr40m0rm0nn00m00004nm0m0n-0-0 -000 >> PHH=50. 55

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Continued

15.1.

a o ET A DE 8 20 BETA DEC 00 >> 000= 20 AS PHH= S/1 2 5 TA BE -00-0-0-0-0-M&WWWWWW-00-0-000 20 BETA DE ATION > \ 00 000= PHH=60 YOR/SP= 58 1 TA R BE ¥ 9; BETA DEC > 3 83 000= PHH=50 55 >

Fable 15.1. Continued

Table 15.1. Continued.

	BETA R DEG		.79	. 41	0.819	66.	99.	.25	.82	.57	.87	. 41	.37	. 12	.94	. 70	.70	.27	. 70	.45	.03	• 24	.33	.65	.83	.06	06.	.74	-	.08	. 84
LION 3	BETA Y		2.70	3.30	43.759	2.24	0.01	0.07	0.82	0.29	9.74	2.01	5.09	3.46	4.92	4.14	9 * * 9	5.66	2.90	99.0	2.27	5.35	1.82	69.6	6.34	4.66	3.82	1.72	8.74	6.37	0.51
STAT	χ < S	00 • 0 = 0	8.13	7.48	17.032	7.02	7.44	7.59	8.05	8 45	8.60	9.14	9.02	9.33	9.51	9.38	0 - 50	09.6	9.57	6.63	9.23	2.47	9.32	9.15	8.87	16.8	9.03	8.66	8.30	7.94	7.93
	Y/SS	PHH=90 YOR/SR	00.	• 05	0.100	.20	. 25	.30	.36	• 41	•46	.51	.54	.56	.59	.61	.64	.66	59.	.71	.74	.77	610	.82	.84	.87	.89	.92	.95	16.	00.
	BETA R DEG		.43	. 40	1.725	.64	• 36	.01	.75	16.	.95	.54	.00	.38	.72	.62	.68	96 .0	06.	1.78	. 40	.01	.63	. 74·	.21	.17	.01	.78	. 98	69.	• 04
	BETA Y		2.86	1.87	40.803	8.04	8.35	6.80	7.81	1.94	7.55	7.35	7.79	2.96	90 .5	7.40	6.65	1.75	4.45	8.73	96.6	1.27	1.29	7.93	8.76	6.28	2.55	3,33	1.56	1.40	1.76
	× × × × × × × × × × × × × × × × × × ×	0000	8.74	8.58	10000	8.57	8.55	8.74	8.88	10.6	9.14	9.27	6.47	9.52	9.78	61.6	0.02	0.35	99.0	0.77	0.55	0.64	0.39	60.0	16.6	9.55	9.31	9.33	9.02	8.93	0.12
	x/.88	PHH=80 Y0R/SB	.00	• 0 5	0.104	.20	.25	.30	.36	.41	.46	.51	.53	.56	.59	.61	.64	999	69.	.72	.74	.77	.79	.82	.84	.87	.89	.92	.95	26.	00.

Table 15.1. Continued.

					STA	STATION 4					
X/ SS	> > %	BETA Y	BETA P	×/88	× × ×	BETA Y	BETA R DEG	Y/55	M/S	BETA Y DEG	BETA P DEG
PHH=50 YOR /SR	00.0=			PHH=50 YOR/SR	0000			PHH=50 YOR/SR	0.00		
000	8.42	0.84	76	000	8.66	3.50	. 88	000	8.33	2.04	57.
• • • • • • • • • • • • • • • • • • • •	200	2.18	19	- 100	7.96	0 4 u	78	122	7.26	2.001	222
12.0	6.95	3.84	82	200	6.39	50.00	444	20	5.40	2.00	20
23	5.05	5.48	400	23	4.89	6.20	.96	.23	3.80	1.91	.10
258	3.26	4.66	.01	288	3.45	3.53	1.19	.28	3.55	1.60	0.74
33	3.69	2.30	52	33	3.25	20.02	24	33	3.24	9.71 8.53	.51
38	5.28	9.58	0.00	.38	4 · 82 5 · 19	0.89	1.25	41	5.29	9.30	63
444	5.78	2.54 2.54 2.54	. 50 . 15	444	5.52 5.67 5.85	2.91 2.93 3.93	95	48 51	5.73 5.90 6.00	0.56 1.44 1.18	.21 .35
556	5.90	3.42	75	55	5.89	3.56	889	56	6.16 6.30 6.70	0.44	000
27.	6.982	2.16	36	727	6.60	1.42	61	.72	6.81	0.91	93
0.873 0.923 0.925 1.001	17.272 17.414 17.688 17.900	28.898 29.128 30.355 31.239	2.053 2.053 2.053 2.053 2.053	0000 0000 0000 0000 0000	17.424 17.467 17.774 18.070	32.624 31.900 33.262 33.317 33.550	2.032 2.032 2.032	0000 0000 0000 0000 0000	17.533 17.933 17.971 17.904	32.271 32.771 32.798 31.526	0.975 0.975 1.324 1.328

ET B > O BETA > \ 0 =000 50 SP X/S PHH= α υ 0000 BETA > G BE TA DE(STATION 0-01-01-00000-04-000040000-000010 > W -00 PHH=50 YOR/SR: S 0000000000000000000000000 80 BETA DEC > ETA) m >> 00 PHH=50 YOR /SR: Y / SS 00000000000000000000000000

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Continued Table 15.1.

EG F

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Table 15.1. Continued.

					STA"	ATION 5						
¥7.88	> \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	BETA Y	BETA P DEG	* /\$\$	> \$	BETA Y	BETA R DEG	×7.5 S	> \	BETA Y DEG	BETA R DEG	
PHH=50 YOR/SP	0 • 0 0 R = 0 • 0 0			PHH=50 YOR/SR	0.00			PHH=50 YOR/SR	-000			
0.001	20.980	41.810	-1.271	0.053	20.943	41.210	-0.836 -1.090	0.027	20.566	43.660 44.891 45.640	0.158	
	0.37	2.29	-1.02	.15	0.20	0.0	0.93	.07	0.23	6.44	.63	
101	06.6	2.76	-0-	. 25	0.10	4 4	0.4.5	112	96.00	6.80	0.0	
. w	0.63	4.57	0.95	30	0.34	50.00	.55	18	0.10	8.87	.03	
44	0.40	5.38	1.44	.33	0.28	8.0	. 29	.23	9.87	5.91	.71	
4 1	1.004	1.07	1.64	.38	0.33	6.5	.25	.25	9.61	9.19	94	
S. R.	0.01	8.31	3.48	43	0.23	100	414	330	9.40	7.83	000	
30	96.0	9.09	4 . 22	4 4	0.62	40	25	36	09.0	2.09	64	
9	1.26	5.16	2-10	54	1.03	100	22	41	0.53	6.82	000	
9	16.0	9.30	1.54	.59	0.83	6.6	.87	46	0.63	4.82	. 85	
	1.00	8.09	1 . 30	.61	0.98	5.9	0.23	.51	0.65	4.47	.69	
	46.0	5.84	0.01	• 66	0.83	5.8	.02	19.	0.79	5.00	.02	
. 80	1.18	5.32	-0.86	.72	0.68	4.3	0.26	.23	0.62	3.84	38	
0 0	1.01	3.91	-0.51	. 82	0.65	3.4	.42	. 82	0.85	3.02	. 38	
000	0.89	2.67	-0-16	-87	0.82	2.	99.	-87	0.49	2.99	.08	
2.0	66.0	1.97	-0.82	100	0.0	200	.33	16.	9.95	5.24	000	
0	1.23	2.10	-1.34	000	0.65	2.6	.39	00	9.83	5.81	.35	

EG F ET 8 > PE BE > > 000= PHH=50 Y0F/SR= S X/8 000000000000000000000000 a U A W FO 8 × 5 5 TA ATION BE > × 67 0 . 00 50 SR 55 PHH= a 5 TAP BE. > BETA -000 >> PHH=50 YOR /SR: 55 0000000000000000000000000

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rable 15.1. Continued.

Table 15.1. Concluded.

VYSS V BETA Y BETA R VYSS V BETA Y FETA R VYSS VV BETA P BETA R VYSS W/S BETA R PETA R PETA R PETA R W/S DEG						STA	STATION 6					
HH=50.00 ONE / SR = 0.00 ONE / SR = 0.	15	>\	ETA	ETA	15	>\	TA	ETA	¥/85	>\	ETA	E O
0.00 15.915 29.685 1.917 0.001 16.143 33.095 3.219 -0.000 16.364 29.078 0.26 0.022 16.5348 31.563 31.997 0.052 16.582 33.527 1.981 0.027 16.703 29.43 0.46 0.052 16.583 31.563 31.997 2.568 0.077 16.736 33.313 0.650 0.077 17.016 29.589 0.275 1.27 0.650 0.077 17.016 29.645 0.991 10.27 0.651 0.31.777 2.758 0.077 16.736 33.313 0.650 0.077 17.016 29.645 0.991 0.092 0.09	HH=5 0R/S	000=			HH=5 0R/S	• 00 =			HH=5 OR/S	000=		
16.510 31.777 2.758 0.077 16.736 33.313 0.650 0.077 17.016 25.589 1.27. 15.4 16.5513 31.777 2.526 0.192 17.032 33.122 0.156 0.102 17.146 25.459 0.591 1.511 1.523 32.997 2.526 0.192 17.102 32.397 2.526 0.192 17.102 32.268 0.1065 0.105 17.146 25.459 0.591 1.511 33.232 1.397 2.526 0.154 17.275 33.2268 0.1065 0.105 17.393 25.685 2.18 3.296 17.396 2.206 17.396 2.206 17.396 2.206 17.398 31.753 0.444 0.309 17.966 29.486 0.710 0.306 17.558 30.074 3.19 3.19 3.19 3.19 3.19 3.19 3.19 3.19	000	5.91	9.68	90	000	6.55	3.52	98	000	6.36	9.04	26
15.5 16.652 31.977 2.658 0.129 17.275 32.268 -0.085 0.205 17.239 29.077 1.518 31.753 32.969 2.171 0.154 17.275 32.268 -0.085 0.205 17.393 29.685 2.18 2.58 0.560 0.205 17.264 3.199 3.	0	6.51	1.7	75	0	6.73	3.31	65	20	7.01	5.58	27
206 16.778 32.969 2.171 0.154 17.275 32.268 -0.085 0.205 17.393 29.685 2.18 32.86 17.369 30.074 3.19 30.87 31.34 0.255 17.564 31.451 0.307 0.356 17.369 30.074 3.19 31.83 32.28 0.644 0.309 17.960 29.646 0.710 0.360 17.569 30.074 3.19 31.851 17.588 31.753 0.444 0.309 17.960 29.258 17.564 32.008 17.569 32.079 2.92 31.758 31.753 0.444 0.309 17.968 29.258 1.512 0.462 17.569 32.079 2.92 453 17.883 29.825 0.386 17.564 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.560 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.564 32.008 17.560 29.497 0.253 0.360 17.724 28.528 1.759 0.515 17.786 31.968 2.25 32.456 29.07 -0.253 0.556 17.709 2.077 0.518 18.070 32.345 0.14 2.52 17.76 29.07 0.515 17.76 29.077 0.518 18.070 32.345 0.14 2.52 17.76 29.077 0.518 18.070 32.345 0.14 2.52 17.76 29.077 0.518 18.070 32.345 0.14 2.52 17.76 29.07 0.518 17.74 29.07 0.518 18.070 32.345 0.14 2.52 17.74 29.07 0.518 17.74 29.07 0.518 18.070 32.345 0.14 2.52 17.74 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.34 29.07 0.518 17.318 31.511 1.218 17.35 29.07 0.0745 17.318 31.511 1.218 17.35 29.07 0.0745 17.318 31.511 1.218 17.35 29.07 0.0745 17.318 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07 17.07 0.0745 17.52 29.07 0.0745 17.52 29.07 0.0745 17.52 29.07	::	6.65	2.99	. 65	.12	7. 10	2.87	.29	. 15	7.23	2006	. 51
368 17.523 322.258 0.560 0.257 17.967 30.482 0.307 0.308 17.558 30.774 3.10 0.308 17.552 322.258 0.560 0.360 0.77960 29.646 0.710 0.360 17.608 32.079 2.92 463 17.981 31.753 0.444 0.309 17.928 29.054 1.212 0.461 17.652 32.426 3.00 463 17.991 0.462 17.724 28.528 1.512 0.441 17.552 32.426 3.00 463 17.824 30.081 0.171 0.462 17.724 28.528 1.512 0.461 17.562 32.426 3.00 463 17.726 30.151 0.253 0.441 17.726 29.057 0.515 17.726 31.968 2.25 42.00 42.17 0.253 0.491 17.726 31.968 17.726 31.968 17.726 31.968 17.726 31.961 0.253 0.661 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.515 17.726 29.497 0.517 17.530 31.611 3.088 0.645 18.23 31.838 0.10 4.42 17.791 31.838 0.10 4.42 17.791 31.838 0.10 4.42 17.791 31.838 0.70 3.2291 0.34 17.791 31.838 0.70 3.2291 0.34 17.791 31.70 0.773 31.511 1.21 1.21 1.21 1.21 1.21 1.21 1.21	30	7.13	2.96	12	.15	7.27	2.26	.08	200	7.39	99.5	100
463 17.788 31.753 0.444 0.309 17.990 29.646 0.710 0.350 17.606 32.079 2.946 463 17.988 31.753 0.444 0.309 17.998 29.654 1.512 0.462 17.652 32.426 3.00 463 17.883 29.825 0.382 0.411 17.923 29.054 1.512 0.462 17.652 32.426 3.00 516 17.856 30.081 0.171 0.462 17.724 28.528 1.759 0.515 17.786 31.968 2.25 32.008 30.051 17.256 30.051 17.256 30.051 1.7706 29.070 3.0568 17.796 31.968 2.25 32.90 1.00 29.407 -0.253 0.565 17.706 29.070 0.515 17.786 31.968 2.25 32.393 0.146 52 17.256 30.057 0.516 17.256 30.070 32.393 0.16 11 3.088 0.645 18.235 31.838 -0.16 6.996 28.941 -0.5575 0.6594 17.550 31.442 3.533 0.668 17.951 31.281 0.34 5.99 33.533 0.668 17.951 31.281 0.34 5.99 33.533 0.658 17.951 31.713 0.47 16.896 28.941 -0.5575 0.694 17.549 31.542 0.694 17.912 31.551 0.34 5.99 33.539 0.724 17.318 31.713 0.47 16.895 29.067 -1.140 0.720 17.365 32.993 33.979 0.777 16.773 31.511 1.21 0.34 5.99 33.379 0.777 16.773 31.511 1.21 0.595 29.067 -1.140 0.797 16.896 23.359 0.797 16.229 32.369 0.893 33.79 0.797 16.229 32.369 0.893 33.79 0.797 16.229 32.369 0.893 33.79 0.797 16.229 32.369 0.893 33.527 31.221 -0.714 0.823 13.954 37.744 2.961 0.824 14.466 33.176 -0.668 12.384 32.710 -3.346 0.874 12.884 32.727 -2.822 0.899 13.159 32.266 -1.557 0.900 13.270 25.159 -3.44 92.266 13.727 -2.822 0.899 13.159 32.266 -1.557 0.900 13.270 25.159 -3.44 0.823 13.642 31.290 -1.595 0.955 13.894 29.30 0.951 14.894 29.31 14.553 30.041 0.12 37.743 -2.05 32.000 15.355 30.041 0.12 30.041	mi	7.52	2.25	56	.25	7.86	0.48	30	30	7.55	77.0	100
463 17.834 29.825 0.382 0.411 17.924 28.528 1.512 0.462 17.786 31.968 2.25 516 17.824 30.081 0.171 0.462 17.724 28.528 1.759 0.515 17.786 31.968 2.25 560 17.756 30.151 0.565 17.690 30.707 2.077 0.565 18.023 31.948 3.838 0.645 18.023 31.838 0.148 32.353 31.838 0.148 0.546 17.838 31.842 33.83 0.665 17.838 31.838 0.645 18.235 31.838 0.645 18.235 31.838 0.148 0.348 <td>E 4</td> <td>7.99</td> <td>1.75</td> <td>400</td> <td>30</td> <td>7.96</td> <td>9.64</td> <td>51</td> <td>.36</td> <td>7.56</td> <td>2.00</td> <td>38</td>	E 4	7.99	1.75	400	30	7.96	9.64	51	.36	7.56	2.00	38
516 17 824 30.081 0.171 0.462 17.724 28.528 1.759 0.515 17.785 31.908 2.225 31.908 31.209 2.225 31.908 31.209 2.225 31.908 31.209 2.225 31.908 31.209 2.225 31.209 3	4	7.83	9.85	. 38	. 41	7.92	9.05	-21	.46	7.65	2.42	.00
620 17-260 29-497 -0-253 0-566 17-690 30-707 2-077 0-618 18-070 32-393 0-14 642 17-176 29-007 -0-160 0-617 17-530 31-611 3-088 0-645 18-235 31-838 -0-16 642 17-176 29-007 -0-160 0-617 17-530 31-611 3-088 0-645 18-235 31-838 -0-16 644 17-176 29-007 -0-160 0-6575 0-669 17-644 31-783 0-694 17-791 31-661 0-38 649 16-893 28-943 -0-575 0-6575 0-694 17-544 31-783 0-694 17-791 31-661 0-38 640 16-893 28-962 -1-286 0-720 17-36 32-993 3-908 0-724 17-791 31-651 0-39 640 16-893 28-962 -1-286 0-720 17-32 33-984 4-920 0-773 16-229 32-244 0-60 641 16-895 29-067 -1-140 0-771 16-033 33-984 4-920 0-773 16-229 32-244 0-60 642 17-71 15-695 29-067 -1-140 0-720 17-32 33-984 4-920 0-773 16-229 32-369 0-83 643 13-727 31-749 0-848 13-954 37-744 2-961 0-874 14-466 33-176 0-669 644 17-71 15-895 13-159 13-951 13-951 11-185 0-846 13-120 30-118 0-699 645 12-815 32-545 -1-769 0-848 13-159 32-266 1-557 0-900 13-20 30-118 0-699 646 13-645 31-749 0-951 14-894 29-371 1-1857 0-901 13-791 27-743 -2-05 647 16-343 30-273 2-401 0-976 15-038 32-613 2-060 1-000 16-355 30-041 0-12	o r	7.75	0.08	0.58	940	7.72	9.63	81	56	8.02	2.45	.03
670 16.996 28.941 -0.575 0.6691 7.550 31.911 3.088 0.668 17.553 31.835 -0.34 6.868 17.952 32.291 0.34 6.941 16.996 28.941 -0.587 0.6694 17.544 31.783 3.383 0.6694 17.791 31.661 0.34 6.941 16.983 29.443 -0.587 0.720 17.365 32.993 3.908 0.724 17.791 31.661 0.34 7.751 16.703 28.962 -1.286 0.720 17.365 33.976 0.724 17.791 31.613 0.47 7.71 15.695 29.067 -1.140 0.771 16.033 33.379 0.773 16.229 32.294 0.60 0.771 15.695 29.067 -1.140 0.771 16.033 33.984 4.920 0.773 16.229 32.244 0.60 0.823 13.727 31.721 -0.714 0.823 13.954 37.744 2.961 0.824 14.466 33.176 -0.665 848 13.954 32.577 4.2961 0.824 14.466 33.176 -0.665 873 12.384 32.710 -3.346 0.824 13.155 0.874 12.815 0.874 12.921 30.941 -1.53 0.925 13.994 29.371 1.1557 0.990 13.270 25.159 -3.44 0.955 13.994 29.371 1.1557 0.990 13.270 25.159 -3.44 0.955 13.994 29.371 1.1557 0.995 13.774 25.328 0.945 0.955 13.994 29.371 1.1532 0.995 13.774 25.358 0.946 0.957 15.343 30.245 0.955 13.0976 15.835 30.041 0.12	9	7.26	9.49	0.25	.56	7.69	0.70	.07	.61	8.07	2.39	. 14
694 16.883 29.443 -0.587 0.694 17.544 31.783 3.536 0.694 17.791 31.661 0.38 725 16.703 28.962 -1.286 0.720 17.365 32.993 3.908 0.724 17.318 31.713 0.47 16.229 31.5713 0.47 16.229 32.244 0.60 0.771 16.033 33.379 0.777 16.229 32.244 0.60 0.771 15.695 29.067 -1.140 0.771 16.033 33.994 4.920 0.777 15.299 32.244 0.60 0.823 13.727 31.721 -0.714 0.823 13.954 37.744 2.961 0.824 14.466 33.176 -0.666 848 12.815 32.545 -1.769 0.848 13.036 37.726 1.185 0.848 13.120 30.318 0.879 1.185 0.879 12.801 3.2.921 30.941 -1.53 0.879 12.801 34.397 -0.781 0.874 13.120 30.118 0.659 0.874 12.801 34.397 -0.781 0.874 13.120 30.118 0.659 0.874 12.801 34.397 -0.781 0.874 13.120 30.118 0.659 0.874 12.801 34.397 0.978 13.200 13.270 25.139 -3.44 0.950 13.270 25.139 -3.44 0.950 13.270 25.139 0.925 14.684 30.245 0.955 13.991 29.756 -0.953 0.9951 14.789 26.238 -0.12 0.951 14.789 26.238 -0.12 0.977 15.343 2.200 13.274 0.976 15.803 31.749 3.159 1.000 16.338 32.613 2.060 1.000 16.355 30.041 0.12	00	66.9	8.90	0.10	199	7.53	1.001	300	• 66	7.95	2.29	34
725 16.703 28.952 -1.286 0.720 17.355 32.993 3.998 0.724 17.318 31.6713 0.474 16.214 28.775 -0.773 0.745 17.127 33.763 3.379 0.747 16.773 31.6713 0.475 17.127 31.625 32.244 0.60 0.771 15.298 32.349 0.60 0.773 16.229 32.244 0.60 0.796 14.959 30.155 -0.651 0.797 15.298 32.369 0.83 13.727 31.721 -0.714 0.823 13.954 37.744 2.961 0.824 14.466 33.176 -0.66 881 13.727 31.721 -0.714 0.823 13.954 37.526 1.185 0.848 13.120 30.118 0.659 87.12 384 32.710 -3.346 0.874 12.801 34.397 -0.781 0.874 12.921 30.941 -1.53 0.951 14.684 30.245 0.955 0.925 13.991 29.756 -0.953 0.926 13.791 27.743 -2.055 0.955 14.684 30.245 0.955 0.951 14.894 29.371 1.195 0.951 14.789 28.238 -0.12 977 15.343 30.273 2.401 0.976 15.707 30.717 1.532 0.976 15.649 25.358 0.46 0.951 14.000 15.809 31.749 3.159 1.000 16.38 32.613 2.000 1.000 16.355 30.041 0.12	9	6.88	9.44	0.58	69.	7.54	1.78	.53	69.	7.79	1.66	.38
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9823 13.727 31.721 -0.714 0.823 13.954 37.744 2.941 0.6797 13.529 32.539 0.656 8823 13.727 31.721 -0.714 0.823 13.954 37.744 2.941 0.824 14.466 33.176 -0.666 8848 12.384 32.727 -2.346 0.874 12.801 34.397 -0.781 0.874 12.921 30.941 -1.53 900 12.775 32.727 -2.822 0.899 13.159 32.266 -1.557 0.900 13.270 25.159 -3.44 925 13.642 31.290 -1.595 0.925 13.991 29.756 -0.953 0.926 13.791 27.743 -2.05 952 14.684 30.245 0.554 0.951 14.894 29.371 1.196 0.951 14.789 28.238 -0.12 977 15.343 30.273 2.401 0.976 15.707 30.717 1.532 0.976 15.649 25.358 0.46	1.1	5.69	9.00	1.14	.77	6.03	3.98	. 92	1.	6.22	2.24	.60
848 12-815 32-545 -1-769 0.848 13.036 37-526 1.185 0.848 13.120 30.118 0.69 873 12-384 32-710 -3.346 0.874 12-801 34.397 -0.781 0.874 12-921 30-941 -1-53 900 12-775 32-727 -2.822 0.899 13.159 32-266 -1.557 0.900 13-270 25-159 -3.44 925 13-642 31-290 -1-595 0.955 13-991 29-756 -0.995 0.992 13-791 27-743 -2-05 952 14-684 30-245 0.554 0.951 14-894 29-371 1.196 0.995 14-789 28-238 -0-12 977 15-343 30-273 2-401 0.976 15-707 30-717 1.532 0.976 15-649 25-358 0.46	. "	3.70	1.72	710	000	3.05	7.74	900	82	4.46	3.17	. 66
•873 12•384 32•710 -3•346 0•874 12•801 34•397 -0•781 0•874 12•921 30•941 -1•53 400 12•775 32•727 -2•822 0•899 13•159 32•266 -1•557 0•900 13-270 25•159 -3•44 255 13•642 31•2920 -1•595 0-955 13•642 31•200 -1•595 0-955 13•642 30•245 0-955 14•684 30•245 0•554 0•951 14•894 29•371 1-196 0•951 14•789 28•238 -0•12 0977 15•343 30•273 2•401 0•976 15•707 30•717 1-532 0•976 15•649 25•358 0•46 000 15•809 31•749 3•159 1•000 16•038 32•613 2•060 1•000 16•355 30•041 0•12	0	2.81	2.54	1.76	.84	3.03	7.52	.18	. 84	3.12	0.11	69.
900 12-775 32-727 -2-822 0-899 13-159 32-260 -1-557 0-900 13-770 25-159 -3-48	8	2.38	2.71	3.34	-87	2.80	4.39	0.78	-87	2.92	46.0	1.53
952 14.684 30.245 0.554 0.951 14.894 29.371 1.196 0.951 14.789 28.238 -0.12 977 15.343 30.273 2.401 0.976 15.707 30.717 1.532 0.976 15.649 25.358 0.46 •000 15.809 31.749 3.159 1.000 16.038 32.613 2.060 1.000 16.355 30.041 0.12	20	300	1.20	200	00	2.00	9.75	0.95	000	3.79	7.74	2.05
•977 15•343 30•273 2•401 0•976 15•707 30•717 1•532 0•976 15•649 25•358 0•46 •000 15•809 31•749 3•159 1•000 16•038 32•613 2•060 1•000 16•355 30•041 0•12	0	4.68	0.24	0.55	.95	4.89	9.37	119	.95	4.78	8.23	0.12
• 000 15.809 31.749 3.159 1.000 16.038 32.613 2.060 1.000 16.355 30.041 0.12	6.	5.34	0.27	.40	.97	5.70	0.71	.53	.97	5.64	5.35	. 46
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					STAT	ATION 3		
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PHH=50.	00			PHH=50 YOR/SR	69.00			
.001	0.74	2.44	966	000	9.28	3.96	. 51	
181	0.86	1.72	31	701	9.57	7.33	40	
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308 335 359 386	1.55 1.19 1.25 1.31	5.78 5.90 3.84	900 900 900	.30 .35 .41	0.91 0.81 0.89	3.58 2.98 3.12 2.91	. 34 . 17 . 07 . 0	
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0.619 2	00000	42.959 42.752 42.768 41.739	0.997 0.200 0.200	0.796 0.823 0.849 0.875	19.813 19.224 18.663 18.355	44.326 45.726 45.700 55.603	0 125 0 716 1 166 2 786	
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